# VALVES AND VALVE GEAR MECHANISMS

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#### BY

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### PREFACE.

VALVE gear mechanisms have fasemated successive generations of engineers, and, it the truth were known, there are few mechanical engineers who have not at some time or other fired to invent a new geat. In consequence, the number of valve gears described in the Patent Office Specifications, and indeed the number of different types which have been actually made, is exceedingly great. My object is not to enumerate these, nor even to enumerate all the types which are in actual work at the present time, but rather to select a few typical gears, well tried, and to some extent representing the survival of the fittest types, and to examine their thoroughly and by methods which may generally be applied to all kinds of gear similar to those chosen.

The scope of this volume is limited to an examination of types of those gears in which there is one, and only one, position of the valve for a given position of the crank. In other words, the position of the valve is a function of a single variable only, namely the crank angle. A few gears are however described modenfully in which a governor is included in the mechanism operating the valve. In this case there is more than one position of the valve for a given position of the crank. The valve position is, in fact, a function of two variables, namely the crank angle and the time, and the valve position cannot be set out on a drawing from kinematic considerations alone. The proper examination of gears of this kind requires a study of the dynamics of governors, and this is not included in the present volume.

The matter is arranged so that those who prefer the graphical to the analytical method may obtain all the useful technical information regarding the gears examined without reading the analytical articles, and so that students of technical colleges may begin the study of the subject in their first year, cantinuing with the later portions of the book in their second and third years. With this purpose in view the first five chapter, include the descriptive matter relating to valves and the discussion of the distribution of steam effected by the simple eccentric gear, the problems in connection therewith being treated by drawing-

board methods alone. Chapter VI covers the same ground as Chapters, III, 18 and V, but the trigonometrical method is substituted for the geometrical method used up to that point. Chapter VI is, in fact, an analytical summary of the previous chapters, and a study of it will show that there are plenty of useful trigonometrical exercises of an interesting kind to be obtained from valve gear mechanisms.

Chapters VII and VIII are devoted mainly to the subject of reversing Jeans and in these the preceding sequence of method is applied to each valve gear mechanism illustrated. That is to say, the properties of the gear are first investigated by drawing-board methods alone, and then the gear is subjected to an analytical examination from which rules are formulated by means of which the distribution of steam the gear can effect may be found approximately without the labour of drawing the actual displacement curves. In the analytical portions of these two chapters my indebtedness to Zeuner's classical work on Valge Gears, and to Rankine's work Machinery and Milluork will be apparent

Chapter IX is devoted principally to the exemplification of certain dynamical problems which arise in connection with high speed valve gears. The method used in the investigation of the acceleration of the parts of the gear is that communicated to the Royal Society of Edmburgh in 1885 by Professor R. H. Smith and further illustrated in Graphics by the same author The gear selected for detailed examination is the standard Joy gear of the Lancashire and Yorkshire Railway Company. Each link of a particular gear was made the subject of experiment at the Horwich Locomotive Works in order that its dynamical peculiarities might be ascertained, and the results of these oscillation experiments are stated in Table 12, p. 303. Without the co-operation of Mi Aspinall it would have been impossible to present such a complete practical example. There are various other examples in the Chapter relating to dynamical problems in connection with the design of connecting and eccentric rods. This Chapter may he considered from two aspects- first, from the purely technical aspect in connection with the design of high speed valve gears, secondly, from the educational aspect, because all the principal theorems regarding the motion of a rigid body in a plane are involved in the working out of the technical problem discussed, and since these principles have a general application to mechanisms a student of the Dynamics of Machines may study this Chapter with advantage without necessarily acquiring a detailed knowledge of the previous chapters

Mithough the representation of the valve displacement by a Fourier series may not have an immediate application in the design of a valve agent, yet the method is exemplified in the last Chapter because of the

# Preface

increasing use which is being made by engineers of this powerful and searching method of analysis. Comparatively recently there was published in the Bulletin de la Novoité Internationale des Electroceus (Nov. 1901, Tome 1, 2de série) the Fourier series corresponding to the crank effort curves of 28 engines, each series being carried to 9 terms. The method is of enormous value in dealing with electrical problems. A brief discussion of the principles on which the Fourier method is based is associated with the examples to which the method is applied for the benefit of those who may not have the time to study the mathematical works devoted to the subject.

The valve diagram used throughout the book is the rectangular form generally known as the Osborne Reynold diagram. This diagram has many advantages, one of them being that a displacement curve is the graph of the equation representing 0 in rect nigular coordinates, so that the change from analysis to the diagram of view versa may easily be made at any time.

It is important to notice that all the valve diagrams in the book are drawn to represent the motion of the valve as it would appear to an observer looking at the engine from a position where the cylinder is seen to the left of the crank shaft. And further that what is called the zero crank position is that position of the crank in the line of stroke where the crank is seen to the right of the crank shaft. The positive direction of rotation from the position of the observer appears to be counter-dockwise.

It any valve diagram be given a quarter turn in the clockwise direction, the displacement curves will represent the movement of the valve in a marine engine

I am indebted to Mr J. A. F. Aspinall of the Lancashire and Yorkshire Railway for the drawings of the Joy gear and for other data, to M. Bosquet for the drawings of the Walschaert gear of the Northern of France engines, to Mr Chirchward for the drawings of the steam controlling gear used on the Great Western Railway, to Mr Holden for the drawings of the Great Eastern Railway link motion, and of the combined hand and power controlling gear, to Mr Malcolin for the drawings of the Walschaert gear used on the Belfast and County Down Railway, to Mr Sulzer for drawings of the Sulzer gear, to Mr F. W. Webb for the drawings of the Thumphry for the drawings of the marine type of link motion and slide valve, to Mr Yarrow for the drawings of the all-round type of controlling gear, and to many other English and American friends and firms for drawings and information, acknowledgements of which are made in the text

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Nearly all the valves illustrated and described can be seen as sectional models, and the valve gears as orking models, in the unique collection of engineeing apparatus which forms the Machinery Section of the Victoria and Albert Museum, South Kensington. This collection is the finest of its kind in the world. The models, which can be set in motion, are supplied with compressed air and can be started at will by the visitor. The models are usually small scale reproductions of actual rigines and machinery, and consequently show the details of construction used in practice. It is impossible to place too high an estimate on the educational value of this fascinating and magnificent collection.

I am specially indebted to Mr Wood Smith and to Mr Goodwin, formerly students at the City and Guilds Technical College Finsbury, for help in the reduction of the working drawings to suitable illustrations and in the drawing of the valve diagrams.

My grateful acknowledgements are also due to Mr C G Lamb for carefully and critically reading the proofs

There are a considerable number of fully worked examples distributed through the book, and I shall be grateful for notice of errors which remain uncorrected.

W. E. D.

CINIBAL TICHNICAL COLLIGI, December 1905.

#### ERRATA

For Mr. J. A. F. Aspinall road Sir John A. F. Aspinall For Mr. Yarrow — read Sir Alfred F. Yarrow For Walschaert — read Walschiefts

Nutr The Bellist and Northern Counties Railway amalgamated with the Midland Railway, July, 1903.

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# CHAPTER I.

#### THE CYCLE OF OPERATIONS

1. Definition of a valve gear. The commonest way of utilizing a fluid pressure for the performance of work is to arrange for it to act on a piston enclosed in a cylinder, the to and fro motion of the piston being maintained by the properly timed entry and exit of the fluid

The **valves** which are used to regulate this entry and exit are of many forms and are uranged in many ways, but whatever the form and however they are arranged the duty is the same, namely to admit, ent off, and release the fluid from the extinder at the proper instants.

A valve gear may be defined as a mechanism, operated by the engine itself, whereby the valves regulating the entry and exit of fluid to and from the cylinder are opened and closed.

The valve gears considered in this volume are those used in connection with steam engines

2. Dead points of piston. Stroke. Since all points in a piston motion at the same speed in parallel lines, the motion of the piston as a whole may be defined by the motion of any one of its points. The context will always indicate which point is chosen.

The points at the ends of the cylinder where the piston changes its direction of motion are commonly called **dead points**. At these points the piston is momentarily at rest. The **stroke** of a piston is the distance between its dead points.

3. The cycle of events in the steam distribution. An event of a stroke is the opening or closing of a valve controlling the entry or exit of steam.

Let the full lines, Fig. 1, represent a diagrammatic view of a steam engine cylinder and piston equipped with valves  $\mathcal S$  and

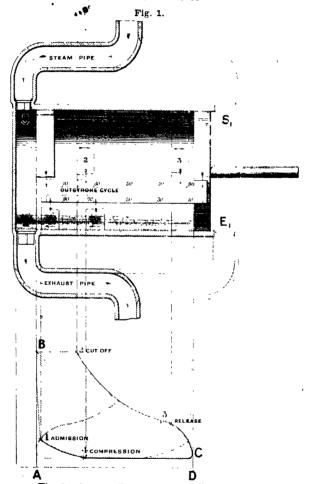


Fig. 2. Cycle of Events in a Steam Engine Cytinder

 $E,\ S$  controlling the admission of steam and E the exit to and from the chamber formed by the cylinder and the left-hand face of

the piston. No method is indicated of working these valves but it is to be understood that they can be opened and closed from outside at the right instants by appropriate mechanism. Fig. 2, below Fig. 1, is a diagram in which pressure is plotted vertically against the volume horizontally, the volume scale being such that the distance between the dead points of the evhider represents the volume displaced by the piston during a stroke.

**1st event. Admission.** Suppose the pist of to be moving towards the left dead centre. The steam valve S is opened for the admission of steam at the piston position marked 1 just before the piston reaches the left dead centre the meaning steam thus meeting and opposing the motion of the piston from the point 1 until it arrives at its dead point. By the time the piston urives at its dead point the whole space between it and the steam valve should be filled with steam at the steam pipe pressure its state as regards column and pressure being indicated by the cross at  $B_i$ , Fig. 2.

2nd event. Cut off. The piston orged by the steam pressure now moves towards the right hand dead point the valve 8 still being held open. The steam pipe should be made large enough to allow sufficient steam to enter the exhibiter to maint in the pressure fully constant as the volume is increased by the notion of the piston. At a certain point 2 the valve 8 is closed and the supply of steam cut off. The state of the steam as regards pressure and volume at this point is shown by point 2 in the pressure volume diagram, assuming the steam pipe to be large enough to admit sufficient steam to maintain the pressure constant as the volume is increased by the motion of the piston. From this point onwards the steam increases in volume is the piston moves towards its right-hand dead point and the pressure falls, though the weight of the steam in the cylinder remains constant providing.

- = 1 That none leaks away through the extract valve E;
  - 2 That none leaks by the piston ,
    - 3 That no fresh steam leaks in through the valve S,

In practice there is always a certain amount of steam lost by leakage. The missing quantity is fully discussed in the author's book Steam Power.

**3rd event. Release.** At the point 3, just before the juston reaches the right dead centre, the exhaust valve E is opened and the steam is released, escaping either to the atmosphere or to the condensing as the engine is of the non-condensing or condensing type.

The state of the steam as regards volume, ad pressure is shown by the point 3. Fig. 2. The pressure rapidly falls to the pressure in the exhaust pipe, and the release point should be arranged so that the pressure just about falls to this when the piston arrives at the dead point.

4th event. Compression. During the greater part of the return stroke, the valve E is held open, and a definite weight of steam escapes from the cylinder and the piston moves back against whatever pressure there may be in the cylinder. At a certain point 4, the valve E is closed and a definite weight of steam is shift in the cylinder. As the piston continues its motion beyond the point 4 towards the left dead point, the pressure of the steam gradually rises, until at 1, where the steam valve is opened, field steam is admitted and the steam pressure rises to the pressure in the steam pipe.

Thus in a cycle there are four events dividing the operations into four stages. The four stages may be summarised thus —

**Admission stage.** During the interval between admission and cut off, E is closed and S is open, and fresh steam is pouring into the cylinder

**Expansion stage.** During the interval between cut off and release both S and E are closed, a definite weight of steam is shut in the cylinder. As the volume increases the pressure falls, and PV, the product of the pressure and the volume is approximately constant until the exhaust valve opens.

**Release stage.** During the interval between release and compression, S is shut and E is open, and the steam is pushed out of the cylinder by the returning piston, the exhaust passages and pipe being large enough to prevent the steam increasing sensibly in pressure.

Compression stage. During the interval between compression and admission both S and E are closed, a definite quantity of steam is shut in the evhider, and as the volume decreases as the piston approaches the dead point, the pressure rises approximately according to the relation PV = a constant. The different positions of the piston for the four ewints are indicated by dotted lines, the arrows indicating the direction of motion

The cycle is considered to begin when the piston is at a dead point with the full steam pressure acting on it.

\*4. Nett work done by the steam during a cycle. The motion of the piston from the left dead point to the right is maintained by the action of the steam pressure, and the work done is represented by the area AB23CD in Fig. 2. The motion of the piston during the return.

stroke from the right to the left diad point must be maintained against the pressure of the steam in the cylinder, consequently work must be done upon the piston to the extent represented by the area DC41BA, Fig. 2. The work required for the return stroke may be drawn from

- The kinetic energy stored in the flywheel and the other moving parts of the engine;
- From the potential energy of weights raised during the outstroke.
- 3 From other cylinders draving the piston through the crank shaft,
- 4 From steam pressure acting on the right-hand face of the piston

The fourth is the general method in use. The second method was usual in the curby pumping engines. The first method is usual in internal combustion engines, and the third method is illustrated by high speed engines of the William type. Whichever method be used, the neft work done by the steam on the piston against all external resist ances on the right hand side of it during the complete cycle of events is represented by the difference between the areas above mentioned, that is by the shaded area. Fig. 2.

5 Single- and double-acting engines. An engine arranged to work as indicated in Fig. 2 is called a single-acting steam engine. In these engines, as just stated, there is always the peculiarity that the return stocke must be provided for by means external to the cylinder under consideration.

If a duplicate set of valves are arranged at the right-hand side of the cylinder, as shown by the dotted lines in Fig. 4, so that the steam passes through the cycle of events described in Art. 3, in the chamber formed by the right-hand part of the cylinder and the right-hand piston face, the engine is termed **double-acting**. This second cycle is **Seewi**n by dotted lines in Fig. 2.

6 Instroke and outstroke cycles. It is necessary to distinguish between the two cycles of a double-acting engine very clearly when considering the valve gear, and this is conveniently done by naming them the outstroke and instroke cycles respectively. The outstroke cycle is that one of the two which begins when the piston is on the dead point faithest from the crosshead. The instroke cycle begins on the dead contre nearest the crosshead. During the outstroke cycle it is pulling it in.

In this way the two cycles may be defined without ambiguity. If the cylinder be eplaced vertical, the dead points are distinguished by calling them the topion bottom dead point, but whether the crank shaft is above or below the cylinder there is no confusion regarding the cycles. A more general way to distinguish between the two cycles is by naming them with the value of the crank angle  $\theta$  at which they respectively begin. They would then be referred to as the cycle beginning when  $\theta = 0$  degree, or the cycle when  $\theta = 180$  degrees, or more briefly the 0 degree cycle and the 180 degree cycle respectively.

7. Specification of a cycle. An event of the cycle, though primarily determined by a valve, is usually fixed by stating the percentage position of the piston in its stroke at which the event takes place. A percentage scale is drawn on the diagram Fig. 1, placed so that its ends correspond with the dead points of the stroke. From this it will be seen that the four events specifying the cycle indicated in Fig. 2 may be fixed as follows.

Admission takes place at 98 per cent of the return stroke,

Cut off takes place at 25 per cent of the stroke,

Release takes place at 85 per cent, of the stroke,

Compression takes place at 69 per cent of the stroke

If the engine is double acting each cycle must be separately specified. The differences in the specifications are usually small.

#### CHAPTER II

#### ON STEAM DISTRIBUTING VALVES

8 General remarks. In the early divs of the steam engine the entry and exit of steam to the exhibit were controlled by separate valves. In double-uting engines these were duplicated so that there were four separate valves to be operated in order to control the two excles.

Murdoch patemed the Clorg D 'slide valve in 1799, a valve which combined the duties of the four separate valves of a double acting engine. By giving the valve a to and fromotion across suitably formed ports in the exhibit, the eight events of the two cycles were controlled by a single valve.

In 1802 Matthew Murray patented the short D" slide valve, a valve which was the same in all escentral particulars as the ordinary slide valve in use to-day

Both the long and the first D valve are described below the short D valve in the form in which it is 5, ed now in Art. 14, and the long D valve as Murdoch described it in his specification in Art. 20.

Though historically second, it will be concernent to describe the orderary slide valve before describing Mardech's valve.

After reading the articles decored to slide valves and their modifications a consideration of Merdoch's valve will how how little any of the modern valves differ in essential particulars from Mandoch's original design. The long D-valve permits the design of short straight steam ways into the cylinder, it is balanced and it is almost a piston valve.

About 50 years ago there was a return to the four separate valves of the early days of Watt. Many builders to day constructs agmes with four "drop valves" per cylinder. patented in America in 1851, an engin, which has been developed in this country by Messis Hick Hargieaves and Co. of Bolton in connection with the Spencer angles patents of 1863 and 1865.

Valves may be distinguished into 3 types.

- 1. Lift or "drop" valves, or those which open by lifting
- 2. Slide valves or those which slide across openings or ports.
- Rocking valves, or those which open ports by turning instead of by sliding.
- 9. Lift valves. The commonest kind of hit valve is that shown in Fig. 3, and known generally as a mushroom or mitre valve. When the valve is closed the conical part of the valve rests on a scating similarly coned. To ensure tightness the actual surface of contact between the valve and the scating, that is the space between the chain dotted lines A, B, should be nuriow, and the upper part of the conical surface of the valve may be backed off with advantage as shown in the figure. The valve is guided to its scating by easily fitting wings,

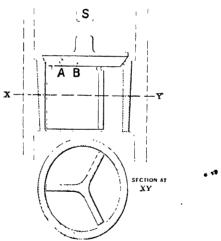


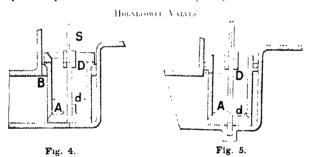
Fig. 3. MITRE VALVE.

shown in the plan, or a central spindle, and its upward motion or "litt" is hunted by a stop S. Theoretically, the valve is fully opened when the vertical cylindrical surface, measured by the product of the circumference of the valve and its litt, is equal-in area to the area of

the steam pipe in which the valve is placed or which the valve is required to supply. Practically, more lift than this should be given, otherwise the steam will drop in pressure during the passage through the valve, by an amount depending upon its velocity.

This type of valve is quite insuitable for use as a distributing valve for a steam engine because the force required to lift it against the steam pressures becomes impracticably large as the diameter of the valve and the magnitude of the steam pressure increase. For example, to lift an eight uich valve, which is about 50 square increase area, against a pressure of 200 lbs, per square inch requires a force of 10,000 lbs, weight

10 Double beat or equilibrium valve. This difficulty existed even with the moderate steam pressures used a century ago, and to surmount it Hornblower invented what is essentially an equilibrium valve about the year 1800. The arrangement is shown in Fig. 4, from which it will be seen that the valve is exhibitional in form and is provided with two scatings, one at A and the other at B. To lift the valve against a pressure p in the pipe S requires a force equal to the product of p and the difference of are is corresponding to the diameters.



D and d, of the valve scatings. There seemed to be difficulty in keeping the scats A and B simultaneously tight, because Tredgold describes what he calls an "Improved Horiblower Valve" where the upper seat B is replaced by piston packing as shown in Fig. 5. In this case the valve is lifted igainst a force measured by the product of the pressure in the pipe and the difference of are is corresponding to the full bore of the pipe D and the inner drameter of the valve d. In both types of Horiblower's valve steam pessed through the lower scattering to that the capacity to transmit steam was only the same as that of a mitre valve of equal diameter. A modern form of double beat valve is shown in Fig. 6 in place at one end of an engine cylinder.

It is provided with two seatings, A and B, arranged so that the steam

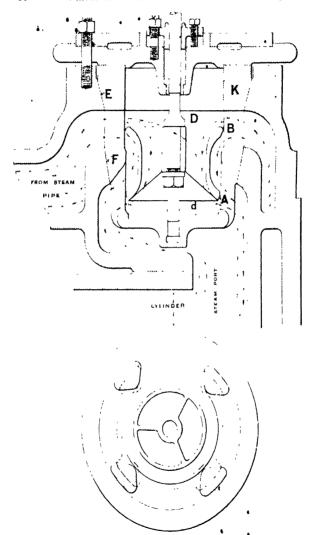


Fig. 6. Double Blar on Equilibrium Valve

has a clear passage through both when the valve is lifted. When closed the steam pressure acts on the difference of areas corresponding to the diameters d and D, that is an area equal to the projected area of the two seatings of the valve on a plane at right angles to the direction of lift.

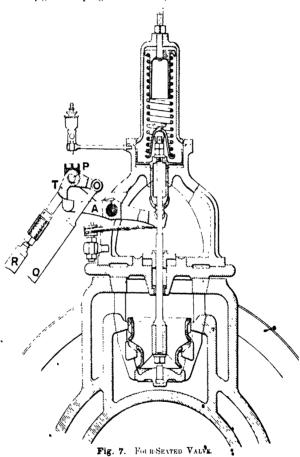
The diameters d and D in the case of the valve shown in Fig. 6 are respectively 7.5 and 8.2 inches, corresponding to a difference of area, 8.6 square inches. The pressure against which this valve has to be litted is thus 8.6 multiplied by the pressure in the steam pipe

For a given lift the opening to steam is equal to that obtained by two valves each 7.86 inches in drameter

The method of fitting the valve should be noted. The two valve scatings are formed in a cissing which his into two deep coincal scats E/F. The cover to this carries the stuffing box for the valve spindle. The study to holding the cover down are fixed into the main body of the cylinder easing so that when the nurs are so wed down the point is made at the cover and the casting in which the valve scatings are formed is held down on its coincal scats.

- 11 Four-seated valve. Fig. 7 shows a valve provided with four scatings. Here a large opening is obtained for a relatively small lift and the exertion of a relatively small force. The area acted upon by the steam pressure in this essential projected area of the four valve seatings. This valve and the valve shown in Fig. 6 are examples from a Sulzer engine, the details of which were limitly supplied by Messis Sulzer Brothers, Winterthur, Switzerland.
- Dashpot and spring. When valves of the double heat kind are used for the admission or exhaust valves of a steam engine they are usually operated by trip g at . That is to say the valve is litted off its seat and held open by means of a lever engaging with the spindle, and at the proper in tant for closing the level is released and \$1 · valve is free to drop on to its seat. Thus in Fig. 7, the rod R, operated by the engine mechanism in conjunction with the eatch or trigger P, engaging the least A is able to lift the valve off its seat. At the proper instant, the governor mechanism acting through the rod Q turns the trigger about the common pin P and the valve is free to drop. But when a valve of the kind under consideration is lifted off its seat it 8 m equilibrium as regards the steam pressures and special means must be taken to close it. Usually the valve is loaded with a spring, and to prevent the spring humbering the valve into its seat it is combined with a dashpot, so that the joint effect of the two is to urge the valve gently back into its seatings

without shock or hammering. The Sulzer combined spring and dashpole is shown in connection with the feur-seated valve, Fig. 7. The valve spindle is prolonged upwards and ferminates in a piston. During the upward motion of the valve and piston the spring is compressed and air is drawn in underneath the piston. When the valve is free from the trip gear, the spring as it closes the valve must at the same time



force the air out from beneath the piston through a small hand adjustable ball valve, so that the valve may be pressed into its searings almost without a sound

13 Effect of heat on double beat valves. It requires nice work to make a double beat valve properly. The difficulties he in the fact that two rigidly connected valves have to be made steam tight simultaneously. It is an easy matter to grind one valve into its seat.

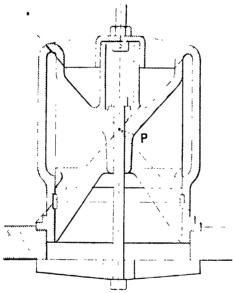


Fig. 8. Column V IVI

and make a good pole of it but to get two sears just right requires considerable skill. Another difficulty in connection with double heat valves is that when they get heated to the temperature of the steam in which they work, the small differences in expansion between the valves and seatings which inevitably occur make them leak although they may be perfectly tight when cold. In the best practice double beat steam valves are finally ground into the scattings at the temperature of the steam in which they are intended to work. Colinain endeavoured to get over the difficulty of unequal expansion by taking

\* Patent Specification, No. 1129 1877

advantage of the fact that if a cone expands under the action of heat, the angle of the cone remains constant. A Colmann valve is shown in Fig. 8. It will be seen that the cones forming the two seats have a common apex. Under the action of heat the scattings are supposed to increase slightly in diameter and to move proportionally further apart so that the cone angle remains constant. Assuming the valves to increase a little more in diameter than the seatings the respective rings of contact with the seatings will move a little faither apart than the seatings themselves. But masmuch as the cone angle is constant the rings of original contact on the valve will find a new surface of confact on the valve scatings. The point P may be taken in any position along the axis. When it is in the plane of either seat, that particular sent becomes horizontal. If the seats are parts of spherical surfaces having a common centre P, the valve will have additional freedom to accommodate itself to changes produced by change of temperature, These valves will leak of course if the valve or seatings distort from the truly circular form during expansion

The slide valve. General description. The general shape and arrangement of a slide valve and the steam ports across which if works are shown in Fig. 9. The two steam passages  $S_{ij}(S)$  connecting the cylinder with the steam chest are in the shape of flittened tubes formed in the exlinder wall itself. Then openings into the steam chest are shaped into narrow shits and ire brought close together. Lying between these openings is a wider shit which forms the entry to the passage  $E_i$ carrying the steam away from the cylinder to the condenser, the atmosphere of to mother cylinder in the case of compound engines This exhaust passage must be led away so that it clears the steam passages at is shown curving found the cylinder wall in the figure, appearing in cross section at  $\mathcal{L}_{i}$  . The three entrances to these passages the ports as they are called, are formed into long narrow slits lying close together in order that the valve which moves across them may regulate the different events of the two eveles by a relatively small to and to excursion across the ports, because the sliding of the valve has to be made against the frictional resistance produced by the steam pressure acting on its back. Figs. 9 and 10 are diagrammatic only

The slide valve V is shown lifted vertically off its seat, and from the section in the figure an idea of its shape can be obtained. It may be roughly described as a box lid with a flat rim. A rectangular frame  $B_i$  forged solid with the spindle  $D_i$  forming what is called the valve buckle, is dropped over the valve, and the two are placed in the steam chest  $C_i$  through the end cover  $G_i$  which may be removed for this purpose. The top steam chest cover  $H_i$  provided to enable the ports to be machined,

is put into its place and the valve is then enclosed in the steam chest but can be moved across the ports from outside by means of the valve spindle D. The valve is shown in its central position with regard to the ports in Fig. 10.

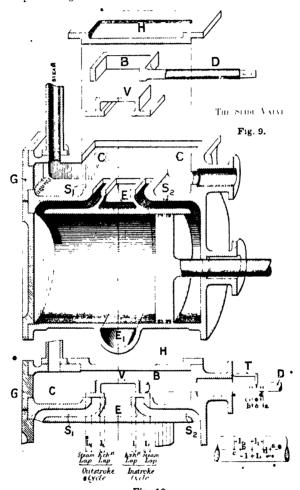


Fig. 10.

The valve is pressed upon its sear by the steam pressure acting upon it and honce wear is taken up autonotically. The valve must be a loose fit in the buckle in order to allow this action to take place, especially having regard to the fact that gun metal of which the valve is usually made, expands at a greater rate under the action of heat than the material of the buckle. There are other ways of connecting the valve spindle to the valve. The method illustrated is used in locometive practice.

To understand the action of the valve the section of pt shown in Fig. 10 should be re-drawn on a separate piece of paper or earl in order that it may be moved to the right or left of the central position shown in the figure. If this be done it will be observed that a sufficient movement of the valve to the right of the central position will put the left steam presize in communication with the steam chest whilst at the same time the right steam pieces is put in communication with the exhaust passage. A movement to the late will so reverse these connections that the right passage is in communication with the steam chest and the left with the exhaust pipe.

15 Steam and exhaust laps. To indy this action more particularly the following definitions must be understood.

Place the valve. Fig. 10 in its central position over the steam ports, their considering the right edge of the valve which determines the events of the instroke evelve.

The amount by which the valve overlaps the steam port on the admission side is called the **steam lap.** It is marked L in the figure

The amount by which the valve overlaps the steam port on the exhaust side is called the **exhaust lap**. It is marked l on the drawing

The dimensions  $L_{\rm t}$  and  $I_{\rm t}$  are respectively the steam and exhaust laps for the outstroke cycle

For the present we may assume that the steam laps are equal and that the exhaust laps are equal for the two cycles

Sometimes the steam lap is called the outside lap, because steam is generally admitted on the outside of the slide valve, though this is not universally the case. Smallarly the exhaust lap is called the inside lap. In

order to avoid possible confusion it is better to define the terms as above.

The width of the opening of the port for the admission of steam is given by the distance of the valve from the central position minus the steam lap.

The width corresponding to a dead point position of the piston is called the lead.

The width of the opening of the port for the exit of steam from the exhibit is given by the distance of the valve from the central position miners the exhaust hip.

16 Negative lap. When the valve is plued in its central position there may be no overlap either on the term or exhaust side of the port in which case of core is the valve less neither to increase she ist lap. Further, the valve may not exercited the ports an it central position, so that there will be a small velocity of port standing open either on the exhaust or the steam side. In the case

The with of the port opening on the fram side is called the negative steam lap.

The width of the port spaces on the exhaust side is called the negative exhaust lap.

The negacine coping. The effective of time of the value from its central position tender for the operation to a uncertakness. Negative steam lap is true by a cut out to a trock to a Tap to more common. For instance it is not an extended to prove the proof by a proceeding to proving a negacine of high speed. These duries residence at a province and other extended to province and other procedures are approximately and the procedure of the procedu

- 17 Critical positions. Because in a real the definitions just given and students the new many view to end of a all end ixin on a proceed and the felicinese store in tensors ally be critical. Consider the instead exerci-
  - (1) Admission of the organization process when the valve is at all defend from its central position equal to the from Tap and the defender of a result.
  - (2) Constitution plan when the value is a distance from its contribution represents the resembly and the distance is diminishing.
  - G) Release takes place when the calculus it and claims from its control point on squal to the collect. Up and the distance is more emig.
  - (4) Compression takes place when the value is at a distance from its central position equal to the exhaust lap and the distance is decreasing.

Thus the two count of edmi son and cut off as determined by the steam Lip and each begins when the x(d) is at the same distantion its central position. Whether the position  $x^{-1/2}$  it corresponding to admission or cut off depends upon the direction in which the valve is moving at the instant

Similarly the events of release and compression are determined by the Cahaust lap and each event begins when the valve is at the same distance from its central position, the position fixing the event of release or compression according to the direction of motion of the talve

These two positions may therefore be appropriately called the critical positions of the slide valve

- 18 Inside steam admission. The slide valve can effect the distribution equally well it steam is admitted on the inside edge and released at the outside edge. In this case the pipe  $\vec{E}$  would be connected with the boiler and S would become the exhaust pipe, Fig. 9, and the steam lap would be added to the inside of the valve and the exhaust lap to the outside. The steam pressure in this arrangement would now act to his the valve off its Seut and therefore provision must be made apart from the steam pressure, to keep it down on the ports. This de admission is more effect in ed with slide valves of the piston type, to be described presently, then with the type shown in Fig. 9.
- 19 Marking the valve spindle. The valve may be placed many one of the critical positions even when it is shut up in the steam chest if the valve spindle has been marked in the manner shown in Fig. 10 To mark the spindle use a trainingl shaped as shown in the figure, made out of, say 1 or 5 steel the length to be such that when one end rests in a conveniently placed centre dot on the cylinder itself (it is shown against the fluige of the stuffing box in the ketch) the other end is at right angles to the spindle. First the steam chest cover being off, place the valve in its central position, mark the line 00 on the valve spindle and put in a centre dot. Consider the Instroke Cycle. Push the valve to the left a distance equal to the steam lap, mark the spindle with the transmel and put in the dot a It can then be brought into this critical position again at any time when the covers are on by merely fitting the transmel to this dot. The dot b marks the critical position for release and compression. The dots c and d similarly mark the critical positions for the Outstroke Cycle, A little consideration will show that when the valve spindle is in any position the application of the transmel to the spindle will fix a point at a distance from the central position O, which distance is the displacement of the valve from its central position. Frowing this distance, the openings of the ports in either eyele may at once be interred. This method is used in valve setting and will be referred to when that subject is under consideration mere specifically. An enlarged view of the marking is shown below the general drawing. Fig. 10

20 Modifications of the typical form. There are many modifications of the typical form of slide valve just described, but in all these moch fications the steam and exhaust laps are defined in the some way and they determine the critical positions of the valve for the eight events of the sticke in the double eyele in the way just explained. The two principal objects aimed at in the modified forms are first to mere ise the area of the port opening for steam for a organ movement of the vilve second Is to deer so the in troud to sistance of the video to shoing

Before describing except hi modifications of the short D valve it will be consenient to describe Murdock system 112 II is copied from Madoch's specification dated. August 1799. The exhader is in conmunication with the steam chest through two short straight passiges 8, and 8 The slide valve working acrosthese ports consists or a rule, D shaped in cross section car " rving at the ends the plates I', and V, which slide over th port surface the semi-impular space between the back of the tube and the inside curved part of the steam chest being packed as indicated in the figure. The steam chest is thus divided into three parts, a central part in communication with the steam

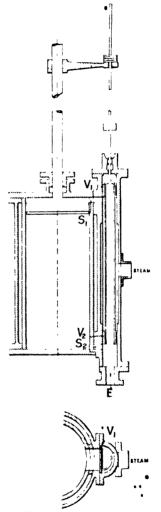


Fig. 11. Member Valvi The cond D Valve

pipe, and two end parts in communication with one another through the central pipe and with the condenser at E. Steam is therefore admitted at othe inside, and released at the outside edges of the plates, the exhaust steam from the top finding its way to the condenser through the central part of the valve. So far as the distribution of steam is concerned, the valve works with inside admission in the same way that the ordinary slide valve works. The sketch shows also that the valve was operated by an arm fixed to the piston rod striking discs fixed to the valve spindle. The motion of the valve was therefore not continuous. For the greater part of the time occupied by the stroke of the piston it was at rest in a position where the steam had free access to one end of the cylinder, the condenser being in communication at the other end.

21 Trick valve. When the sliding movement of the valve across the ports is continuous, as when operated by the simple eccentric gear, there is only a gradual merease of the width of the opening, so that for a considerable fraction of the time arranged for admission the steam has to make its way through a relatively small area of opening, and in consequence falls in pressure, a loss generally known as "wire drawing." In the Trick or Allan valve, Fig. 12 a passage P is east in the back, so that when the valve is just opening for steam the usual supply at tho

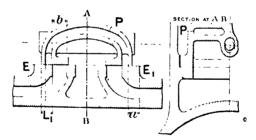


Fig. 12. TRICK VALVI

edge is supplemented by a second supply introduced into the port through the passage P, the opening and closing of this passage being effected by the edges of the valve scat E and  $E_1$  as the valve slides across them. If the valve Fig. 12 is separately drawn and placed in the critical positions it will be apparent that, considering the admission from the left edge of the valve, the distance a from the inside edge of the passage P to the edge of the seat  $E_1$  must be equal to the steam lap  $L_1$  in order

that the steam port and the passage P may open simultaneously. When the valve has moved a distance b to the right of its central position, a further movement to the right increases the width of the opening determined by the steam admission edge of the valve, but decreases the opening of the passage P by an equal amount, so that the opening for steam remains constant until the passage P is entirely closed by the bridge between the steam and the exhaust port. Admission at the right edge of the valve for the Instroke Cycle is similarly supplemented by steam passing through the passage from the left, the edge E controlling admission and ent off so tar as the passage is concerned.

In designing a valve of this kind care must be taken that sufficient width exists between the edge of a steam port and the adjacent edge of the exhaust port to prevent the passage P opening communication between the steam chest and the exhaust passage

**22 Double ported valve.** A valve designed to secure sufficient port opening with a relatively short stroke and in general use for the low pressure cylinders of manne engines and known as the double ported valve is shown in Fig. 13. Here two steam ports are formed on each side of the exhaust port and the right side of the valve is provided with two edges B - B to give admission at these two ports simultaneously and corresponding to these are two edges  $C_D C_D$  which

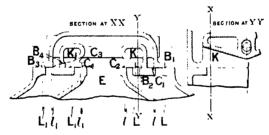


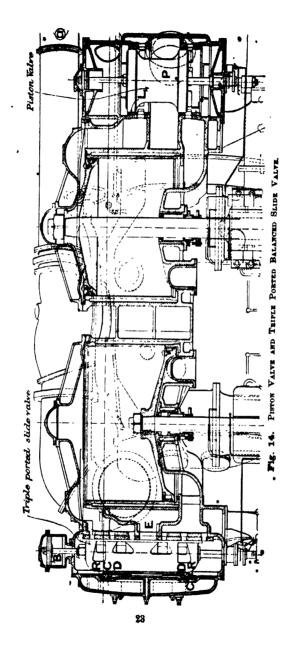
Fig. 13. Double Ponter Valvi

open communication with the exhaust passage E. A passage K is formed across the valve to convex steam to the edge  $B_i$ . A similar set of edges  $B_i$ ,  $B_i$ , C, C determine the distribution at the left side of the valve for the outstroke eyele. The steam and exhaust lapt are indicated by  $L_i$ ,  $L_i$  and l for the instroke cycle and  $L_i$ ,  $L_i$ ,  $l_i$  and  $l_i$  for the outstroke cycle.

Valves of this kind can be made with three, or even more, ports for each steam way into the cylinder. A section through the intermediate pressure and one of the low pressure cylinders of a battleship engine of 11,000 indicated horse power is shown in Fig. 14, which illustrates, amongst other things, the general arrangement of the triple ported slide valve used with the low pressure cylinders of this engine. The triple ported entry to the steam ways at each end of the cylinder is clearly shown. It will be noticed that the face on which the valve slides is really one face of a plate through which the ports are cut, ports in the cylinder casting corresponding with them. The exhaust port E lies between the steam ways.

- 23. Balancing piston. The weight of a slide valve of a large engine is considerable. The triple ported valve just described weighs 1½ tons, and in the largest engines the weight may be as much as 3 tons. To relieve the valve gear the weight of the valve is taken by a balancing piston B, Fig. 14. The bottom of the balancing piston cylinder is in free communication with the steam chest, a clear way being left round the piston rod. The upper part of the cylinder is maintained in continuous communication with the condenser. Thus the difference of pressure per square mich between the lower and the upper sides of the piston is the difference between the steam chest pressure and the condenser pressure. The area of the piston is proportioned to take the weight of the valve and valve gear, less the weight of one eccentric rod.
- 24. Balanced valves. A steam pressure of 200 lbs per square inch is not uncommon either in marine or locomotive practice. Methods of relieving the total pressure on the back of the valve in order to decrease the frictional resistance to sliding are used with pressures of this order.

One way of reducing the total pressure on the valve is shown in Fig. 15. A rectangular groove G is formed in the back of the valve and metal strips R are fitted to the groove. Springs at the bottom of the groove press the strips upwards into contact with a face F prepared in the cylinder cover. The strips and the springs are shown removed from the grooves in the valve in the perspective sketch, above the sectional elevation. In this way the area enclosed by the frame is cut off from the action of the high-pressure steam and the frictional resistance of the valve is reduced in proportion. These Richardson strips, as they are called, have been extensively employed in the United



States. Mr Aspinall\* made some experiments with a Lancashire and Yorkshire locomotive in connection with this subject, and found that the average pull on the valve spindle was reduced from about 1946 lbs to 854 lbs. by the addition of these strips to the valve. Fig. 15 is in fact a section of the valve with which the experiments were made.

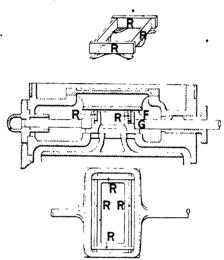


Fig. 15. Balanced Valve Lancashire and Yorkshire Railway.

Quoting two experiments, with a phosphor-bronze valve of the usual type, the force required at the spindle to push the valve was 1972 lbs, when the pressure in the steam chest was 140 lbs per square inch. This pressure, allowing for the lifting action of the steam in the passages, produced a nett load on the valve of 1995 lbs. The corresponding coefficient of friction was therefore 0.098. With the Richardson valve shown in Fig 15, when the steam chest pressure was the same as above, namely, 140 lbs per square inch, the total nett pressure on the valve was reduced to 8633 lbs., and the pull on the valve spindle was reduced to 760.5 lbs, corresponding to a coefficient of friction 0.088. The coefficient of friction is reckoned by dividing the force required to move the valve by the nett pressure acting on the back of the valve. Mr Aspinall's

<sup>\*</sup> J A. F. Aspinall, "On the Friction of Stide Valves," Ptc Inst Civil Engineers, Vol. 133.

experiments show that the average coefficient of friction for valves working on a vertical face is about 0.068, whilst for an unbalanced valve on a horizontal face it is about 0.088. For the partially balanced valve the coefficient found was slightly higher, being 0.092. A complete account of these experiments, with details of the dynamometer used to measure the force at the valve spindle, will be found in the paper quoted and in an earlier paper in Vol. 95 of the Proceedings of the Institution of Civil Engineers. In the discussion of the second paper Mr.F. W. Webb stated that instead of four separate strips he had used a rectangular frame milled in one piece, packed round with asbestos cord, with good results.

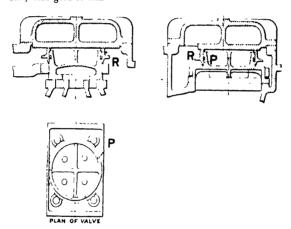
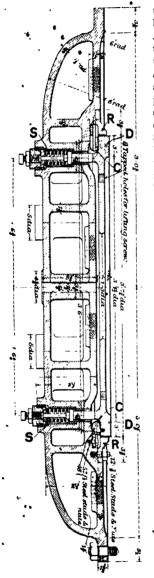


Fig. 16. Balancid Valve Northern Rahway of France.

Fig. 16 shows the slide valve and the way it is balanced in the early De Glehn Compound Express becometries of the Northern Railway of  $^{\bullet}$ France. The relief frame is in the form of a ring  $R_i$  bered out to fit the circular projection P turned on the back of the slide valve.

A relief frame as applied to a large marine engine valve is shown in Fig 17. Returning to the triple ported valve shown in Fig 14, its actual size is 5' 6" methe direction of its stroke and 5' 8½" wide. The area is thus 4521 square inches. A considerable fraction of this is cut off from the action of the steam pressure by the method indicated in the figure, but shown on a larger scale in Fig. 17, which is a section



through the cylinder cover and balancing ring. A circular plate D is pressed into contact with the back of the valve by springs, two of which are shown at S and S. This plate is free to move in a direction perpendicular to the port face, being guided by the steel ring RR, secured to the cylinder cover by 12, 4" studs. Steam is prevented from getting behind the plate by means of a flexible copper ring ("I' in the form of a single deep corrugation. This copper corrugation is fastened by one limb to the plate by 48, 1 studs, and by the other limb to the cylinder cover by 52 studs. The copper corrugation forms a flexible connection between the cylinder cover and the circular plate resting on the back of the valve, the plate is therefore free to move into close contact with the surface of the valve under the action of the springs. In this way an area of 1503 square inches is relieved from steam pressure.

There are other ways of preventing steam from getting behind the balance plate. The method indicated has been used successfully for many years by Messrs Humphrys and Tennant.

In fitting these frames care must be taken that the valve is not relieved too much, since the pressure on the inner side of the valve due to the steam in the passages tends to lift the valve off its seat. A certain quantity of steam is sure to find its way

Fig. 17. Valve Chrst Cover and Balancing Plate for Triple Ported Slide Valve.

behind the plate as the valve moves to and fro under it, and to prevent the gradual accumulation of pressure from this cause the inside of the relief frame is placed in communication with the exhaust passage or with the condenser.

25. Piston valve. Theoretically the slide valve can be relieved of all pressure on the back by changing it to the cylindrical form, obtaining what is known as a piston valve. Two essential properties of the flat slide valve are lost by this change. The valve is no longer kept up to its seat by the steam pressure, and the valve can no longer lift off its seat against the steam pressure to allow trapped water to escape. When a piston valve is used therefore it is absolutely necessary to provide relief valves on the cylinder to allow water to escape.

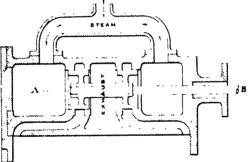


Fig. 18. PISTON VALVE

If a thin section of the slide valve shown in Fig 10 be supposed to revolve about the axis of the valve spindle it will describe a corresponding piston valve in space. The ports of the steam passages, both for supply and exhaust, must now eneircle the valve as shown in Fig. 18, and provision must be made for placing the ends of the steam chest or valve chamber in communication with one another. This is generally effected either by casting a passage for the purpose with the valve chest or with the cylinder, or by casting a passage through the valve itself.

This change in form of the valve does not involve any change in the distribution of steam it can effect. The definitions of the steam and of the exhaust laps and of the critical positions are precisely the same in a piston valve as in a valve of the ordinary type. The usual mode of construction adopted with piston valves is shown in Fig. 14. The steam chest is bored out to receive two liners, L and  $L_0$ , in which the ports are machined to the correct size. The corresponding ports in the cylinder are east slightly wider than those in the liner, so that when the liner is forced into its place the ports in it have a tur opening into the steam passages. In some cases the liner is made in one piece and all the ports are cut in it. The piston valve P is indicated in general elevation and it will be seen that its weight is carried by a balancing piston.

A section of the piston valve for the high pressure cylinder of the engine of which Fig. 14 is a part is shown in Fig. 19. This valve

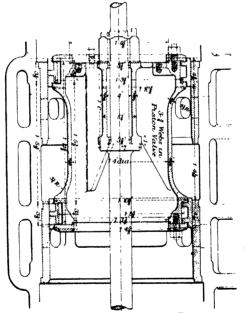


Fig. 19. PISTON VALVE MARINE ENGINE.

is two feet in diameter. The cylindrical body of the valve carries a bass inside it supported by three webs, the boss being connected to the valve spindle, which below is continued to the valve gear, and above to a balance piston. The ends of the valve are increased in

diameter and are formed into circumferential grooves carrying packing rings. One side of a groove is formed by the addition of a flat? steel ring to the end of the valve. The removal of this ring enables the packing rings to be put in place, after which it is replaced and held securely in position by a ring of study. The packing rings are split and a tongue piece is inserted as indicated, thus leaving the ring free to expand against the liner. The edges of the packing rings form the respective steam and exhaust edges of the valve. The valve shown works with outside steam admission.

Sometimes an uncut floating ring is used for packing the valve. The ring is turned a few thousandths of an inch smaller than the liner in which it works and is free to move a small amount in a radial direction relatively to the valve so that it can accommodate its position to the small distortions of the liner due to changes of temperature without danger of sticking.

A floating ring can either be put over the end of the valve, being held in its place by a washer or junk ring, or it can be spring over the end of the valve into a groove turned to receive it in the way discovered by Mr Yarrow\*. A floating ring passes a small amount of steam, but the gain in other directions in the opinion of some engineers more than compensates for this. The advantage of this form of packing is that there is practically no frictional resistance to sliding, because the unent packing ring is actually smaller in diameter than the liner in which it slides. Some makers dispense with even a floating ring and use a solid valve. In this case the design must be carefully considered with regard to the change of form likely to be caused by the change of temperature to which the valve and sectit will be subjected.

26 Vauclain valve. Fig. 20 shows the type of piston valve which was used with the Vauclain Compound Locomotive, built by the Baldwin Company of Philadelphia. This one valve effects the distribution of steam to two cylinders. There are therefore four cycles to be arranged for, namely, the in- and outstroke cycles for the high pressure cylinder, and the in- and outstroke cycles for the low pressure cylinder. The cycles involve 16 events per revolution. The course of the steam for the position of the valve shown is indicated by arrows. Steam enters the high pressure cylinder for the outstroke cycle at A simultaneously with the exit of steam from the instroke cycle at B. The steam leaving at B finds its way into the centre of the valve, which is designed to have sufficient capacity to act momentarily as a receiver

when required to do so. In the figure, however, the way is shown

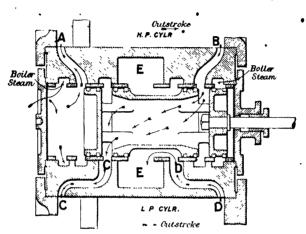


Fig. 20. PISTON VALVE. VAUCLAIN COMPOUND LOCOMOTIVE.

open into the low pressure cylinder at U and the steam is entering for the performance of the outstroke cycle. Steam from the instroke low pressure cycle is leaving the cylinder at D, passing round the valve into the exhaust eavity E, which is in direct communication with the blast pipe. If the valve is drawn separately on a piece of card the distribution of the steam can be followed through a revolution, and the two steam and exhaust laps measured without difficulty.

27. Segmental valve. A valve which combines the essential properties of the slide valve with part of the advantage of the piston valve has been invented by Mr W. M. Smith and is used by the North-Eastern Railway Company and in the new compound engines introduced by Mr S. W. Johnson on the Midland Railway. The main object in the design is to obtain a valve which, whilst retaining the advantages of the cylindrical form, will allow trapped water to escaps. For this purpose there are two rings of packing at each end, one narrow in width and the other relatively much wider. The wider ring is cut into three

See Mr Smith's paper in the Proceedings of Inst. of McChanical Engineers, July, 1902.

segments  $S_1$ ,  $S_1$ ,  $S_2$  (Fig 21). The head of the valve is formed by clamping a washer W against the main body of the valve B. The washer carries three horns  $H_1$ ,  $H_2$ ,  $H_3$  arranged so that they form radial guides for the segments. Two segments  $S_1$ ,  $S_2$  are shown drawn off these horns.  $S_2$  is in its proper position. Steam gets to the inside of the segments through holes in the washer and presses them on to the liner, and the segments are also free to move inwards a slight distance radially under the action of a sudden rise of pressure in the ports due to the presence of trapped water. The spaces between the ends of the segments are brought over bridges in the steam ports of the liner, two of which are shown at  $K_1$  and  $K_2$ . About one-third of the section of

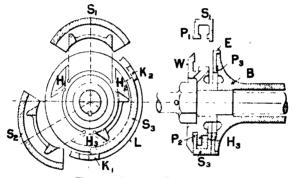


Fig. 21. SLGMENTAL PISTON VALVE

the liner L is shown in the figure, enough to include the two bridges  $K_1$ ,  $K_2$  and the part of the steam port between them. The narrower ring E is a piston ring somewhat of the ordinary type, cut in one place and expanding by its own elasticity on to the valve seat. Its object is to prevent the passage of steam through the spaces between the ends of the segments direct into the exhaust cavity. The segments and the ring E are all provided with projecting hps,  $P_1$ ,  $P_2$ ,  $P_3$ , in order to limit the radial movement outwards and to prevent, as far as possible, broken pieces of the rings getting into the ports in case of fracture. These six segments really constitute a set of small slide valves arranged so that the area acted upon by the steam is a minimum

In some comparative experiments made on the North-Eastern Railway the wear of these segments was found to be about 3/32, of an inch for 100,000 engine miles, and the wear of slide valves of the

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usual type, which were tried in comparison with them under such identical conditions as it is possible to get on a railway, was 25/32 of an inch per 100,000 engine imiles. At the Engineering Conference, May, 1897, Mr S. W Johnson stated that the segmental valves he used with the Midland engines required one-sixth of the power necessary to work the ordinary slide valve, whilst the loss by wear was also about one-sixth.

28 · Rocking valve. The essential features of this type of valve are the same as those of a slide valve. The valve oscillates to and fro about some central position, but the motion is an angular oscillation about the axis of the valve spindle instead of a linear motion in the direction of the valve spindle.

Fig 22 shows a rocking valve arranged to perform all the functions of a slide valve. The central portion of the valve is shown separately above the section, and the valve spindle again, separately above the valve. It will be observed that a squared part of the spindle engages the valve along a slot formed in the back. By this arrangement the valve is free to find its seat under the action of the steam pressure, and free to lift off its seat to allow trapped water to escape.

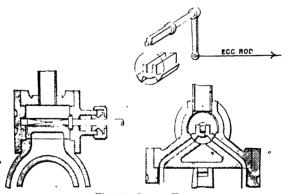


Fig. 22. Rocking Valve.

It is unusual to effect the distribution of steam by one valve of this type. The usual practice is to provide four separate valves, two at each end of the cylinder, the valve spindles being parallel to one another and at right angles to the vertical plane containing the cylinder centre line.

The general arrangement of four "Corliss valves" of this type is shown in Fig. 23. The valves S and E are respectively the steam and exhaust valves for the outstroke cycle: Si and Ei being those for the instroke cycle. The valve chambers in which S and S, work are connected by the steam passage P, this passage itself being in communication with the main steam pipe through the stop valve. The advantage of this arrangement is that the steam passages from the valve chambers into the cylinder are short, as will be seen in the figure, and therefore the clearance spaces are reduced to a minimum.

A cross-section through the valve chambers for the outstroke cycle across BB is shown in Fig 24. Considering the arrangement of the steam valve S more particularly, it will be observed in Fig. 24 that the ends of the valve spindle are well supported by the covers of the valve chamber, one end of the spindle being brought through a gland, so that by suitable connection with the valve gear mechanism it may receive an angular oscillation.

The valve itself engages with the valve spindle by means of slots cut across the ends, as shown in the separate drawing of the steam valve, Fig. 25. The spindle, Fig. 26, is squared at A, and carries a rectangular cross-piece or hilt at B . The internal diameter of the valve is large enough to allow the spindle to be pushed through it up to the hilt, and when it is in its proper place the squared part A rests in the slot at one end of the valve, whilst the hilt rests in the slot at the other The valve is ribbed at intervals R, R, R, and these ribs find corresponding ribs to support them in the valve chamber at  $r, r, r^*$ .

By the arrangement shown, the angular motion which the valve spindle receives from the valve gear is communicated to the valve, whilst the valve is left free to find its seat on the curved port surface under the action of the steam pressure or to lift off in order to allow trapped water to escape.

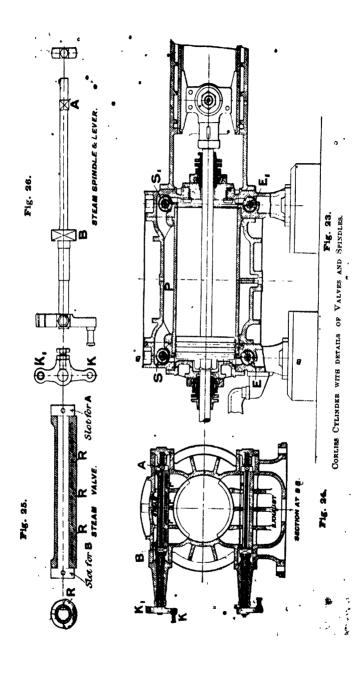
The angular displacement,  $\beta$ , which must be given to the valve spinule to move the edge of the valve through a given distance L is easily calculated. Thus, if u is the radius of the port surface, the angle in radians through which the lever on the valve spindle must be turned in order to move the edge of the valve a distance L is given by

$$\beta = \frac{L}{u}$$
.

The steam valves of engines fitted with valves of this type are commonly . worked by means of a trip gear which is under the control of the governor. The angular oscillation they receive is of the quick return

I am indebted to Messra Hick Hargreaves and Co. for the drawings on page 84. D. V.

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type. That is to say, the valve is opened by the mustion of the valve gear link work, and at some point in the stroke, determined by the governor, the valve is suddenly disconnected from the valve gear, and a powerful spring which is connected to the lever at  $K_1$ , closes the valve quickly, the rate of closing being controlled by a dashpot.

The gear operating the exhaust valves is unprovided with trip gear, and the angular motion in one direction is an exact repetition of the motion in the other direction.

29 The inertia of a valve. The resistance to be overcome at the valve spindle, to move the valve against the friction produced by the steam pressure acting on it, has been discussed in Art. 24. In high speed engines the resistance to motion due to the inertia of the valve must be added to this in order to get a correct idea of the force to be overcome. If W is the weight of a slide valve, a the acceleration at any instant, this force is given by

$$\frac{W}{a} \times a$$
.

The acceleration of the valve's motion can easily be calculated in the case of the simple eccentric gear, and it is not difficult to estimate it approximately in any ordinary case. General methods of finding the acceleration are discussed in Chapter ix.

To give some indication of the magnitude of the force, suppose an ordinary slide valve, weighing 200 pounds and having a stroke of 6 inches, to make 800 strokes per minute, and that the motion is of the simple harmonic kind, that is to say, the motion due to a crank and a relatively long connecting rod

The acceleration at each end of the stroke is

$$\omega^2 r = 4\pi^2 n^2 r,$$

where n is the number of revolutions of the crank per second, r is the radius of the crank in feet. In the case supposed, this is numerically equal to 437.5.

The force exerted by the valve spindle to start the valve at the end of each stroke is therefore

$$\frac{200}{32 \cdot 2} \times 437 \cdot 5 = 2720$$
 lbs. app.

. At the centre of the stroke this force becomes 0 and changes sign.

In the case of a rocking valve, the couple, acting on the lever of the

valve spindle, which is required to produce an angular acceleration of A radians per sec., is given by

$$C = \frac{I}{g} \times A,$$

where I is the moment of mertia of the valve and the spindle, about the axis of oscillation. If Q is the distance between the centre of the valve spindle and the centre K, at which the force is applied, the force corresponding to this couple, acting at right angles to the lever, is given by the quotient

#### CHAPTER III.

#### THE CRANK AND CONNECTING ROD

30 The crank and connecting rod. General description. The general form of the mechanism is too well known to need any special description. A drawing of it is shown incidentally in Fig. 77. In Fig. 27 OK is the crank and KB is the connecting rod. The end of the connecting rod is constrained to move in a straight line by the slide bars, the connection between the sliding blocks and the end of the rod being made by the crosshead. The piston rod is fixed to the crosshead, so that the motion of the piston, the piston rod, and the crosshead is the same. Hence the motion of the piston may be represented by the motion of any one of the points in the reciprocating mass. It is usually convenient to take the centre of the crosshead pin for this purpose.

The stroke of the piston, that is, the distance between the dead points, is constant and equal to twice the crank radius,

In what follows, the mechanism is restricted to the arrangement where the line of stroke, produced, passes through the centre of the crank shaft.

31. Determination of the piston position corresponding to any given value of the crank angle. The position of the piston on relation to its dead points is determined by the following simple geometrical construction

Set out the centre line of the cylinder, Fig. 27: draw the crank in any position as OK, and from the crank pin axis as centre, and with a radius equal to the length of the connecting rod, draw an are cutting the line of stroke at B. The point thus determined fixes the position of the centre of the small end of the rod. Arcs drawn with the same radius from the centres 0 and 6 fix the dead points of the small end of the rod. Every point in the reciprocating mass

bas the same motion as the centre of the small end of the connecting rod. The point B in the line of stroke may therefore be taken to represent the centre of the piston, and the points 0 and 6 the dead points of the piston.

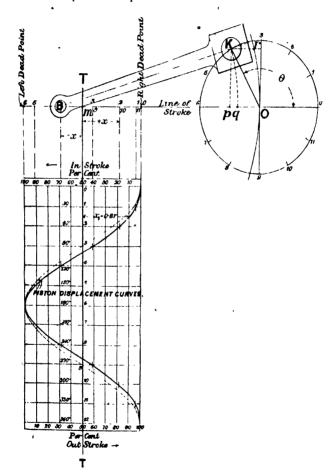


Fig. 27. Piston Displacement Curves.

Repeat this construction for several equidistant positions, 12 say, of the crank, obtaining thereby the corresponding positions of the piston in the line of stroke. Then the distance of the piston, corresponding to any one of the 12 equidistant values of the crank angle, may be measured from either of its dead points.

32. Piston displacement curve. It is an easy matter to extend the results of these twelve constructions so that the piston position may be fixed for any given value of the crank angle  $\theta$ . To do this, draw a vertical line TT through the point m, bisecting the distance between the dead points 0, 6. Fig. 27. Take any convenient length on TT, as 0-12, and divide this length into the same number of equal parts as the equidistant positions of the crank divide the circumference of the crank circle. Through each division draw a line at right angles to TT. The distance between each one of these horizontal lines corresponds to a certain change in the crank angle. This change is 30 degrees in Fig. 27. The part 0-12 of TT, may be looked upon as the circumference of the crank circle developed into a straight line, and set out to some convenient scale. Instead of numbering the points where the horizontals cut TT, 0 to 12, they may be numbered to give the angular position of the crank in degrees. This alternative numbering is shown in Fig. 27 by the figures to the left of TT. Now project the 12 points giving the positions of the piston in the line of stroke on to the correspondingly numbered lines below, and draw a smooth curve through them as shown by the thick full line. This curve is called the piston displacement curve. By means of it the piston displacement can be found at once for any given value of the crank angle  $\theta$  by merely finding  $\theta$  on TT, and measuring the horizontal distance from TT to the curve

If the stroke be divided into ten equal parts, and corresponding lines be drawn parallel to TT dividing the diagram vertically into ten equal parts, the piston position can be read off, as a percentage of the stroke reckoned from either dead point. In the diagram, Fig. 27, the upper scale corresponds to the **instroke**, and the lower to the **out** stroke.

- 33. Example. Find the piston displacement when  $\theta = 45$  degrees,
  - (1) from its central position,
  - (2) from the right dead point,
  - (3) from the left dead point.

Finding 45 degrees on TT and measuring the horizontal distance  $z_i$  to the curve, the answers are:—

- (1)  $x_1 = 0.8 \times \text{the crank radius}$ ,
- (2) ten per cent.,
  - (3) ninety per cent.

Notice that each of the three answers is numerically the same if the angle  $\theta$  is  $(360-\theta)=315$  degrees.

The difference in the two cases is that, when  $\theta = 45$  degrees and is increasing in value,  $\alpha_1$  is decreasing in value, but when  $\theta = 315$  degrees, and is increasing in value,  $\alpha_1$  is increasing in value.

Again, let  $\theta = 90$  degrees, then  $x_1 = 0.172 \times \text{crank}$  radius. Or in percentages, the piston is 41 per cent. of its stroke from the right dead point or 59 per cent. from the left dead point. These values are precisely the same for the angle 270 degrees.

In general, however, the displacements corresponding to two crank positions 180 degrees apart, are unequal except for the values 90 and 270 degrees, and of course 0 and 180 degrees

34. Alternative construction. The displacement diagram may be drawn in a slightly different and sometimes more convenient way as follows:—

Take any crank angle  $\theta$ , Fig. 27, and find the corresponding position, B, of the centre of the small end of the connecting rod as before, for number 4 crank position, say. Using this point in the stroke as centre, draw an are through the crank pin centre K, cutting the line of stroke produced in q. Then it is clear that the distance Oq is equal to mB, the actual displacement of the piston from its central position. Points similar to q are to be found for the twelve equidistant positions of the crank. The part of the line of stroke cut off by the crank cincle will then be divided by the several points q in the same way that the stroke is actually divided by the corresponding positions of the piston. To draw the displacement curve, take TT at right angles to the line of stroke so that it passes through O, the centre of the crank shaft, then project each point q on to the corresponding horizontal line below, as before, and sketch in the curve.

35. Use of a template to find q. If the displacement curve is to be drawn full size, or even to a large scale, the fixing of the several pirton positions in the line of stroke, and the drawing of the corresponding arcs through the crank pin centres, will usually require a trainmel some feet in length. The arc Kq, Fig. 27, may however be drawn without finding the corresponding centre point B in the stroke,

and without using a trammel at all. This is done by means of a template so fashioned that the edge ARB, Fig. 28, is curved to the radius of the connecting red, and the other edge CQD is straight and truly at right angles to a radius of the curve QR, which radius is to be marked on the template. To draw the are 4q, place the template as shown in Fig. 28, so that the radius QR lies in the line of stroke, and the curved edge passes through the point 4 on the crank circle. The

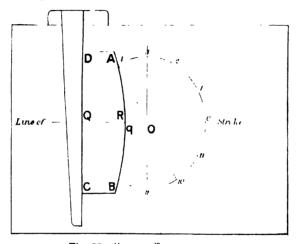


Fig. 28. Use of a Template to find q.

placing of the template in this position is much facilitated if the straight edge CQD is worked off a T square, as shown in the figure Care must be taken that the top edge of the drawing board is truly at right angles to the usual working edge.

In this way the positions of the piston may be found relatively to the dead points for stated crank angles without drawing anything but the crank circle. The displacement curve may then be constructed in the way already explained.

# 36. On the effect of changing the proportion between the length of the connecting rod and the crank radius.

The form of the displacement curve depends upon the ratio of the length of the connecting rod to the length of the crank only. As the length of the fod increases relatively to the crank, the displacement

curve, Fig. 27, continually approaches the form of the dotted curve shown on the diagram. In the limit where the rod becomes infinitely long, the dotted curve becomes the displacement curve. In this limit the displacement Op of the piston is given in terms of the crank radius, r, and crank angle  $\theta$  by

$$Op = r \cos \theta$$
,

a minus value of Op, showing that the piston is to the left of its central position. The piston displacement curve in the limit may be constructed by plotting this expression.

The curve in Fig. 27 is drawn for a connecting rod three times the length of the crank. The distance qp, in Fig. 27, shows the difference in piston position corresponding to an infinitely long connecting rod, and one three times the length of the crank, when the crank angle is  $\theta$ . The difference for any crank angle is the horizontal intercept between the dotted and full displacement curves. This difference decreases rapidly as the ratio of the length of the connecting rod to the length of the crank increases.

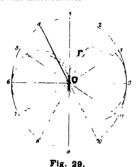
37. Piston displacement curve on big end base. Referring to Fig. 27, it will be seen that if an arc be drawn through the crank shaft centre  $\theta$  with radius equal to the length of the connecting rod, the horizontal distance between it and the arc drawn through the crank position K will be constaint, since both curves are drawn with the same radius from centres a horizontal distance apart equal to  $\theta q$ . It follows that the horizontal distance rK is equal to  $\theta q$ , and hence rK represents the displacement of the piston from its central position. This construction is true for any position of the crank pin, and the following simple method therefore may be used to find the piston displacement.

With a radius equal to the length of the connecting rod, and from the central position of the crosshead as centre, draw an arc of a circle through the centre of the crank pin circle. The horizontal distance between the crank pin and this arc is then equal to the displacement of the piston from the centre of its stroke. The crank pin circle thus becomes the piston displacement curve with reference to this curved base. This contral arc is conveniently referred to as the big end base, because it is the path the big end would move in, if the horizontal motion of the crosshead were suppressed.

This method of finding the piston displacement is sometimes very tiseful.

• 38. The polar diagram. The displacement x of the piston from its central position may be set out along the corresponding position

of the crank radius, as shown in Fig. 29. A curve joining up the ends of these radial quantities forms a polar displacement curve. The complete curve is like a figure 8, since twice during the revolution the piston passes through its central position where x=zero. In this diagram the distance of the piston from its central position corresponding to a given value of  $\theta$  is the part of the crank radius cut off between the centre  $\theta$  and the curve. Thus when  $\theta=60$  degrees, the piston is at a distance  $\theta r=0.56r$  from its central position. The disadvantage of this form as a practical diagram is that when the crank is in the region where x is nearly zero, it is difficult to measure r accurately because the crank itself is almost parallel to the curve, and the points of cutting are therefore somewhat indeterminate



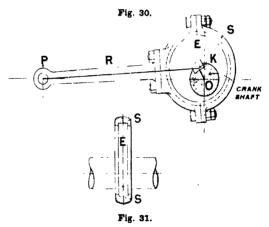
PISTON DISPLACEMENT CURVES POLAR FORM

As the ratio of the length of the connecting rod to the length of the crank increases, the displacement curve continually approaches the form of two dotted circles touching at  $O_c$  the diameter of each circle being equal to the radius of the mank. In the limit where the rod because infinitely long, the two circles themselves become the displacement curve. Thus the two circles in the polar diagram, Fig. 29, represent the same conditions as the dotted or cosme curve in Fig. 27.

## CHAPTER IV.

#### THE SIMPLE ECCENTRIC GEAR

39. Description. This gear is the type most commonly used when the crank shaft is required to turn in one direction only. Its essential features are shown in Figs. 30 and 31. Keyed to the crank



SIMPLE ECCENTRIC GEAR

shaft is the eccentric sheave E, which is merely in principle a flat disc with the hole for the shaft bored eccentrically through it. The sheave is usually made in two halves, bolted together. Surrounding the sheave is the eccentric strap S, put on in two halves, and held laterally by the grooving together of it and the sheave, as shown in the section, Fig. 31. The strap is bolted to the eccentric rod R, which is jointed to the valve spindle at P. The movement of the valve is the same as the movement of the point P. As the shaft turns, the point P receives a to and fro motion which, with properly proportioned parts, enables the slide valve to effect a distribution of steam suitable for driving the engine.

40 Eccentric gear equivalent to a crank and connecting rod. The names and the form of the parts in the simple eccentric gear disguise the fact that, so far as the motion given to the point P is concerned, the gear is equivalent to a crank and connecting rod. This geometrical identity is readily seen if the crank pin belonging to an ordinary crank shaft is imagined to increase gradually in diameter until it is large enough for the shaft to pass through it. It grows, in fact, into an eccentric sheave, so that the distance from the crank shaft to the centre of the sheave, called the eccentricity, is the crank radius corresponding to the sheave, and the distance from the centre of the eccentric strap to the centre of the pin P is the length of the corresponding connecting rod. The names of the corresponding parts in the two gears are compared in the two columns below.—

### Crank and connecting rod year

ur and connecting tod bear.	Eccentific gear			
Crank pin	is equivalent		to	Eccentric sheave
Crank radius	,,	,,	"	Eccentricity or eccentric radius.
Connecting rod	,,	31	,,	Eccentric rod
Big end	,,	,,	,,	Eccentric strap
Stroke of piston	"	,,	11	Travel of valve
Stroke = 2 x crank radius	Travel = 2 × eccentricity.			

In dealing with any problem concerning the motion imparted to a slide valve by an eccentric goar, it is therefore only necessary to treat it as a crank and connecting rod problem in which the eccentricity of the sheave is used for the crank radius, and the length of the eccentric, from the centre of the pin to centre of strap, is used for the length of the connecting rod

The crank and connecting rod equivalent to the eccentric gear shown in Figs. 30 and 31 is indicated in Fig. 30 by thick lines, OK being the eccentricity and KP the length of the eccentric rod.

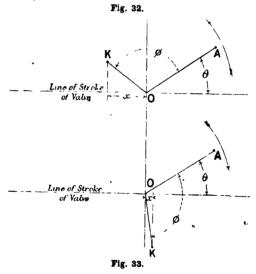
41 Displacement diagram of the valve centre. Assume for the time being that the crank in Fig 27 represents the eccentricity of a sheave, the connecting rod representing the length of the eccentric rod. The displacement curve for the valve centre would then be identical with the piston displacement curve in Fig. 27 and would be drawn in exactly the same way. The peculiarity of the simple eccentric gear compared with grank and connecting rod mechanism is, however, that the ratio of the length of the eccentric rod to the eccentricity is usually so large that the displacement curve of the valve is not sensibly different from the displacement curve corresponding to an infinitely long accentric rod.

# 42. Angular difference between the main crank and the eccentric radius.

A. Steam taken on the outside of the valve as explained in Art. 14. In order that the motion given to the slide valve by the eccentric gear may be properly timed to determine the distribution of steam described in Art. 3, the sheave must be placed on the crank shaft so that the eccentric radius stands at an angle  $\phi$  with the main crank. Thus, if the position of the main crank is specified by the angle  $\theta$ , as shown in Fig. 32, the corresponding position of the eccentric radius for positive rotation is given by

$$(\theta + \phi)$$

and the corresponding displacement of the valve from its central position, by .a.



Angular Difference between the Main Crank and Ecoentric Crank for the two directions of rotation when Steam is taken on the outside of the Slide Valve.

It is important to notice that, with outside admission, the eccentric angle is measured in advance of the main crank and is greater than 90 degrees. If for instance the main crank, were revolving in the

clockwise direction, Fig. 33, the angle φ would be set out as shown. In this case the position of the eccentric crank at any instant would be given by the angle

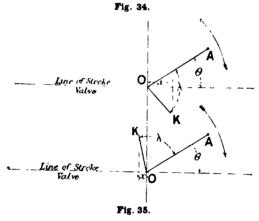
$$(\theta - \phi)$$

and the corresponding displacement of the valve from its central position, by x. It should be noticed in this latter case that the angle  $\theta$  decreases with the time. In the first case the angle increases with the time. In this way the difference between the two directions of turning is mathematically stated

Why this angular difference is necessary will be made clear in the valve diagram about to be explained.

#### 3 Steam taken on the insule of the valve as explained in Art. 18.

In this case the eccentric must be placed on the shaft behind the crank at an angle which is always less than 90 degrees. The relative



Angular Dipperence or Lag between the Main Chank and Eccentric Crank for the two directions of rotation when Steam is taken on the inside of the Slide Valve.

positions for clockwise and counterclockwise running are shown in Figs. 34 and 35. It will be seen that the angle at any instant between the eccentric radius and the line of reference is

 $(\theta + \lambda)$  for counterclockwise running, and that x is the valve displacement,  $(\theta + \lambda)$  for clockwise running, and that x is the valve displacement,

 $\lambda$  in each expression being the angle by which the eccentric radius lags behind the main crank.

The relation between  $\phi$  and  $\lambda$  for a given distribution is a simple one. If, for instance, it is found that the angular difference to effect a stated distribution of steam is  $\phi$  degrees when the steam is taken one the outside of the valve, the angle  $\lambda$  for the corresponding inside distribution would be  $(180 - \phi)$  degrees.

In each of the four figures the displacement x is found by projecting OK the eccentricity on to the line of stroke of the valve.

This projection should strictly be made by an arc equal in radius to the eccentric rod in the way explained in Art 34. Commonly the eccentric rod is so long relatively to the eccentricity, that the error introduced by using a straight line instead of the arc is negligible, so that the valve displacement from its central position may be calculated from

$$\alpha = r \cos(\theta \pm \phi)$$
 or  $x = r \cos(\theta \mp \lambda)$ .

43. Angular advance. Angular lag. Although the angle  $\phi$  is strictly the angular advance of the eccentric in front of the main crank, the term is often used, in fact most generally used, to denote the excess of  $\phi$  above 90 degrees. Thus

$$\phi = (90^{\circ} + \delta),$$

the symbol  $\delta$  being used to denote the angular advance in this sense.

If a slide valve receives its motion from an eccentric gear in which the eccentric sheave is keyed at 90 degrees in front of the main crank, the line of stroke of the valve being assumed parallel with the line of stroke of the piston, the cycle of events determined by the valve is one in which compression and admission take place at the same instant, that is, there is no compression stage, and cut off and release take place at the same instant, that is, there is no expansion. The pairs of points 4 and 1 in Fig. 2 are coincident, points 2 and 3 also coincide, and the diagram takes the form of a rectangle.

In order to obtain a time interval for expansion to take place between cut off and release, outside lap must be given to the valve and the eccentric angle must be increased beyond the 90 degrees. A certain small increase in the angle is also necessary to give lead to the valve. These increases allow of a time interval between compression and admission, which time interval may be increased or diminished by increasing or diminishing the inside lap

In general where the line of stroke of the valve is parallel to the

line of stroke of the piston the angular difference between the main crank and the eccentric sheave is given by

$$\mathbf{d} = (90 + \delta).$$

8 being what is often called the angular advance

In what follows the actual angle between the main crank and the eccentric sheave will be called the angular advance and little further mention will be made of  $\delta$ . It is introduced here merely to explain that the term angular advance may in general bear two meanings. The context of any work will however make it clear which meaning is being attached to the term.

In the case where steam is admitted on the inside of the valve the angular difference,  $\lambda$ , between the crank and the eccentric radius may be called angular lag because the eccentric is always behind the crank whichever way rotation takes place

44. To find the simultaneous displacements of the piston and valve corresponding with a given crank angle and a given value of the angular advance. Let the radius of the main crank be one foot, and the eccentricity three inches. Steam is to be taken outside the valve so that  $\phi$  is to be set out in front of the crank.

Draw the crank circle, Fig. 36, and divide it into a number of equal parts. Twelve only are used in the figure to avoid complication. Draw the piston displacement curve by either of the methods of Arts 32 to 35. The method of Art 35 is used in the figure, and the rod is taken to be four times the length of the crank. Then set out \$\phi\$, the angular advance, as shown. Draw the circle representing the path of the centre of the eccentric sheave with radius equal to the eccentricity, and starting from figure 0 on this circle, divide it into the same number of equal parts as the equidistant positions of the main crank divide the crank pin circle, and number these correspondingly with the numbers on the crank pin circle, being careful to number round in the same direction as on the grank pin circle. A pair of numbers on these two circles will fix corresponding positions of the crank pin and the centre of the eccentric. Assuming the ratio of the eccentricity to the length of the eccentric rod to be small, perpendiculars dropped from the successive positions of the eccentric sheave centre to the correspondingly numbered lines below, Fig. 36, will determine points on the valve displacement curve with sufficient accuracy. (If the eccentric rod is short relatively to the cecentricity, the exact construction of Art. 35 should be used.) Sketch in the curve through these points and the valve displacement curve is obtained in its proper relative position with regard to the piston displacement curve.

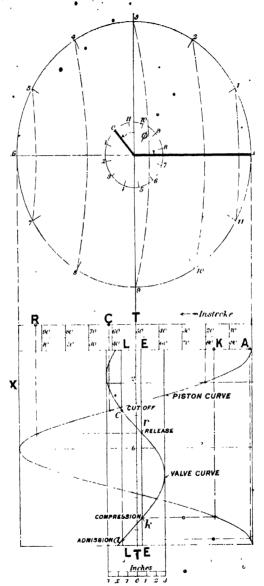


Fig. 36. THE VALVE DIAGRAM.

Any crank angle being assigned the corresponding piston and valve displacements can at once be found from the diagram by merely diawing a horizontal XX through the given angle. The simultaneous positions of the piston and valve are then shown by the parts of this line intercepted between TT and the respective displacement curves.

Example. What are the respective positions of the piston and the valve when the crank angle is 60 degrees?

On the diagram, Fig 36 60 degrees corresponds with the position marked 2. Draw a horizontal XX through 2, and it will be seen that the piston is at 20 per cent, of its stroke, whilst the valve displacement from the central position is 2.95 inches to the left.

45. The valve diagram. The object of the valve diagram is to discover what is taking place with regard to the steam distribution, or to exhibit the relations between given data, and from them to obtain complete data so that the gear and the valve may be designed to effect a distribution of steam according to a stated cycle.

Referring to  $\Delta tt$  17 it will be seen that directly  $\sigma_t$  the displacement of the valve from its central position, is known, it is at once possible to determine what is taking place with regard to the steam distribution, assuming the steam and exhaust laps to be known.

The diagram, Fig. 36, links the valve position with the piston position so that the piston position corresponding with a stated value of x is shown. Hence, if the displacement x is found for the different events of the stroke, the corresponding piston position may at once be found by projecting horizontally on to the piston curve and then vertically on to the appropriate percentage scale. Now, for the different events, x is equal either to the steam or exhaust lap, so that it is only necessary to locate these positions to determine the complete distribution of steam Considering the instroke, this is conveniently done by drawing the vertical line LL to the left and at a distance from TT equal to the -outs de lap. This line cuts the valve displacement curve at the two points c and a. These two points fix the positions at which the valve displacement is equal to the steam lap. Point a corresponds to admission of steam, since the displacement of the valve from its central position is increasing, and point c corresponds to cut off, since the valve displacement is decreasing. If XX be moved down so that it passes through c, it will cut the piston curve in a definite point and projecting this point on to the upper percentage scale, the position, C, of the piston at cut off may be read off. Similarly A is the point on the percentage scale corresponding to a.

For the events of compression and release, draw the vertical line EE

to the right-and at a distance equal to the exhaust lap from TT, cutting the valve displacement curve in the points r and k. At r the valve displacement is increasing, therefore it marks the release point; at k the valve displacement is decreasing, therefore it marks the compression point. These two points are projected first horizontally on to the piston curve as shown, and then vertically to the points K and R.

Again, since the opening for steam is given by

x - steam lap,

the cross hatched area shows by its horizontal width the actual opening of the steam port for any crank angle between admission and cut off.

Similarly, since opening to exhaust is given by

x - exhaust lap

the horizontal width of the dotted cross hatched area shows the opening of the port for any crank angle during release and compression.

The lead, being the opening when the piston is on a dead point, is shown on the horizontal through 0 or 12.

The events of the **outstroke** cycle, beginning when  $\theta$  is 180 degrees, are found in a similar way, the only difference being that the line LL must be drawn to the right of TT, and the line EE to the left, the distances in each case being respectively the steam and exhaust lap of the valve corresponding to the 180° cycle (that is the distribution from the front port), which distances may or may not be equal to the corresponding distances for the 0 degree or **instroke** cycle.

This particular form of diagram was, I think, first taught by Professor Reynolds. From the draughtsman's point of view it will be found the most generally useful, although it is not by any means the simplest or quickest to draw for the simple eccentric gear. It exhibits the relations between the different quantities, however, in a simple way, and keeps clearly in view the actual movement of the parts concerned.

46. Adjustment of scales. A very cursory consideration of the diagram, Fig. 36, will show that if the valve displacement curve is drawn full size, as it always should be, the corresponding piston displacement curve is unnecessarily large for the purpose for which it is required, namely, to read off the percentage position of the piston.

The scale of the ordinates of the piston curve may clearly be reduced to any convenient size, whilst the valve curve ordinates are kept full size. It is of course essential that the curves te drawn on the same base TT, otherwise the main object of the diagram is destroyed. If the curves were drawn on different bases, it would no longer be possible to read off a pair of simultaneous displacements on the line passing through a given angle at right angles to TT.

A valve diagram set out with suitable scales is given, in the next article. It may be mentioned that the work is considerably reduced if the diagram is drawn on a sheet of squared pape; the scale for the piston curve being chosen so that the stroke corresponds with ten of the main divisions of the paper. The diagram is then subdivided vertically, by the lines of the squared paper, and the percentage position of the piston can be read off quickly and accurately.

## Examination of the Distribution of Steam effected by the Simple Eccentric Gear

 Measurement of data. This is most conveniently explained in connection with the problem presented, as follows —

Given a double-acting engine, find at what percentage of the stroke the different events of the steam distribution take place, find the maximum port openings for steam and exhaust, and find the respective leads.

In the first place, data sufficient for setting out the valve diagram must be obtained from the engine. The data required are —

- for the piston displacement curve, the ratio of the length of the connecting rod to the crank,
- (2) for the valve displacement curve, the eccentricity of the sheave, and the angle between the sheave radius and the main crank, that is the angular advance or the angular lag,
- (3) the steam and the exhaust laps, and the widths of the ports and the bridges

Let it be assumed that all the measurements are to be made without taking the gear down.

The measurements required for (1) may be obtained most accurately in connection with the measurements for (2)

The first thing to decide is whether the slide valve is taking steam on the inside or outside of the valve. Stand facing the engine with the cylinder to the left. Turn the shaft round until the main crank is approximately in the zero position as shown in Fig. 36. Then notice the position of the eccentric. If the angle between it and the main crank is less than 90 degrees, the valve is taking steam on the inside, if greater than 90 degrees, on the outside. The direction in which the engine runs can at once be inferred by comparing the position of the eccentric sheave relatively to the crank, with Figs. 32 to 35.

The eccentric rod is usually so long in relation to the eccentricity

that the effect of its obliquity may be neglected without introducing sensible error, it follows that the displacement of the valve from its central position is given, with negligible circr, by

$$x = r \cos(\theta + \phi)$$
.

To find r, chalk the valve spindle in a convenient place near the stuffing box, and, whilst the engine is being turned round slowly, mark the valve spindle with a traininel of the kind illustrated in Fig. 10, finally fixing the extreme marks of the traininel point in either direction by a centre punch dot. The distance between these extreme dots is the valve travel, and half this distance is the eccentric radius.

The measurement of the angle  $\bullet$  between the sheave and the crank can be made without taking the gear down by making use of the above expression for the displacement, for if x and the corresponding crank angle  $\theta$  are known, since r has just been measured,  $\phi$  can be calculated. The values of  $\theta$  at which it is easiest to place the main crank are 0 and 180 degrees, corresponding to the dead points of the piston. The placing of the crank in either of these positions requires some care, because near the dead points the crank turns through a large angle for an extremely small motion of the piston, so that it is impossible to tell, by mere observation, when the crosshead comes to the end of its stroke, or when the crank is at 0° or 180°, with any degree of precision. The following method is used in the process of valve setting, and it should be studied earcfully.

To place the crank at 0° or 180', the positions corresponding nith the dead points of the piston.

Assume that it is to be placed at 0 degree. Turn the crank shaft round, Fig 37, until the crosshead is within about one-eighth of the stroke from the dead point. Then put a centre dot, A, on the slide bar, and with a traininel of any convenient length scribe an arc on the slide block and put a centre dot at B, on the arc. Keeping the gear in this position, take a long training of the engine, scribe an arc on the face of the wheel or crank disc, to cut a circular arc drawn on the face of the wheel or erank disc, to cut a circular arc drawn on the face of the wheel in D. Next turn the crank shaft round slowly until the crosshead, passing through its dead point, comes back to the position fixed by the training AB. Of course it requires at least two men to do this, one to turn, the other to watch the crosshead. Be careful not to overshoot the position, because the block must be stopped dead at the place by turning in the direction shown, in order to avoid error due to any slackness in the joints. Having brought the block to the correct position, mark the

<sup>\*</sup> See Appendix.

rim of the wheel with the trammel CD from the centre C. The point E would thus be obtained. Now bisect the arc ED in the point E. Then holding the large training with one point at C, turn the shaft slowly until the other point drops into the dot E. The crank is then in the position 0 degree, corresponding to the dead point of the piston. In a similar way the crank may be put in its 180 degree position.

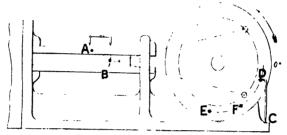


Fig. 37. Setting the Piston on a pead point.

Assuming the crank to be placed at 0 degree, carefully measure the distance of the valve from its central position by scribing the valve spindle with the trainmel used to find the travel, and then measure this distance from a centre dot placed indway between the dots marking the limits of the valve travel. This quantity is the x of the above expression. The angular difference  $\phi$  can now be calculated from

$$\cos \phi = \tilde{\tau} \frac{x}{r},$$

the + sign being used if there is angular advance, and the + sign if there is angular lag

Thus in a particular case where there was angular advance, as measured 0.96 inch when the crank was placed in its zero position. The travel measured 3 inches, so that the eccentricity was 1.5 inches. Hence

$$\cos \phi = -\frac{0.96}{1.5} = 0.642$$

From the tables this is found to be the cosine of 50 degrees, but since the sign is migus it is 180-50=130 degrees. The angular lag would have been 50 degrees if the valve had taken steam on the inside,

To measure the length of the connecting rod, place the engine successively on the two dead points and measure the distance from the centre of the crosshead pin to the centre of the crank shaft in each

position. Half the sum of these two distances is the length of the connecting rod. The length of the stroke can be easily measured at the slide bars.

- 3. The laps are to be measured from a drawing showing a section of the valve in its mid-position over the ports. To make this drawing.—
- (1) Place the engine on its respective dead points by the method just explained and measure the respective point openings, that is the "leads." Measure also  $x_1$  and  $x_2$ , the respective displacements of the valve corresponding to  $\theta = 0$  degree and 180 degrees, in the way just explained.
- (2) Take the valve out and measure the ports. This is conveniently done by taking a rubbing of them on a sheet of paper
- (3) Draw a sectional view of the ports and draw the edge of the slide valve in the position where it shows the "lead" when the crank is say at 0°. Measure the distance  $x_1$  from this edge obtaining thereby the positions of the edge when the valve is in its central position, and working from this edge draw as much of the valve in as is necessary for the purpose in view
  - (4) Repeat for the 180" dead point as a check
  - (5) From this drawing all the laps can be measured.
  - 48. Drawing the valve diagram. Let the data be the following.

Ratio of crank to length of connecting rod, 1 to 55,

Eccentricity of sheave, 15 inches,

Angular advance, 130 degrees,

Steam lap, 08 meh for both cycles;

Exhaust lap, 0.28 mch for both cycles.

Assume that the eccentric rod is long enough for the effect of its obliquity to be neglected.

- 1. Draw the piston displacement curve by the method of Arts 34 or 35, preferably on a sheet of squared paper selected so that ten of the main divisions are somewhat greater in length than the travel of the valve, that is 3 inches. For this particular example a sheet divided into square centimetres will be found convenient.
- 2. Draw the valve displacement curve by the method of Art. 44, on plot it from the equation

$$\alpha = 1.5 \cos{(\theta + 130)}$$

being careful to set out x to the right or left of the centre line TT according to the sign of the cosine.

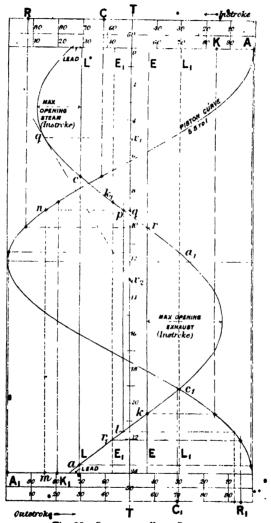


Fig. 38. RECTANGULAR VALVE DIAGRAM.

3. Considering the instroke cycle beginning at 0 degree, draw the line LL at 0.8 inch to the left of TT cutting the valve displacement curve at a and c. Transfer these points horizontally to the piston curve and vertically to the percentage scale for the instroke cycle, obtaining

Admission, 99½ per cent, of the return stroke. Cut off, 61 per cent of the stroke

Again, draw the vertical *EE* at 0.28 meh to the right of *TT*, cutting the valve displacement curve in the points r and k. Project these points horizontally to the piston curve and then vertically to the percentage scale for the **instroke cycle**, obtaining

Release, 92½ per cent\_of stroke.

Compression, 841 per cent, of the return stroke.

The lead measures 0.17 mch.

The maximum port opening for steam is 15 + 0.8 = 0.7 inch, and occurs when the piston is at 16 per cent of its stroke.

The maximum port opening for exhaust is 1.5 - 0.28 = 1.22 inches and occurs when the piston is at 21 per cent of its return stroke,

4 Consider now the outstroke cycle beginning at 180 degrees. Draw the line (dotted)  $L_1L_1$  at 0.8 meh to the right of TT, cutting the valve displacement curve in the points  $a_1$  and  $c_1$ . Project these points horizontally to the piston curve and then vertically downwards to the piecentage scale for the outstroke cycle, obtaining

Admission, 99½ per cent of return stroke.

Cut off, 69½ per cent. of stroke.

Again, draw the vertical  $E_i E_i$  at 0.28 inch to the left of  $TT_i$  cutting the valve displacement curve in the points  $r_1$  and  $k_i$ . Project these points horizontally to the piston curve and then vertically downwards to the **outstroke cycle** percentage scale, obtaining

Release, 941 per cent of the stroke

Compression, 79 per cent, of the return stroke.

The lead measures 0.17 inch, as before.

The maximum port opening for steam is 0.7 inch, as before, and occurs when the piston is at 21 per cent. of its stroke. The maximum port opening for exhaust is 1.22 inches, as before, and occurs when the piston is at 16 per cent. of its return stroke.

Finally, any position of the piston being assigned for either cycle, if the corresponding point be found on the appropriate percentage scale, and projected vertically on to the piston curve, and if through this second point a horizontal be drawn, as XX in Fig. 36, all the circum-

stances of distribution for both cycles can at once be obtained by considering the intercepts of the valve displacement curve along this line. The several events of cut off, release, compression and admission are indicated on the percentage scales by the capital letters

a subscript dash being used to distinguish the events belonging to the outstroke cycles.

49. Velocity of the valve. The rate at which the valve is moving can be readily found from the displacement curve. At a point on the curve which is at a maximum distance from the axis *TT*, the valve is instantaneously at rest, it is in fact at a dead point. The more horizontal the curve becomes the greater the velocity.

An exact measure of the velocity can be found by measuring the slope of the curve and then multiplying this by a suitable factor, the factor depending upon the scales used in the valve diagram and the speed of rotation of the crank. Suppose, for instance, that the velocity of the valve at the point q on the curve is required, Fig. 38, corresponding to a crank angle of 75 degrees.

Draw a tangent to the curve at q and produce it to cut the vertical axis in  $x_s$ . Then the slope at the point q is measured by the ratio

$$x_i i_i$$

Measuring these distances off, it will be found that  $qx_1$  is 1.35 inches, and  $x_1x_2$ , 2 inches.—The slope is therefore.

$$\frac{1.35}{2} = 0.675.$$

The multiplying factor to bring this to beet per second may be calculated in the following way.—

1 inch horizontally on the diagram represents p feet, say.

1 inch vertically on the diagram represents  $\theta$  degrees

The time taken by the crank to turn through  $\theta$  degrees, if the crank makes n revolutions, that is 360n degrees, per second, is

$$\frac{\theta}{360n}$$
 seconds.

Therefore one inch vertically on the diagram represents

$$\frac{\theta}{360n}$$
 seconds.

The distance  $qx_1$  represents  $qx_1 \times p$  feet. And the distance  $x_1x_2$ 

represents  $x_1, x_2 \times \frac{\theta}{360n}$  seconds. The actual velocity represented by the ratio is therefore.

$$\frac{qx_1}{x_1x_2} \times \left(\frac{p \times 360n}{\theta}\right)$$
 feet per second.

The quantity in brackets, which is the multiplying factor, therefore depends only on the scales chosen for the diagram and the speed of the engine.

In the present example

 $p = \frac{1}{12}$  feet, since the movement of the valve is shown full size.

 $\theta$  = 61 degrees. Therefore the numerical value of the multiplying factor is 0.492n.

The speed of the valve at q, that is when the crank is passing through the angle 75 degrees, is the slope, 0-675 multiplied by the factor 0-492n, and that is 0.33n.

If the engine crank is making 4 revolutions per second the actual instantaneous velocity is therefore 1.32 feet per second

From this it will be seen that if the slopes of the displacement curve be tabulated against a series of corresponding crank angles, they will represent the varying velocities of the valve, and these slopes can be converted into actual instantaneous velocities by multiplying with the common factor whose complete numerical value is known when the speed of the engine is stated.

When the obliquity of the eccentric rod is neglected it is usually more convenient to calculate the velocity from the expression

$$v = -r \sin (\theta + \phi) 2\pi n,$$

which is found by differentiating the equation for the displacement x, with regard to the time. Working the above example in this way,

$$r = 1$$
 feet and  $\phi = 130$  degrees.

Therefore

$$v = -\frac{1}{3} \sin (75 + 130) 2\pi n$$
  
= 0.332n feet per second.

This method is more accurate than the graphical way because the drawing of a tangent to a displacement curve cannot be done with great accuracy, though the accuracy is as a rule sufficient for all practical purposes. The graphical method has the advantage, however, that it is perfectly general and can be applied to find the velocity at points on any displacement curve, for instance, on the displacement curve shown in Fig. 52, which is distorted by the introduction of a rocker to make it pass through the two points required to give equal cut offs. It may also be applied to all the reversing motion displace-

ment curves given below. Before the analytical method can be applied the equation of the displacement curve must be known, and this cannot be found exactly for the cases just quoted, though, of the curve is given, a Fourier Series may quickly be found to represent it. This matter is discussed below in Chapter x.

There are other geometrical constructions for finding the velocity of the valve in connection with the forms of valve diagram given in the next few articles, but they are based on the assumption that the valve is moving with simple harmonic motion and therefore give the same results as the above expression. Moreover when the solution is found it must be interpreted in connection with the scale of the drawing, so that altogether the work is no more expeditions than with the general method.

Many further illustrations of the analytical way of calculating v will be found in the sequel.

It may be mentioned that r will sometimes come out positive and sometimes negative, according to the value of  $\theta$ . The positive sign denotes that the valve is moving from left to right, and the negative from right to left.

50. On the variation of the elements of the gear and the effect on the distribution of steam. This may be easily studied if the valve displacement curve is drawn on a piece of tracing paper, calling the angle zero when the displacement is a maximum in the positive direction, or in other words plotting the curve  $x=r\cos\alpha$  to represent the motion of the valve.

Mark on the axis of the curve the angle  $\phi$ , corresponding to the angular advance between the sheave and the main crank.

Set out the piston curve with its attendant percentage scales on a separate sheet of drawing paper. Then place the tracing of the valve curve over this drawing so that the vertical axis  $T_i T_i$  on the tracing coincides with the vertical axis TT on the drawing of the piston curve. Keeping these lines in coincidence, move the tracing upwards until the angle  $\phi$  is brought into coincidence with the angle zero on the axis of the piston curve. If there is angular lag, the angle  $\lambda$  must be set out in the negative direction on the tracing, that is upwards, starting from zero, and then the tracing must be moved downwards over the drawing to bring the angle  $\lambda$  on the tracing into coincidence with the zero of the piston axis. Having adjusted the tracing to this position pin it down and complete the diagram by adding the steam and exhaust lap lines to the tracing, obtaining thereby the diagram of Fig. 38, only with this difference, that the piston curve with its attendant percentage

scales is on a drawing beneath the tracing on which the valve displacement curve is drawn with its attendant steam and exhaust lap lines.

The effect on the distribution of changing the angular advance can be studied by moving the tracing up or down into new positions, this of course being equivalent to changing the angular advance. It will soon be discovered that although an increase of the angular advance, or a decrease in the angular lag, will give an earlier cut off point, yet every yettical movement of the tracing must be accompanied by an appropriate change in the steam lap if the lead is to be maintained at a constant amount. Also an increase of the angular advance will generally have to be accompanied by some change in the exhaust lap, otherwise the release will take place too soon and the compression may be excessive.

If, instead of changing the angular advance, the displacement curve be changed by varying r, the eccentricity (this involves sketching two or three cosine curves on the tracing on the same axis for different values of r), it will be found that a decrease in r determines an earlier cut off, but here again the lap must be altered if the lead is to be kept constant. Similarly the exhaust lap must be changed if the release and compression are to be kept at the same points.

In general the effect of changing the angular advance is much the same as the effect of changing the eccentricity. Neither change can be made without an appropriate change in the steam and exhaust laps, and both changes interfere with the maximum openings of the valve for steam and exhaust.

The student is recommended to reproduce the valve diagram of Fig. 38 in the manner here explained, that is with the valve displacement curve set out on a tracing, and to study the effect of the distribution of steam caused by changing

- 1. The steam lap:
- 2 The exhaust lap;
- 3 The angular advance, both an increase and decrease;
- The eccentricity, both an increase and decrease.

In each case, study the effect of the change with all the other quantities constant. Then the effect of varying two together may be tried. An hour spent in this way will teach the student moge about the properties of the kind of valve gear under consideration than ever he can hope to learn by reading about it.

In every case look carefully to the lead and assume that it must be kept constant.

There are many other ways of studying the question but none which will give a clearer insight into what is taking place.

Four other valve diagrams will be explained in the next few articles. The differences in form all turn upon the different ways of setting out or obtaining the valve displacement

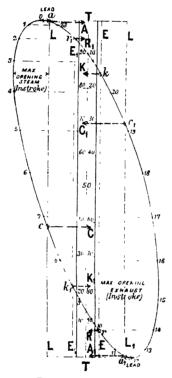


Fig. 39. OVAL DIAGRAM.

51. The oval diagram. A way of drawing a valve diagram, much used by locomotive engineers, is to plot the valve displacement on a stroke base. This is illustrated in Fig. 39. The vertical TT now represents the stroke, and the chain dotted horizontal lines pass through

the piston position corresponding to 24 equiangular positions of the crank. Any length may be chosen for  $TT_i$  and then piston positions for a series of crank positions may be found by either of the methods explained in Arts. 34 or 35. The corresponding valve displacements are measured from Fig. 38 and are plotted at right angles to the stroke, giving the points 1, 2, etc. to 24. Joining these, there results an oval curve which tends to become an ellipse as the ratio of the connecting rod to the erank is increased, until in the limit when both the connecting rod and the eccentric rod are infinitely long the curve is an ellipse. This oval is the valve displacement curve on a piston base. To turn it into a valve diagram, draw LL,  $EE = L_1L_1$ ,  $E_1E_1$  representing the respective steam and exhaust laps, exactly as in Fig. 38, cutting the oval in the points

taken in order. The undashed letters refer to the instroke cycle, the dashed to the outstroke cycle. Projecting these points horizontally to the percentage scale drawn about the vertical axis TT, the juston position is obtained for the different events in the two cycles. As will be readily seen the opening for steam and exhaust can be measured off the diagram for any assigned juston position. The lead, being the opening when the piston is on a dead point, can be measured off for each cycle at the ends of the stroke.

The diagram is drawn for the data of Art. 48. This form of valve diagram is a convenient one when the valve displacement is obtained from a model of the kind where the simultaneous values of the piston position and the valve displacement can be read off.

52 The Zeuner diagram. This celebrated and much used diagram is the polar form of the rectangular diagram. If the valve displacement, x, is plotted radially from the centre along the arm of the main crank for a succession of angular positions, as shown in Fig. 40, and a curve be drawn through these points, the valve displace ient curve takes the form of a figure 8.

The convenience of this form of displacement curve lies in the fact that if the length of the eccentric rod is a large multiple of the eccentricity, the curve does not differ sensibly from two circles, touching at the centre O. Moreover the line AB passing through O, the point of contact, at right angles to the common tangent at O, is inclined to the horizontal representing the line of stroke at an angle of  $(180-\phi)$  degrees, measured in advance of the crank, so that knowing  $\phi$ , the line AB, and consequently the displacement circles, can easily be set out. Of course the line AB may equally well be set out by measuring  $\phi$  in a direction  $o_1$  posite to

the motion of the crank, from the 180 degree position of the crank, or if

$$\phi = (90 + \delta)$$

by setting out the angle  $\delta$  to the right of the vertical through O.

The rule for drawing-the polar displacement circles may be stated 'thus:—

- 1. Set out the line AB at an angle (180  $\phi$ ) with the zero erank position, in the direction of rotation of the crank.
- 2 Set out OA, OB respectively equal to the eccentricity r, and on OA and OB as diameters draw circles touching at O

AB represents the travel of the valve since it is twice the eccentricity.

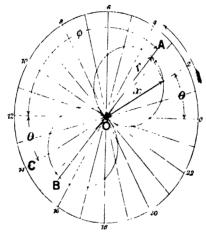


Fig. 40. POLAR VALVE DISPLACEMENT CURVE.

These two circles together form the polar valve displacement curve and have the property, that if the crank be placed in any position as 2, the intercept between the centre O and the curve, as x, is the corresponding displacement of the valve from its central position.

This may be proved as follows:-

When the effect of the obliquity of the eccentric rod is neglected, the displacement of the valve is given by

$$x = r \cos(\theta + \phi)$$

for outside steam admission.

Produce the direction of the crank aim through the centre O, when it will be seen that the angle  $(\theta + \phi)$  is equal to the angle AOC. The cosine of this angle is  $\frac{r}{r}$ , since the angle in the semicircle is always a right angle, so that  $x = r\cos(\theta + \phi)$ . This is true for all positions of the crank, the upper circle cutting off x for all positions of the crank above the common tangent at O, the lower circle serving to cut off x for all positions below the common tangent

The position of the crank for the various events can be found by fixing the points on the circles where x is equal to the respective steam and exhaust laps. This is most conveniently done by drawing arcs from the centre  $\theta$ , with radii equal to the steam and exhaust laps respectively, Fig. 41, cutting the circles in the points

$$a, \epsilon, k \rightarrow a, \epsilon \leftarrow k r_{\epsilon}$$

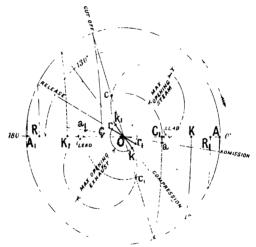


Fig. 41. ZEUNER VALVE DIAGRAM

The several radii drawn from  $\theta$  through these points fix the angular positions of the crank corresponding to the eight events of the two cycles. Consider, for instance, the position of the crank  $\theta c$ , the displacement x is given by  $\theta c$ . But this is equal to the steam lap, and the displacement is decreasing, therefore cut off is just taking place. Hence  $\theta c$  is the crank position for \_cut off''.

The port opening for steam on the instroke cycle is the intercept on the crank arm between the displacement curve and the are ac. The port opening for exhaust is the intercept on the crank arm between the displacement circle and the arc rk. The outstroke cycle can be similarly preared. The leads for the two cycles are the respective intercepts when the crank is in the 0 degree and the 180 degree positions.

The corresponding piston positions are projected from the crark purpositions, by the curved arcs shown in dotted lines on to the diameter of the crark pur circle which is taken to represent the stroke

The case with which this diagram can be constructed has led to its extensive use. It must not be overlooked that the displacement curves are only circles when the obliquity of the eccentric roll is neglected. If this is great and requires to be taken into account the curves then take as long to draw as in the rectaingular form of the diagram, since they must be set out by actually finding values of r corresponding to a series of crank angles, and then plotting these several values along the crank arm in its various angular positions instead of plotting them on a crank base.

Fig. 41 is drawn with the data of Art. 48

53 The Reuleaux diagram. In the explanation of this and the following diagram it is more convenient to use the sine form for the valve displacement. Thus, since  $\phi = 90 + \delta$ ,

$$i = i \cos(\theta + \delta + i\theta)$$
,  $-i \sin(\theta + \delta)$ 

The position of the Roule arx diagram Fig. 32, is that the angle  $\delta$  is set out below the zero position of the crank so that when the crank is in any position OQ, the angle QOD is equal to  $(\theta + \delta)$ . The perpendicular QS from Q on to OD, the radius of the circle OQ being equal to r the eccentricity, is therefore equal to

$$\tau \sim m(\theta + \delta)$$

The positions of the crank can be found for the various events of the stroke by finding these positions at which the perpendicular is equal to the respective laps. This is most conveniently done by drawing  $Q_iQ_i$  parallel to  $\partial D$  at a distance from it equal to the steam lap, and  $Q_iQ_i$  at a distance on the other side equal to the exhaust lap. These lines cut the circle in the points  $Q_i$ ,  $Q_i$ ,  $Q_i$ ,  $Q_i$ , and these points fix the crank positions for the corresponding events, admission, cut off, release and compression. The positions for the instroke cycle only are shown, all the circle be taken to represent the path of the crank pin to scale,  $Q_i$ ,  $Q_i$ ,  $Q_i$ ,  $Q_i$ , represent the positions of the crank pin. Considering the crank position  $Q_i$ , for instance,  $Q_iP_i=r\sin(\theta+\delta)$ , is equal to the

displacement for that crank position, but this distance is equal to the steam lap, and the displacement is decreasing, therefore cut off is just taking place.

The opening for steam or exhaust for an assigned crank pin position is equal to the length of the perpendicular from the crank pin on to OD minus the appropriate lap. Hence the lead is found at once by dropping a perpendicular on to OD from the zero position of the crank pin and measuring the distance between the line  $Q_1Q_2$  and the crank pin.

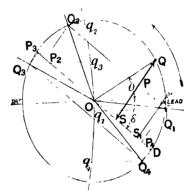


Fig. 42. RECTEAUX DIAGRAM

The corresponding positions of the piston with reference to the centre of the stroke are exhibited by the horizontal distances,  $Q_1q_1$ ,  $Q_2q_2$ ,  $Q_3q_3$ ,  $Q_4q_4$ , between the crank pin positions and the arc drawn through the centre O with radius equal to the length of the connecting rod. See Art. 37. Or, of course, they may be projected on to the diameter of the circle, by arcs, as in the previous case

The diagram is drawn for the data of Art 48.

54. The Bilgram diagram. This is a diagram of the same type as the previous one, only here the angle  $\delta$ , Fig. 43, is set up from the 180 degree position of the crank in a direction opposite to the direction of rotation of the crank. A cucle is drawn from  $\theta$ , with radius equal to the eccentricity, thereby fixing a point Q. Suppose the crank to be placed in any position defined by the angle  $\theta$ . Produce the crank through  $\theta$ , and it will be seen that the angle this direction makes with the line  $\theta Q$  is equal to  $(\theta + \delta)$ . Hence, a perpendicular QS from the fixed point Q on to the crank is equal to  $r \sin \theta + \delta$ , and it therefore

represents the valve displacement. In the crank position  $\theta_i$  the crank is at right angles to QO, QO is therefore the valve displacement. Between the angles  $\theta_i$  and  $\theta_i + 180$  degrees the foot of the perpendicular falls on the crank aim itself, as shown for the angle  $\theta_i$ .

If circles be drawn from the centre Q with radii respectively equal to the steam and exhaust laps, the crank positions for the four events of the instroke cycle are fixed by the four tangents which can be drawn to these circles from the point O. Consider the event of "cut off," for instance. The valve displacement is given by  $Qs_i$  and this is clearly equal to the steam lap, therefore the crank is in the position corresponding to cut off by the valve.

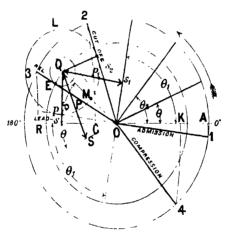


Fig. 43. Bitgraw Diagram.

In the position  $\theta_1$ ,  $Qs_1$  is the displacement of the valve, and  $Qp_1$  is the steam lap, therefore the difference  $p_1s_1$  is the opening for steam. When the crank is at zero, Qs is the displacement, and Qp is the steam lap; therefore ps is the lead.

No difficulty will be found in following the crank positions from the figure which is drawn for the instroke cycle with the data of Art 48.

The piston positions A, C, R and K, are projected from the crapk pin positions 1, 2, 3 and 4, by the ares shown.

DISIGN OF THE GEAR TO FULLIL GIVEN CONDITIONS.

55. Determination of the displacement curve to pass through two given points. A study of the valve diagram, Fig. 36, will show that, for a given gear, the valve displacement curve can be drawn when the two constant quantities r and  $\phi$  are known.

It is a mathematical principle that a curve involving two constants for its specification may be made to pass through two given points. In this case the constants r and  $\phi$  are connected by the relation

$$x = r \cos(\theta + \phi) \dots \qquad (1),$$

from which x, the variable displacement, can be calculated when the value of the other variable  $\theta$  is assigned. Hence, following the principle stated above, the displacement curve may be made to pass through any two points P and Q. Fig. 14 taken within the limits  $\theta=0$  and 360 degrees, by suitably fixing the values of r and  $\phi$ 

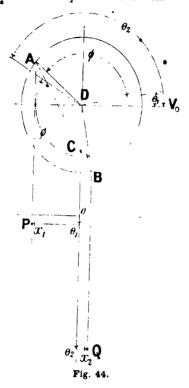
Each of the two points P and Q requires two quantities to specify it, namely, the angle  $\theta$  and the displacement  $\tau$  so that, in general, valve gear problems in which the motion of the valve is not sensibly affected by the obliquity of the cerentric rod involve primarily, the consideration of six quantities, of which four must be given and the remaining two are to be found

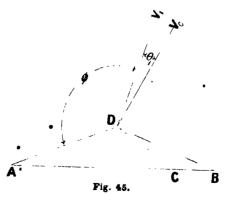
Let two points P and Q be given P being specified by the angle  $\theta_i$  and the displacement  $x_i$ . Q being specified by the angle  $\theta_i$  and the displacement  $x_i$ . The angles are measured as abscissae from the point Q. The most convenient way to find r and  $\phi$  is to substitute the given values of x and  $\theta$  in equation (1), getting thereby two simultaneous equations in r and  $\phi$ . The solution of these equations will give the values of r and  $\phi$  required. A geometrical solution may however be given here. Consider Fig. 44, which, assuming the solution, shows the eccentric radius in the positions DA and DB, corresponding with the crank angles  $\theta_1$  and  $\theta_2$ . The key to the solution has in the errormstances that, if AB is joined, ABD is an isosciles triangle whose vertical angle is  $(\theta_2 - \theta_1)$  and that the base AB is divided in C, so that

$$AC: CB = x_1 - x_2$$

and that the mittil line  $DV_n$  from which the crank angles are measured is at right angles to DC. The geometrical problem is therefore to draw this isosceles triangle having given the vertical angle and the ratio of the segments of the base. The construction is as follows —

Draw, Fig. 45, any isosceles triangle  $ABD_i$  having a vertical angle  $\theta_i - \theta_i$ . If  $\theta_i - \theta_i$  is greater than 180 degrees make the angle  $360 - (\theta_i - \theta_i)$ 





Divide the base at C in the ratio of the given displacements  $x_1$  and  $x_2$ . If  $x_1$ ,  $x_2$  are of unlike sign, divide AB interiorly: if of like sign, divide AB exteriorly.

Join DC and from the apex D draw a line  $DV_{\rm 0}$  at right angles to DC

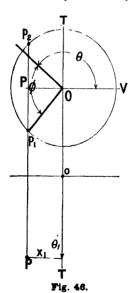
Then DA is the eccentric radius to the scale on which CA represents the displacement  $x_1$ .

From  $DV_0$  set out the angle  $\theta_1$ . Then  $V_1DA$  is the angular advance  $\phi_1$ .

If P and Q are plotted on a polar diagram, as in Fig. 40, the problem resolves itself into the drawing of a circle through three given points, namely the points P and Q and the centre O.

56. The determination of the displacement curve to pass through one given point. It either r or  $\phi$  is given, the displacement curve can only be made to pass through one point. The construction

is then, assuming r to be given —



Draw a circle with the given radius, Fig. 46

Let  $\theta_i$ ,  $x_i$  define the given point P.

Draw a line through P, parallel to TT, to cut the circle in points  $p_1$  and  $p_2$ . The two points of intersection show that two solutions are possible. Which of the two is that required is to be determined from the conditions of the problem. Let  $p_1$  be taken in this case. Join  $p_1$  to O. From OV set out  $\theta_1$  the given angle. Then  $\phi$  is the required angular advance.

If  $\phi$  is given and r is to be found, set out the angle  $\theta_1 + \phi$  from the initial line OV. Set out OP equal to the given value of  $x_1$ , and then a perpendicular to

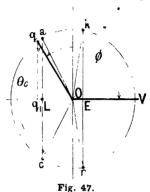
OV, through P, will intersect the line  $Op_1$  in  $p_1$ , fixing thereby the radius  $Op_1$ .

- 57 Quantities which determine points on the displacement ourse. In valve gear problems, the giving of the angle of the crank at which a definite event of the distribution takes place fixes one of the quantities necessary to define a point through which the displacement curve must pass: the nature of the event determines the displacement corresponding to this angle. Thus if
- $\boldsymbol{\theta}_{e}$  is the crank angle at cut off, the displacement is equal to the steam lap
- $\theta_r$  is the crank angle at release the displacement is equal to the exhaust lap
- $\theta_a$  is the crank angle at admission, the displacement is equal to the steam lap.
- $\theta_k$  is the crank angle at compression, the displacement is equal to the exhaust Lap
- $\theta_{0}$  is the crank angle at a dead point, which is either 0 or 180 degrees, the displacement is equal to the lap plus the lead

Hence if any two of the above pans of values be given, the construction of Art. 55 may be applied to find the constants of the displacement curve which will pass through the points defined by the given data.

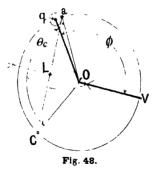
If the data given are equivalent to the fixing of three points on the displacement curve, the problem is impossible with the form of displacement curve under discussion. If one point only is specified, the solution is indefinite in the sense that the number of solutions is infinite. In this case one of the constants may be chosen, either r or  $\phi$ , and the problem then becomes the definite one of Art. 56.

58. Design problems. Since six quantities are primarily concerned with valve problems, it will be obvious that a large number of exercises may be manufactured in which four of the six are given and the remaining two have to be found. In many cases the value of the displacement corresponding to given angles has to be found from known relations existing between the displacements themselves. The problems presented in practice, in connection with the design of a valve gear, are however restricted to a few, and in solving them geometrically it is well to keep in mind the relations existing between the various constants of the gear and illustrated in Fig. 47. Thus, if OV represents the crank at a dead point, and Oq the eccentric radius, the projection of the radius, namely  $Oq_1$ , is equal to the valve displacement from its central position, and this is equal to the steam lap plus the lead. Further if Oa represents the position of the eccentric radius at admission, the projection, OL, represents the displacement of the valve at admission, which is of course the steam lap, moreover, if the projector be produced to cut the check at c, Oc is the position of the eccentric radius at cut off. Similarly Ok, Or are the respective positions of the eccentric radius at compression and release,



OE being the exhaust Lap. The lines  $\sigma c$  and kr are parallel, and both are bisected at right angles by the  $\lim_{t\to\infty} \Gamma O$  produced, which marks the zero position of the crank. Two problems are of particular interest, one of which may be stated as follows:—

Problem 1. Given the crank angle at cut off  $\theta_i$ , the lead, and the eccentric radius, find the steam kap and the angular advance.



The solution of this depends upon the facts that the angle turned through by the eccentric radius from the position corresponding to the zero position of the crank up to cut off is equal to  $\theta_{\rm s}$  that the position of the crank at zero, produced, bisects the angle between the eccentric radius at admission and at cut off, and that the projection of the eccentric radius on the zero position of the crank, produced, is equal to the steam lap. Hence the following construction, Fig. 48:—

Draw a circle with the given radius  $r_i$  and set out two radii  $Oq_{ij},OC_i$  to contain the angle  $\theta_i$ . With radius equal to the lead draw a circle from q as centre, and from O draw a targent to it cutting the eccentric circle in  $\sigma$ . Esset  $\sigma C$  in L and draw LOV OV is the zero position of the crank, VOq is the angular advance, and OL is the steam lap

From these, and the given data the valve displacement curve may be set out and the various events of the stroke determined. The displacement curve being now fixed the exhaust lap may be arranged to determine either release or compression at a stated per cent of the stroke.

The second problem is in particular called the design problem

Problem 2.—Given the crank angle at cut off  $\theta_0$ , the lead, and the maximum opening of the port for steam, find the eccentric radius, the angular advance and the steam Lip.

It will be noticed that the data specify no point on the curve in particular. Two angles namely  $\theta$ , and  $\theta$  are known and the displacements corresponding to them have to be found from known relations existing between the displacements at cut off in eximum opening, and at the dead point. The geometrical problem here is given three parallel lines of indefinite length as  $QP_{ij}(qq_{ij}, aC)$ . Fig. 49, to draw a circle touching one, of such a radius that the extremities of a chord in it, subtending an angle  $\theta_i$  at the centre, is strespectively on the remaining two of the three parallels.

## Construction, Fig. 49.

Draw a circle of any radius, and set out two radii Oq, OC, to contain the angle  $\theta_c$ . Produce the chord Cq to Q, taking Q so that if Cq represents the lead, qQ represents the maximum opening. In the figure the maximum opening is taken equal to twice the lead only, in order to bring the point Q within the limits of the page. Ordinarily it would be from 8 to 10 times the lead. From Q, draw QP tangent to the circle, and join P to the centre Q and produce it to V = OV is the zero position of the crank, and the angle VOq is the angular advance.

Through the points q and C respectively, draw lines parallel to PQ cutting OP in L and  $q_1$ . Then OP represents the eccentricity, LP the maximum opening, and OL the steam lap, the scale being fixed by the given value of the maximum opening  $LP_{\bullet}$ 

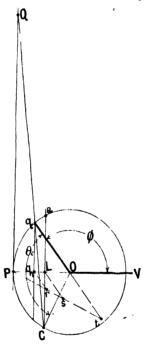


Fig. 49.

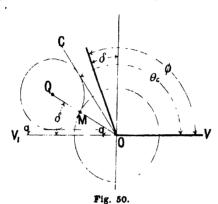
Hence if Pt be drawn at any angle to PV, and Ps be set out equal to the given maximum opening, the parallels to  $q_i r_i$ , namely Ls and Ot, cut off a length ts giving the lap required, and the length Pt giving the eccentric radius required. The given lead is equal to rs.

The disadvantage of this construction is that, when the maximum opening is a large multiple of the lead, the point Q falls at an inconveniently great distance from q.

The Bilgram diagram, Art. 54, may be used to solve this problem, and though not strictly a geometrical solution, it is a very good practical one.

The problem consists in the drawing of the Bilgram diagram, Fig. 43, having given the lead ps; the crank angle at cut off, and the maximum opening OM. The construction is as follows, Fig. 50.—

Set out the position of the crank at cut off, OC, draw a circle with radius OM equal to the given maximum opening, and draw qq parallel to  $OV_1$  at a distance from it equal to the lead. Find by



trial the centre Q of a circle which will touch OC, qq, and the circle OM. Then QM is the steam lap. The angle  $QO|V_1 = \delta = \phi - 90$  degrees, and OQ is equal to the eccentric radius.

A way of solving this problem analytically is given in Art. 75.

59. Adjustment of the inequalities of distribution by means of unequal laps on the slide valve. Comparing the results obtained for the two cycles in Art. 48, it will be seen that, owing to the shape of the piston displacement curve, the corresponding events of distribution take place at different percentages of the stroke in the two cycles. It will readily be seen, or can easily be tested, that if the piston curve were a true cosine curve corresponding to an infinitely long connecting rod, this inequality in the two cycles would not exist. In practice it is not possible to use connecting rods long enough in relation to their cranks to make the difference between the true piston displacement curve and a cosine curve negligible, so that this inequality must always be reckoned with.

It will be apparent from the valve diagram, Fig. 38, that if the steam lap line *LL* be moved slightly to the right or left of its position,

the cut off it determines can be varied a few per cent of the stoke, but that this cannot be done without at the same time chariging the percentage of admission, and, what is more important, the lead Similarly a movement of the exhaust lap line *EE* will cause a change of the compression by a few per cent, changing the release point, however, at the same time. By making the exhaust laps, therefore, unequal, it is possible to adjust the event of compression to equality in the two cycles. Also the events of cut off in the two cycles may be brought towards equality by making the steam laps unequal but masmuch as a difference of steam laps means a corresponding difference in the leads of the two cycles the difference between the steam laps cannot be made very great.

Applying this method to the valve diagram, Fig. 38 for the adjustment of the compression of the outstroke cycle to equality with the compression of the instroke cycle take the point m at 84½ on the appropriate percentage scale, project this vertically on to the piston curve at n, and project n horizontally on to the valve displacement curve obtaining the point p. The distance pq is the required exhaust lap, since it represents the displacement of the valve from its central position when compression is to take place. This measures 0.1 inch To find what change has taken place in the release in consequence of this adjustment, draw the vertical pt cutting the valve curve in t. Projecting t horizontally on to the piston curve and then vertically on to the appropriate percentage scale it will be found that the release has been changed from 94½ per cent of the stroke to about 92½ per cent

Obviously the release points could have been adjusted to equality in the same way at the expense of the compression

It will be found from the diagram that it an attempt is made to bring the "cut offs" to equality at 61 per cent in the same way, the lap must be changed to 1 inch approximately, obliterating all the lead of the outstroke cycle. All that can be done therefore is to make the difference in the cut offs less pronounced by introducing as runch inequality in the ste in Tips as the leads will allow

60 On the adjustment of the inequalities of distribution by means of a rocking lever. Pans of corresponding events, namely "admission" and 'cut off," or release and compression, and in a particular case all the four events, may be made to occur at equal fractions of the stroke in both cycles by the introduction of a rocking lever in the manner shown in Fig. 51. The effect of the rocking lever is to distort the valve displacement curve slightly so that its ordinates have the proper lengths to determine the events at equal pattions of the stroke

without introducing an inequality in the laps. The distortion of the curve is very little in the neighbourhood of the dead points of the stroke so that the leads of the two cycles are not sensibly different.

The method of designing the rocking lever to effect the necessary distortion of the displacement curve is fentative. The gear is first to be designed in the usual way to give a stated distribution of steam in one cycle. Then the design of the tocking lever to adjust the events of the other cycle, say admission" and "cut off," to the stated fractions of the stroke depends upon the fact that "admission" and "cut off occur when the valve is at the same distance from its central position. Hence so far as the position of the valve is concerned, without having regard to its direction of motion, the valve spindle crosshead is in exactly the same position relative to the fixed framework of the engine at the instants when either of these events occurs. (See Fig. 10.) But the eccentric sheave occupies different angular positions in the two cases. In the one case the rotation of the crank shaft tends to increase the displacement of the valve, in the other it tends to decrease it. The first step in the design is to plot the eccentric sheave centres  $p_i$  and  $p_s$ . Fig. 51 in the positions corresponding to admission and cut off for say the instroke cycle, and using these points as centres,

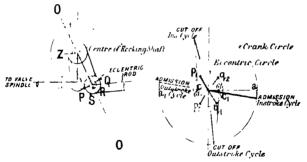


Fig. 51. Rocking Lever to equative cut off and admission

fix the corresponding position P of the end of the eccentric rod by the intersection of two arest each drawn with a radius equal to the length of the eccentric rod. Do the same for the other eyele, fixing the position Q of the end of the eccentric rod. If a rocker is introduced, so situated and proportioned that, whilst the arm coupled to the eccentric rod stands midway between the positions P and Q the arm coupled to the valve rod is at right angles to the line of stroke of the valve, the adjustment is

accomplished, providing that the travel of the valve, as determined by the ratio of the lengths of the arms of the rocker, is consistent with the steam lap. That is to say, when the arm coupled to the valve rod is in either of the positions corresponding to P and Q, the valve must have a displacement to one or other side of its central position equal to the steam lap.

To illustrate this, take the data of Art 48 and equalise the admission and cut off for both cycles. The data determine the following distribution of steam for the instroke cycle:—

Admission	991 pc	ı cent	of th	e stroke.
Cut off	61	11	n	**
Release	$92\frac{1}{2}$	11	,,	11
Compression	844			,,

The problem is to design a rocking lever which will distort the valve displacement curve so that admission and cut off take place at 99½ and 61 per cent, respectively in each cycle, keeping the steam laps for both cycles 0.8 inch.

- (1) Set out the crank in the four positions corresponding to the given data, as shown in Fig. 51, where the full lines refer to the positions for the instroke cycle, and the dotted lines to the outstroke cycle.
- (2) Set out the corresponding positions of the eccentric sheave by measuring the angular advance, 130 degrees, in front of each crank position. The points  $p_i$  and  $p_i$  indicate the centres of the eccentric sheave for the respective events of admission and cut off, instroke cycle. Similarly the points  $q_i$  and  $q_i$  fix the eccentric sheave centres for admission and cut off for the outstroke cycle.
- (3) With centres  $p_1$  and  $p_2$  respectively and radius equal to the length of the eccentric rod, assumed for the purposes of this example to be 12 inches, although any radius may be taken according to circumstances, strike arcs intersecting in P. With centres  $q_1$ ,  $q_2$  respectively and with the same radius, strike arcs intersecting in Q.

The end-of the arm of the rocker coupled to the eccentric rod must now move in the arc of a circle passing through the points P and Q. Join PQ and draw the indefinite line OO bisecting PQ at right angles. The centre of the rocking shaft may be taken anywhere in this line. In the example it is chosen at Z so that the arm coupled to the eccentric rod is  $3\frac{3}{3}$  inches long. From Z draw a perpendicular to the line of motion of the valve, this perpendicular is the centre line of the arm coupled to the valve rod.

The travel of the valve depends now upon the ratio of the lengths of the two arms. In the figure the second arm is taken such a length that when the arm coupled to the eccentric rod is up either position, P or Q, the horizontal distance between the end of the second arm and its mid position is equal to 0.8 inch, the steam lap.

This adjustment cannot be made without disturbing the events of release and compression in both cycles, but in general they are brought nearer to equality by the introduction of the rocker

The valve displacement curve after the introduction of the rocker is shown in Fig. 52. The dotted curve is the displacement curve without the rocker, that is, it is the curve of the diagram, Fig. 38, where it is assumed that the motion of the valve is simple harmonic

It will be noticed from the valve diagram that, although the distorted displacement curve brings the events of the stroke into better agreement, the maximum displacement of the valve on either side of the centre line is unequal, resulting in unequal maximum port openings.

The advantage of this method of adjustment is that it may be made without sensibly interfering with the leads of the respective cycles.

Release and compression may be equalised in a similar way. The point R, Fig. 51, shows the position of the end of the eccentric rod for release and compression at  $92\frac{1}{2}$  and  $84\frac{1}{2}$  per centrof the stroke respectively for the instroke cycle. S is the position of the end of the eccentric rod for release and compression at the same respective fractions of the stroke for the outstroke cycle. If the rocker arm moves in an arc of a circle through the points R and S, the equalisation of release and compression is accomplished.

A particular case arises when there is no exhaust lap, because in this circumstance the points R and S merge into one point, U say. There will therefore be only three points on the diagram, namely P, Q, and U, defining the path of the end of the rocker arm for equalisation of all the events. The centre of the circle through these points fixes the centre of the rocking shaft uniquely, although with some data the diameter of the circle is too small to enable a practicable rocker to be designed with its axis at this centre.

This method was first used by Professor Sweet and incorporated in the design of the Straight Line Engine\*, the first of which was designed as an experimental engine for Cornell University

## 61. The effect of a rocking lever on the angular advance of the eccentric sheave and on the steam admission. Angle

<sup>\*</sup> Professor Thurston, Stationary Steam Engines, J. Wiley and Sons, New York, 1884. See also an article in the American Muchinist for March 14, 1889 by F. A. Halsey.

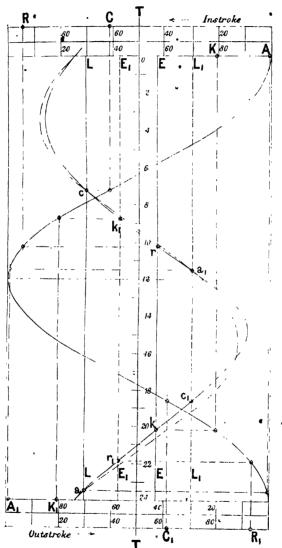


Fig. 52. VALVE DIAGRAM SHOWING THE EFFECT OF & ROCKING LEVER.

between centre line of main gear and valve gear. A rocking lever is sometimes used merely to transfer the motion of the end of the eccentric rod to a valve rod moving in a parallel plane, or to after the direction of motion of the end of the eccentric rod in the same plane, or for both purposes combined. If the arms of the rocker in the first case are on the same side of the rocking shaft, as in Fig. 51, or if the angle between the arms is equal to the angle between the two directions of motion in the second case, no change is necessary in the general angular position of the eccentric sheave in relation to the crank. Of course in either case the angle between the arms of the rocker may be adjusted slightly for the purposes of the last Article. If the arms of the rocker are placed on opposite sides of the central shaft, the distribution of steam is that due to an imaginary eccentric keyed exactly opposite to the actual eccentric. If the rocking lever in Fig. 51, for example, had been made with the arms oppositely placed, as indicated by the dotted end the distribution would be that due to an imaginary eccentric sheave keyed 50 degrees behind the crink. But such an eccentric sheave cannot effect a proper distribution unless the steam is admitted on the inside of the valve, see Figs. 34 and 35. Hence this change in the arms involves a change from outside to inside steam admission

If outside steam admission is to be retained along with the use of a rocker with oppositely placed arms, the eccentric sheave must be keyed on the shaft in such a position that the imaginary eccentric sheave stands at the proper angular advance in front of the crank to determine the steam distribution with outside admission. Figs. 32 and 33 may be taken to represent the general angular positions of the imaginary eccentric sheaves which determine the distribution, and therefore the actual sheave must be keyed on at exactly 180 degrees from the positions given. If, for example, the rocker of Fig. 51 had had oppositely placed arms, the actual coefficient would have an angular lag of 50 degrees.

In general, if a rocker is introduced with arms on the same side of the centre, the general eccentric sheave position for a stated direction of revolution and steam admission is to be chosen from the Figs-32 and 35. If a rocker is introduced with arms on opposite sides of the centre, the actual position of the eccentric sheave for a stated direction of revolution and stated steam admission will be exactly opposite the positions given in Figs-32 to 35.

Sometimes the centre line of the valve gear is placed at an angle with the centre line of the main gear for constructive convenience. In such cases, if there is no rocking shaft interposed between the eccentric rod and the valve, imagine the two centre lines brought into coincidence by a turning motion about their common intersection in the crank axle,

and deal with the design of the gear or its examination by the methods given, remembering that the angular advance now used is the actual angle between the main crank and eccentric diminished or increased by the angle between the centre lines.

62. The design of the steam ports and passages. The minimum area of the steam passages is usually adjusted so that the steam shall have an average velocity of from 4000 to 6000 feet per minute, though in special cases the greater of these figures is exceeded, and in other cases the smaller figure is not reached.

Neglecting the steam shut in the cylinder at compression, the confection which has to be pushed out of the cylinder by the piston after the first rush of steam during the drop of pressure from the exhaust to the back pressure and the dead point has been turned is practically equal to the effective volume of the cylinder itself.

Let A be the area of the cylinder in square inches, V the average piston speed in feet per minute, v the average velocity of the steam through a cross section of the steam passage whose area is a square inches.

Then the cubic feet of steam pushed through the exhaust passage per minute is VA/144 cubic feet—and neglecting the effect of changes of temperature and changes in the digness of the steam, this quantity must be equal to va 144, hence

$$VA = va \dots \dots$$
 (1),

so that

$$a = \frac{1^n A}{n} \dots \qquad (2).$$

The area of the steam passage is thus a fraction of the area of the cylinder, the value of which depends upon the juston speed.

With a piston speed of 600 feet per minute, the area of the steam passage must be 1/10 of the cylinder area, if the steam is to have a mean velocity of 6000 ft. per minute, and about 1/7 if the limiting velocity is 4000 ft. per minute.

With slide valves the area of the minimum cross section is commonly the area of the steam port at the entry to the cylinder. The passage itself is usually somewhat greater in cross section than the minimum determined from equation (2).

The width of the steam port is small in order to keep the travel as small as possible. The cylinder can be suitably designed if the length of the port is made about from 0.8 to 0.9 times the cylinder diameter. Calling the length of the port d, the width is a/d square inches.

The opening for steam is usually made about ? the full width of the port, so that the steam opening may be written

$$\frac{3a}{4d}$$
 .....(3)

With piston valves the minimum area of the steam passage does not usually occur at the port entry but in the passage. If the nett circumferential width of the piston valve be taken as the length of the port, d, it will generally be found greater than the cylinder diameter. Hence in calculating the velocity of the steam in the case of piston valves it must be remembered that the velocity through the passage is in general greater than through the ports of the liner

The value obtained from (3) is the maximum opening for steam.

Fixing now the lead, the cut off, and the compression, the appropriate valve diagram yields the outside lap, the travel, and the inside lap. The two latter quantities are required for the design of the width of the exhaust port.

The steam escaping through the steam passages from the cylinder is guided by the inside of the slide valve into the exhaust passage through the exhaust port

As the valve slides to and fro over the ports, the inner edge, A, regulating the release and compression, for say the instroke cycle, moves alternately towards and away from the incre remote edge, B, of the exhaust port. When the edge A has moved as far as it can go towards the edge B, of the exhaust port, the area for the passage of the exhaust steam is a minimum. When designing the width of the exhaust port, care must be taken that this minimum width is not less than the width of the steam port. Usually it is made considerably larger.

Let p be the width of the steam port,

b the width of the bridge separating the steam port from the exhaust port,

a the width of the exhaust port,

- I the inside lap of the valve,
  - t the travel of the valve.

Then when the slide valve is in its mid position, the edge A is distant (x+b-l) inches from B. The greatest movement that the edge A can make towards B is half the travel, t/2. Then the minimum exhaust area is

$$(x+b-l)-t/2=pq,$$

where q is a number which should not be less than unity. If q = 1, the minimum width is equal to the width of the steam port. Solving for  $\omega$  we have

$$x = pq + t/2 + l - b$$
 ......(4).

No difficulty will be found in arranging these formulae for inside admission \*

63 Valve setting. The final adjustment of the valve gear to bring the centre of oscillation of the valve into its correct position relatively to the ports is technically known as valve setting. A reference to the valve diagram will make the object of the process clear. Suppose the valve displacement curve to be drawn on a separate sheet of tracing paper, whilst the piston displacement curve and the steam and exhaust lap lines are drawn on a sheet of drawing paper as described in Art. 50. Then the placing of the tracing of the vertical axis of the valve displacement curve into coincidence with the axis of the piston curve is equivalent to the setting of the valve so that its centre of oscillation is in the proper position with regard to the ports. If the tracing be moved a slight distance laterally, thus throwing the vertical axes out of coincidence, it will be found that the quantity most sensitive to the disturbances is the lead. Hence the method used in the workshop to set the valve is to adjust the length of the valve spindle, or valve rod, until the valve has stated leads for each cycle

To perform the adjustment, set the crank at a dead point position by the method of Art 47, or by a method similar in principle, then adjust the length of the valve spindle until the lead at the steam port, corresponding with the dead centre position of the crank, has a specified value. Now place the crank in the other dead point position and measure the lead of the valve at the corresponding port. It should be equal to the lead specified for that port. The adjustment is to be retried until the specified leads are obtained, although it should not be forgotten that the valve spindle will lengthen slightly when working in the hot steam, thereby introducing a slight change in the leads, and this should be allowed for in the setting. It it is found after repeated trials that equal leads of the specified amounts cannot be obtained, it is probable that the eccentric sheave has not been placed on the crank shart at the proper angular advance. This point should be studied by moving the tracing of the valve displacement curve, vertically, over the drawing beneath it, since a vertical movement always corresponds to a change in the angular advance. An adjustment of the eccentric sheave on the shaft will generally enable the valve to be set with the specified leads. An error in the eccentricity of the sheave will also disturb the lead to an extent which can easily be studied from the valv dugram.

The lead may be observed, and directly measured, if the valve chest covers are off and the valve is designed for outside admission, or the lead may be obtained from the marking of the valve spindle as explained in Art. 19.

Generally the leads are equal but in the case where the laps are adjusted to secure equality of cut off, the leads are necessarily unequal, but each has a specified value.

Another way of measuring or observing the lead is to draw out a section of the ports and the valve respectively on two pieces of board, and bolt the one to the cylinder cover or in fact to any part of the framework, and the other to the valve spindle, arranging them in such a way that the board representing the valve slides with its edge against the board representing the ports. If the boards are also fixed so that the distance from the centre of the actual exhaust port to the centre of the exhaust port of the drawing on the board is exactly equal to the distance from the centre of the slide valve to the centre of the drawing of the slide valve, the drawing on the board will always occupy the same relative position to the drawing of the ports that the actual valve occupies with reference to the actual ports. The valve may therefore be set by observations made on the boards. This method is equally applicable to inside steam admission and outside steam admission. The events of the stroke may also be reachly followed on the boards, and the percentage of the stroke at which the different events take place may be found by combining the observations taken from the boards with a percentage scale marked off on the slide bars.

## CHAPTER V.

#### INDEPENDENT OUT OFF GEARS.

The separate cut off valve. The examples already considered in connection with the simple eccentric gear have indicated that an early cut off is necessarily accompanied with early release and early compression. With high piston speeds, such for example as those used in locomotives, early release and compression become an advantageous feature in the distribution. Locomotives running at high speed commonly cut off as early as 20 per cent, of the stroke with release and compression occurring in the region of 50 per cent of the stroke Many examples of this will be found in the chapter on Reversing Motions. But with the low piston speeds usual in factory engines the case is altogether different. Here the pressure drops to the back pressure at release, whilst the piston moves through a very small fraction of its stroke, consequently so far as the nett work done on the piston is concerned the stroke is ended at release. If, for example, release takes place at 40 per cent from the end of the stroke, the stroke is virtually shortened by that amount. This, combined with the necessarily accompanying early compression, results in a very attenuated indicator card.

To gain the advantages resulting from an early cut off and yet at the same time to avoid any prejudicial interference with the release and compression, a separate cut off valve is employed.

In the Gozenbach\* design for this purpose, the steam chest is divided into two parts by means of a partition parallel to the face of the steam ports leading to the cylinder. There are thus two steam chests, an upper and a lower. The steam pipe opens into the upper steam chest. Steam ports are formed in the partition, their general disposition being parallel with the steam ports of the cylinder in the lower steam chest. A slide valve without any exhaust cavity is worked across the ports of the partition by an independent valve gear, thus admitting and cutting off steam to the lower steam chest. A slide valve of the ordinary type

<sup>\*</sup> See Zeuner's Treatus on Valve Gears.

works in the lower chest distributing steam to the cylinder in the ordinary way. It is designed so that steam is cut off late in the stroke, say 75 per cent, and providing the lower chest were continuously filled with steam, the engine would always work with 75 per cent. cut off.

The valve working across the ports in the partition may however be set to cut off the supply of steam to the lower chest at an earlier fraction of the stroke, in which case no steam can get through the steam port opened by the main slide valve to the cylinder after this cut off has taken place. In this way cut off is determined by the partition valve, whilst admission, release, and compression, are determined by the main slide valve. The cut off point cannot be very sharply defined with this arrangement, because there is a considerable quantity of steam in the lower chest after steam has been cut off at the partition, and this of course finds its way into the cylinder through the main valve. The partition valve or "separate cut off valve," as it is called, is practically a stop valve worked by an independent valve ge ar

In the design patented by Paxman in 1885, the partition is not continuous through the steam chest, but forms a kind of fixed bridge through which steam ports are cut. The steam chest is therefore not divided into two separate parts, and to prevent steam getting through the main valve it is carried up so that its upper surface slides in contact with the lower surface of the bridge, ends being added to the valve, thereby forming ports or passages in the main valve through which the steam, coming through the bridge ports, is led to the distributing edges of the main valve. This change reduces the clearance inseparable from the Gozenbach design, and at the same time balances the main valve. The main valve is similar in general design to the valve illustrated in Fig. 53

In the majority of the designs, where a separate cut off valve works in combination with a main distributing valve, the partition is done away with altogether and the cut off valve slides on the top of the main valve, itself, the design of the main valve being suitably modified for this purpose. The simplest design, so far as the valves are concerned, is the case where the cut off valve is simply a plate moved to and fro over a main valve in which steam passages are formed

Let V, Fig. 53, be an ordinary slide valve arranged to give a suitable release, compression and admission with a cut off of say 75 per cent. of the stroke. Add to the ends of the valve the portions indicated. The steam edges of the main valve, namely s and S, now become the inner and lower edges of the respective steam ways through the valve which are formed by the additions to the ends.

If a plate  $V_1$  be placed on the back of the main valve (shown

lifted up a distance ab in Fig 53) and if it be worked by a separate eccentric goar, a little consideration will make it clear that the combined motion of the main valve and the plate will result in cutting off the steam supply to the passages through the main valve at some definite fraction of the stroke. By properly proportioning the size of the plate and the travels of the respective eccentries and their angular advances, this cut off can be made to take place at any stated fraction of the stroke between zero and the cut off determined by the main valve, without any interference with the other events of the stroke

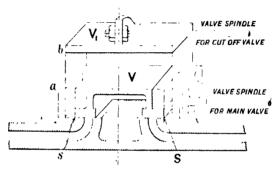


Fig. 53. Separate Cut Off Valve

From what has already been done with regard to the simple eccentric gear it will be clear that if the cut off is to be susceptible of variation, the cut off valve must be so arranged that either

- (1) its travel can be altered.
- (2) the angular advance of its eccentric may be varied
- (3) its lap can be altered relatively to the ports in the main valve.

In some designs the valve gear is arranged to alter the travel and the angular advance simultaneously

Fig. 53 shows the principle of the arrangement of a gear where the cut off valve is a plate and the cut off is varied by varying the travel

65. The Meyer gear. Constant Travel—Variable Lap—In this arrangement, the travel of the valve is kept constant and the lap of the cut-off valve is varied—That this may be done, the plate is divided into two parts connected by a left- and right-handed sciew, the screw forming in fact the valve spindle. The valve spindle is connected to the eccentric

gear outside in such a manner that it may be turned relatively to the valve rod operated by the eccentric rod.

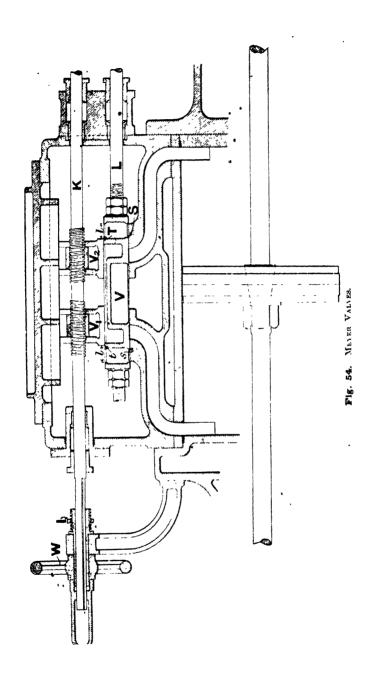
Fig. 54 shows an actual arrangement. V is the m. in valve, which is connected by its valve spindle L to a simple eccentric valve gear, and \_V, V, are the two separate parts of the cut off valve connected by the left- and right-handed screw K . This series can be turned from outside by the hand wheel W, and it is connected to the valve rod of a simple eccentric gear by a joint which allows the necessary freedom of rotation, The wheel W is carried on a sleeve held in a fixed bearing, and the end of K, squared, passes through the sleeve. Thus K can be turned at the same time that it is free to move to and fro through the sleeve. The projecting head of the sleeve is serewed and it carries an index  $\operatorname{nut} I$ . which serves to indicate how far the blocks are separated. Associated with I is a scale which is usually graduated so that the cut off corresponding to any angular position of the sleeve may be read off. The cut off edges of the main valve are at s and S respectively, and the cut off edges of the cut off valve are at t and T. The cut off valve is drawn Fig. 54, in its central position with regard to the main valve, and it will be noticed that the ports stand open on each side by the amount LThis quantity is the negative lap of the valve. If the wheel is turned so that the blocks are separated sufficiently to just close the ports on each side of it, it has no lap, and if by a further separation it overlaps the ports, the amount of overlap is, as in the case of the simple slide valve, the positive lap

Cut off takes place when the expansion valve is at a distance from the centre of the main valve equal to the lap. This distance may be found in terms of the crank angle by plotting the displacement curve of the main valve and the displacement curve of the expansion valve on the same crank base. By adding the displacement curve of the piston cut off may be found in terms of the stroke. Since the expansion valve has no effect on the lead it may be made with unequal laps without interfering with the lead, so that cut off may be adjusted to take place at equal fractions of the two strokes without difficulty, for one stated cut off

The way to examine the distribution of steam effected by gears of this type will be understood by working the following problem.

Example. The eccentric gears of an engine, fitted with the Meyer combination of main and cut off valves, have the following dimensions.

Main gear. • Eccentricity of sheave, 15 inches Angular advance of sheave, 130 degrees. Steam Iap, 08 inch.



Expansion gear. Eccentricity of sheave, 1.5 inches.

Angular advance, 180 degrees.

Find the lap of the expansion valve so that cut off may take place at 20 per cent of both strokes.

The first step is to draw the valve diagram for the main valve in the way already explained in Art. 48. This is shown in Fig. 55, from which it will be seen that the distribution effected by the main valve is:—

	Instroke	Outstroke	
Lead	0.17	0 17"	
Cut off	61 per cent.	694 per cent	
Release	92½ per cent	921 per cent	
Compression	84½ per cent	84½ per cent	

It will be observed from the diagram that the compression has been equalised by using different exhaust laps

Next, add to the diagram the displacement curve for the expansion valve, using the data above. The ordinates to this curve represent the displacement of the expansion valve from the centre of its travel.

In order to solve the problem the distance of the expansion valve from the centre of the main valve must be known when the piston is at 20 per cent of its stroke

Consider the instroke first. From 20 per cent, on the instroke scale at the top of the diagram draw a vertical line to cut the piston curve, and then a line at right angles to cut the displacement curves in the points a and b, and the axis of the diagram in c.

Then, when the piston is at 20 per cent of the instroke, the main valve is the distance cb from its central position, and the expansion valve the distance ca from its central position. The distance of the expansion valve from the centre of the main valve is therefore

$$cb - ca = ab$$

This distance therefore represents the required lap of the expansion, valve with respect to the ports of the main valve. But is it to be negative or positive lap?

This matter is settled by observing whether the displacement of the expansion valve from the axis of the diagram is greater or less than the displacement of the main valve.

When the displacement of the expansion valve is less than the corresponding displacement of the main valve, the hip is negative; when greater, positive.

The distance ab on the diagram measures 0.68 inch, and, so far as the instroke is concerned, this must be the negative lap of the expansion valve.

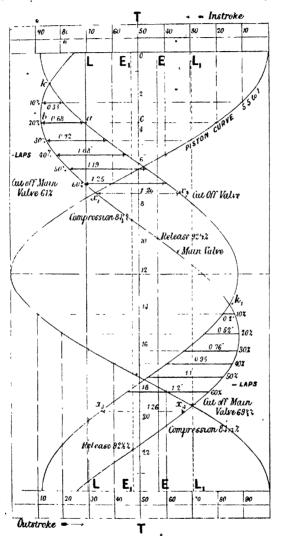


Fig. 55. VALVE DIAGRAM. MEYER GEAR.

Consider the outstroke. Projecting, in a similar way to that just described, from the 20 on the outstroke scale, the intercept between the two valve displacement curves measures 0.52 inch.

If therefore the length of the valve spindle is adjusted, and the blocks set the proper distance apart, so that the expansion valve has these respective negative laps, cut off will take place at exactly 20 per cent of the stroke for both strokes, whilst the leads remain equal at 0.17 inch, and release and compression retain the values stated above

The problem may now obviously be extended to find the Lips for a series of stated values of the cut off between zero and the cut off of the main valve. The projecting lines from 10 to 60 per cent, increasing by intervals of 10 per cent, are drawn in the figure for both the in- and the outstroke cycles and the value of the intercepts between the two curves marked in. Thus, to cut off, at 40 per cent of the stroke for both strokes the negative Lip for the instroke cycle must be 108 inches, and for the outstroke cycle 0.95 inch. The difference between the Lips for 20 per cent, cut off is 0.16 inch. The difference for 40 per cent is 0.13 inch.

The cut off valve can only be set to have one difference between the laps because when once the difference is established by adjusting the valve spindle to the proper length, the turning of the wheel W changes the lap at each side by equal amounts

Thus, after the drigi in has been drawn, the differences of the laps must be written down and then that particular difference chosen which gives the best general result.

Taking the differences of the figures marked on the valve dragram,

Per cent cut off	Determine of hip and and to equal to the cut off		
10 per cent	0.13 mch.		
$20^{\circ}$ . ,	0.16		
30 , ,	0.16		
40 ,	0.13 ,,		
50 , ,	0.09		
60	0.05		

If the valve spindle is a justed for a difference of 0.16 inch, cut off will be exactly equalised over the range from 20 to 30 per cent; very nearly equalised over the whole range from 10 to 40 per cent, and there will be small errors over the range from 40 to 60 per cent.

Engines provided with this kind of gear can therefore be set to give almost perfect indicator cards over a large range of expansion, the cut off being equalised by the expansion valve, and the compression and release by the main valve.

At the point, k on the valve diagram, where the two displacement curves cut one another, the expansion valve is in its central position with regard to the main valve, and if the expansion valve has no lap, cut off will take place. For regions above this point it will be seen that the expansion valve is at a greater distance from the axis of the diagram than the main valve, and therefore it cut off is required to take place at the excessively early fractions of the stroke to which the horizontals crossing this region correspond, the expansion valve must have positive lap. The same remarks apply, of course, to the region included between the horizontals through  $k_1$  and the point 12 on the vertical axis

When considering the general design of the gear it will be found convenient to draw the displacement curve for the expansion valve on tracing paper. It may then be pinned over the valve diagram for the main valve with any required angular advance, and the effect of varying this can be studied.

Care must be taken when designing the valves to see that, when the blocks are separated to the greatest distance, the ports in the main valve are not opened by the inside edges of the blocks. The blocks should be wide enough to prevent their inner edges from ever approaching near enough to the inner edges of the ports to allow steam to leak through.

The minimum overlap of the blocks on the inside can be determined with the aid of the diagram for a given gear in the following way. Adjust the cut off blocks to the maximum distance apart, and place them in their central position with regard to the main valve. Let the overlap on the inside in this position be denoted by u. Then when the valves are moving, this overlap is continually increasing and decreasing as the cut off blocks move about their central position with regard to the main valve. The greatest diminution of u is equal to the greatest displacement of the cut off valve from its central position with regard to the main valve, and this distance can be easily measured from the diagram. Call it z. Then the minimum overlap on the inside is u - z, and the maximum overlap is u + z.

It will be found by measurement that the greatest horizontal distance between the two displacement curves, Fig. 55, which is, of course, the greatest displacement of the cut off valve relatively to the main valve, is 1 26 inches at the two positions lett@red  $x_1$ ,  $x_2$  and  $x_3$ ,  $x_4$  on the diagram. Hence when u is measured, the minimum overlap is (u-1 26) inches.

When designing the valves the overlap u, in the central position, has

to be found for a given minimum value. Thus suppose the minimum overlap is to be 0.75 inch. Then,

$$34 = u - 126$$

from which u = 2 inches, say

In this case the design of the valves would be regulated by the condition that when the blocks were adjusted to their maximum distance apart, the miside overlap in the central position would be 2 inches. The minimum distance between them will depend upon the range of cut off required, since enough room must be left to bring them close enough to give the negative steam lap required for the latest cut off

The velocity of cut off is in this case, the velocity of the cut off valve relatively to the man valve, at the instant the event occurs. This may be found from the diagram by finding the respective velocities of the main valve and expansion valve at cut off by the methods of Art. 49, and then subtracting the velocity of the main valve from the velocity of the expansion valve.

An instructive way of working problems connected with the relative motion of the expansion and the main valves is to consider the main valve at rest and then find an imaginary eccentric sheave which, keyed to the main shaft and coupled to the expansion valve, would give it a movement over the main valve precisely the same as it has when both valves are moving in the engine. The way to do this is to combine with each

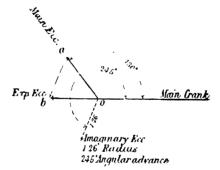


Fig. 56. MEYER GRAR. IMAGINARY FORESTRIC SHEAVE.

valve a motion equal and opposite to the motion of the main valve which has the effect of reducing the main valve to rest. The imaginary eccentric which will give the expansion valve the motion resulting from the combination is found by subtracting the eccentric radius of the main

valve as a vector from the cecentric radius of the expansion valve. The line giving this vector difference represents the imaginary eccentric in its proper angular position with regard to the main crank and of the proper radius. The way to take this difference is to set out the two eccentrics

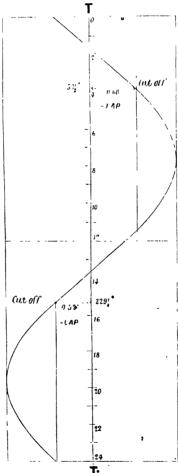


Fig. 57. MEYER GEAR VALVE DIAGRAM FOR THE CUT OFF VALVE.

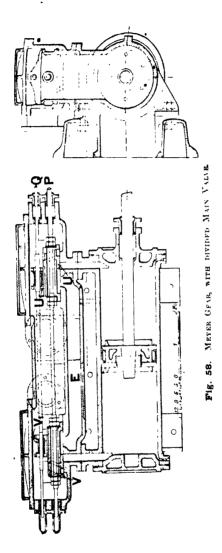
with their proper angular advances with regard to the main count and then to join their ends, placing an arrow on this joining line "in circuit" with the subtracted vector. Thus, in Fig. 56, the main crank and eccentric cranks, corresponding to the example, are set out, and ab is the required difference. The dotted eccentric crank drawn parallel to ab from the centre O in the direction of the arrow, represents the required imaginary crank, and this, if coupled to the expansion valve, would give it the proper movement relative to the main valve, which is now sunposed uncoupled from its eccentric sheave and at rest. The angular advance of the imaginary crank is 245 degrees and its radius is 126 The displacement curve corresponding to it can now be set out in the usual way. It is shown in Fig. 57. The negative lap is added to the figure and cut off is found just as if the problem were that of a simple valve gear. It will be observed, however, that the displacement curve is only suitable for determining cut off. The velocity of cut off can be measured from this curve by the method of Art 49, and the maximum displacement of the expansion valve from its central position with regard to the main valve can be measured also

It will not have escaped the student's notice that the displacement curve found from the imaginary crank is merely a curve representing the horizontal distances between the displacement curves of the main and expansion valves, shown in Fig. 55

The design of the typical form of the Meyer combination may be varied in many ways. A design which allows short straight ports into the cylinder is shown in Fig. 58, which is reproduced from Engineering, June 13, 1884. The main valve is now made into two separate valves, V and U, each part carrying one of the two separate blocks which together form the expansion valve. The form of valve diagram for this case is of course exactly the same as in Fig. 55, the separation of the main valve making no difference to the distribution which it effects. Each of the valve spindles, P and Q, is coupled up to a simple eccentric gear.

The exhaust space is marked E. The modification of the exhaust part of the valve, necessary in consequence of the division into two parts, can easily be followed on the drawing.

In setting the valves of a Meyer gear of the usual type the following method may be employed. First set the main valve to equal leads. Then from a drawing find the total width between the cut off edges of the blocks when the cut off is to be, say, 30 per cent. of the stroke. This can be found by drawing the blocks in their central position with regard to the main valve and having the laps determined by the valve diagram for equalising the cut off at 30 per cent. Then adjust the blocks by



means of the wheel W to this distance between the cut off edges. Next turn the engine until the piston stands at 30 per cent of its stroke, say for the instroke cycle, which can easily be done by marking the slide bais. The length of the valve spindle is then to be adjusted so that cut off is just taking place for the instroke cycle. Turn the engine into the 30 per cent position for the outstroke cycle. If everything has been correctly done the expansion valve will be just cutting off steam for the cycle. This last operation is really a check on the accuracy of the work.

The lap with which the cut off valve must be set, to cut off at a given percentage of the stroke, may readily be found by means of the

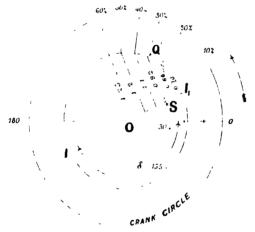
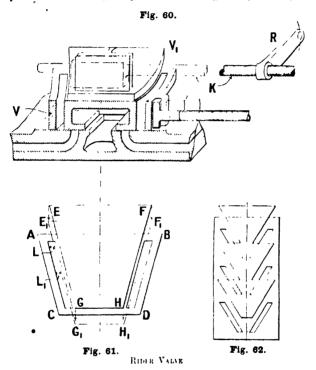


Fig. 59. MEYER GEAR. REULIAUX DIAGRAM APPLIED TO FIND LAPS OF CUT OFF VALUES.

Reuleaux valve diagram, the properties of which are described in Art. 53. When using it for this purpose, consider the main valve at rest and the expansion valve to be driven by the imaginary eccentric just discussed. Thus, the imaginary eccentric for the example just considered has been found to have a radius of 1.26 inches and an angular advance of 245 degrees. Referring to the description of the Reuleaux diagram in Art. 53, it will be seen that the angular advance, less 90 degrees, is the quantity to be set out behind the crank, and in the present example this angle is 155 degrees. Set out therefore, Fig. 59, an angle  $\delta = 155$  degrees, and make OI 1.26 inches long. Find the crank position for the

given cut off, say 50 per cent, thus fixing the point Q on the eccentric circle, and following the instructions of Art. 53, drop a perpendicular on OI, which in this case must be produced through O in order to meet the perpendicular at S. QS is the distance of the cut off valve from the centre of the main valve, and therefore it is the negative lap to which the cut off valve must be adjusted. The crank positions corn sponding to piston position from 10 to 60 per cent, at 10 per cent intervals, are set out in the figure, and the negative laps corresponding to them dimensioned. If Q should coincide with  $I_1$ , the valve is to be set without lap, and if the cut off is so early that Q falls between  $I_1$  and the horizontal diameter, the lap is positive. The laps for the outstroke cycle can be found in a similar way by setting OI behind the 180 degree position of the crank

66 Rider cut off valve. Constant travel Variable lap. In this gear, invented about 1869, there is a main valve and a cut off valve, each of which is worked by a separate eccentric gear as in the Meyer design, and the cut off is varied by varying the lap of the cut off valve. The point of difference between the two gears lies in the method of varying the lap. In the Mever gear, as already explained, the lap is varied by moving the two parts into which the cut off valve is divided, in a direction along the valve spindle by means of a left- and right-handed screw. In the Rider design the cut off valve is in one piece, and the lap is varied by turning it about the axis of the valve spindle by means of the lever R, the joint between the valve spindle and the eccentric rod being such as to allow of this turning action. The necessary modification of the design of the valves is shown in principle in Fig 60. The surface of contact between the two valves forms part of a cylindrical surface whose axis coincides with the axis of the cut off valve spindle K. The arrangement of the ports in the main valve and the way the lap of the cut off valve is varied with regard to them, will be understood from Fig. 61, which represents the cylindrical surfaces of contact developed out on the flat. ABCD is the developed surface of the main valve V, the steam ports in it being equally inclined to one another and to the centre line. The developed surface of the cut off valve is represented by EFGH. The inclinations of the edges of the valve to one another and to the centre line are the same as the corresponding inclinations of the ports, so that the edges \* EG, FH, he parallel with the corresponding steam ports Therefore, the horizontal distances between the respective edges of the steam ports and the valve are constant on each side. This distance is marked L on the lefthand side and represents the negative lap of the valve, it being assumed that the cut off valve is in its central position with regard to the main valve. When the engine works with the valves in this relative angular position with regard to one another, cut off will be determined by the negative lap L. If the cut off valve is turned into a new angular position, by means of the lever R, the lap will be altered. Thus suppose the new position is shown in Fig. 61 by  $E_1F_1G_1H_1$ , the negative lap has changed



from L to  $L_1$ . In this way the lap may be varied between stated limits, and in practice the variation is usually effected by means of a governor connected to the arm R. The full consideration of the gear therefore involves a discussion on governing, and this is outside the plan of the present volume. It may be stated, however, that directly the angular position of the cut off valve is given the lap is known, and the valve lagram can be set out in exactly the same way as for the Meyer gear.

There are variations of the design shown in Fig. 60 all alike in principle. One common arrangement is to continue the surfaces of contact round the axis, so that the cut off valve becomes a piston valve. In this case, if the inclined points were made continuous round the inside cylindrical surface of the main valve, the horizontal distance between the wide ends would be inconveniently great. This difficulty is evaded by cutting them in a series of steps, as indicated in the developed surface, Fig. 62, which shows also the corresponding saw tooth edges of the cut off valve. Of course this stepwise arrangement of ports may be made in any case whether the cut off piston valve is a piston valve or not

The obvious advantage of making the cut off valve a piston valve is that it is balanced as regards the main valve. Working examples of the Rider valve can be seen at South Kensington Museum

67 Cut off plate. Constant lap. Variable travel. Fig. 63 shows an actual example, which has kindly been supplied by Messrs Marshall, Sons and Co., Gainsborough of a cut-off plate in which the travel is varied. This design has already been illustrated in principle in Fig. 53. It will be noticed that the main valve, so far as the steam distribution is concerned, is divided into two parts, V and U, involving a division of the exhaust ports into two parts, P being the common exhaust passage leading away to the condenser or the atmosphere as the case may be

The two ends of the valve are held together by connecting ribs along the sides of the valve, these ribs being connected with one another by a cross piece, whose cut T section is seen in the drawing. The two ends U and V, the side connecting ribs and the cross piece are all cast The valve spindle passes through the part U of the valve and is secured to the central cross bar by the lock nuts seen in the The cut off valve  $V_1U_1$  is formed in one piece—the valve spindle passes through the valve and is secured by lock nuts screwing down on to appropriately formed surfaces at each end. A feature to be noticed is that the main valve is double ported with regard to the cut off valve. This involves the cutting of a steam port through the cut off plate at each end. Thus, considering the left-hand end, a and b are the respective cut off edges of the plate, A and B being the corresponding edges in the main valve. The cut off edge of the main valve is marked s, the corresponding edge in the cylinder ports being The corresponding edges for exhaust are e and E.

. The way the travel of the valve is varied will be understood from Fig. 64, which shows a general arrangement of the valve gear. The eccentric working the cut off valve is not connected directly to the valve rod Q, but to a link which it oscillates about a fixed tentre C. The

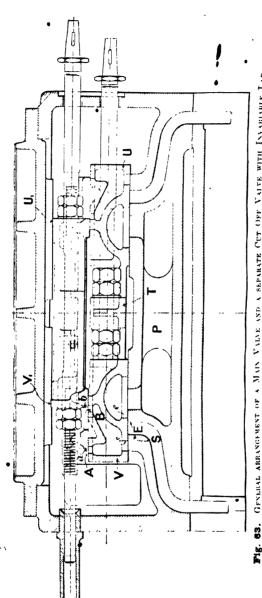


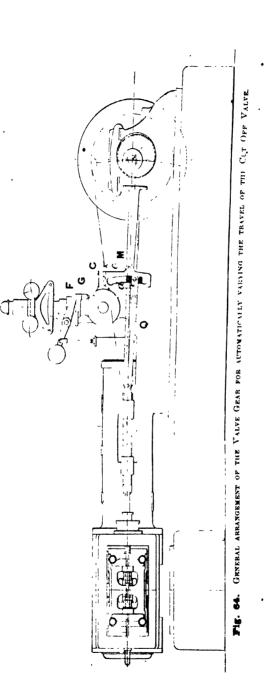
FIG. 63. General arranchment of a Main Value and a separate Cut Off Vaive with Invariable Lap

valve rod Q is pented to a block M shding in the slot of the link, its position being determined by the governor coting through the rod G. When the governor is running at a constant speed, the centre F, about which the suspending link G is free to swing, is a fixed point, and the stroke of the block M is greater or less than the stroke due to the eccentric sheave driving the link, approximately in the ratio of d to c. Hence if r is the radius of the cut off eccentric, the half stroke of M is given by

it being understood that d is a variable quantity depending upon the speed of the governor. Neglecting the obliquity of the valve rod Q, due to the constraint of its motion by the suspending link G, and the obliquity of the eccentric rod, the above expression is the half stroke of the valve. Thus for a given value of d the valve diagram can be drawn as in Fig. 55.

68 The Corliss gear. This gear was introduced about 1849 by G. H. Corliss, of Providence, U.S.A.—The characteristic features of the gear are four independent distributing valves of the kind illustrated in Figs. 23 to 26, two for the admission and cut off of steam, and two for the release and compression, and a valve gear mechanism which gives a continuous rocking motion to the exhaust valves, and at the same time allows the steam valves to cut off the supply of steam sharply at a fraction of the stroke determined by the governor. Amongst the many forms of the gear which have been devised, the Spencer Inglis type made by Messis Hick, Hargreaves and Co., occupies a prominent place. The rocking valves of this type have been described in Art. 28, and the general arrangement of the gear used to work them is shown in Fig. 65. The basis of the mechanism is a four bar chain, six of which combine to four the mechanism is a four bar chain, six of which

Consider the exhaust valve E in the figure. A circular plate, centred at A, is coupled to an eccentric on the crank shaft by the pin Z, so that  $AZ_i$  the eccentric rod, and the eccentric form together a four bar chain. A pin B in the plate is coupled to the crank arm CD by the coupler  $BD_i$ , this combination forming a second four bar chain. Similarly A,  $B_i$ ,  $C_i$ ,  $D_i$  is the chain for the exhaust valve  $E_i$ . There is a similar four bar chain for each of the steam valves S and  $S_i$ ; but when the cut off is to be made automatic the coupler in each of these two chains is made telescopic, and the connection between the two halves can be temporarily destroyed by means of a trigger. Immediately the two halves



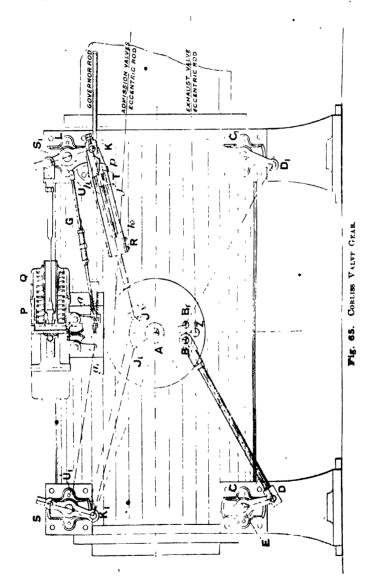
are disconnected the steam valve corresponding to the coupler is unconstrained by the valve gear, and a strong spring Q, in a dashpot P, immediately closes the valve. The way this is done can be seen from the figure, which shows the coupler to the right-hand steam valve in detail.

AJ and KL are the two canks of the four bar chain to the valve  $S_i$  and JK is the telescopic coupler, one part of which terminates at j, and the other part at k. The part  $J_J$  has a square block R formed about the middle of its length to which two flat springs are bolted which stretch along to, and engage with, projections formed on the other part of the coupler

The part terminating at k is suitably formed near the end K to carry a pin p, on which a trigger or eatch T is free to turn, its turning being controlled by the curved lever k, terminating in the joint U. This point U is connected, through the rod U and the lever U, with a short shaft, to which the governor gives an angular motion as the speed varies, which angular motion causes a small motion of the point U. A corresponding point,  $U_1$ , on the left side receives a similar motion through the toothed sectors attached to the levers U and U. When the engine is running at a uniform speed,  $U_1$  and of course  $U_2$ , are fixed points.

The steam valve  $S_i$  is opened by the movement which puts the coupler in tension, the projecting edges of the springs belonging to the part  $J_I$  gripping on corresponding projections on the part Kk, and as the necessary movement towards the centre of the cylinder takes place, U being fixed, the trigger T turns relatively to the coupler, forces the springs apart, and thus easts the crank LK free from the valve gear. The part  $J_I$  continues its movement, but the part Kk instantaneously flies back under the action of the spring Q, the dashpot P moderating the action of the spring. This latter part remains at rest, the valve being closed, until the spring catches belonging to the other half glide over the projections and close up in the position where they engage with them immediately the movement is reversed. The instant at which the trigger T releases the spring catch depends upon the position of the point U. When the load is thrown off an engine of this type, the governor changes the position of U sufficiently to cause the release of the trigger so early in the stroke that hardly any steam is admitted to the cylinder. If a load be now suddenly thrown on, the governor immediately moves U to a position where steam is taken through a large fraction of the stroke. The control effected in this way is well exhibited when the engine is used to drive a rolling mill.

When the ingot is put in the rolls the full load is thrown on the engine, but after a few seconds the ingot has passed through, and



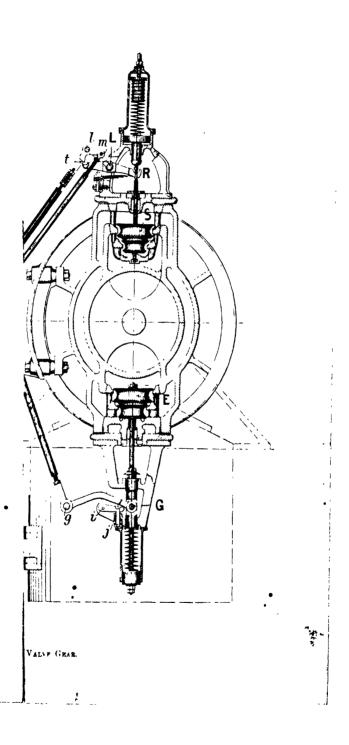
nearly the whole load is thrown off; the valve gear answers at once, and automatically refuces the cut off. The cranks AJ and  $AJ_1$  are determined by pins  $J_1$  and  $J_1$  put in a circular plate, immediately behind the plate driving the exhaust valves, and connected to the crank shaft by a separate eccentric rod which is driven by a separate eccentric. There are thus two eccentric sheaves on the shaft driving respectively the steam valve plate and the exhaust valve plate.

The valve displacement curve for each of the exhaust valves can be set out by drawing the gear in a series of configurations corresponding to, say, 24 equidistant crank positions, and measuring off the corresponding displacements of the edge of the valve from some selected position, finding thereby 24 points on the diagram through which the curve must pass

The shape of this curve will be very different from that shown in Fig. 38 for the simple eccentric gear. The displacement curves of the steam valves can be drawn in a similar way for a given position of U.

69 · Sulzer gear. The Sulzer valve gear was introduced in 1867 and includes a governor. It is designed to work four valves per cylinder, two admission valves and two exhaust valves. A pair of steam and exhaust valves control each cycle in the way explained in Art 2 and indicated diagrammatically in Fig. 1. Corresponding to these valves there are really two valve gears, one for each cycle. Fig. 66 shows a cross section of the high pressure cylinder of a Sulzer engine, taken through the valves controlling the instroke cycle, and the figure, shows also the gear for operating the valves. The valve and valve gear are duplicated for the outstroke cycle, being placed at the end of the cylinder remote from that shown. Restricting our attention to the instroke cycle, steam is admitted to the cylinder by the valve S, shown open, and released from the cylinder through the exhaust valve E, shown shut. The steam valve has already been illustrated in detail, Fig. 7. The exhaust valve is similar in construction to the steam valve, having four seats. The valve gear may be analysed into a series of four bar chains, and to make this clear a skeleton diagram of the gear is drawn to the left of the actual drawing, so that the geometrical basis of the Frear can be followed castly. The lettering on this skeleton diagram corresponds with the lettering on the actual drawing.

A shaft A, placed alongside the engine and driven by equal gearing from the crank shaft, is supported in journals carried by two brackets which are bolted to the cylinder itself, one of which, lettered B, is seen in the figure. Keyed to A is an eccentric sheave, the crank corresponding



to which is shown by Aa in the skeleton diagram. A point c on the eccentric rod is jointed with a crank arm cC, which is centred on the shaft C, this shaft being merely a support for this clunk. This combination of two cranks, Aa and Cc, and the connecting link ac forms, with the fixed frame, a four bar chain. Every point in the eccentric rod, shown black in the skeleton diagram, is thus constrained to move in a definite path

First trace out the connection of this chain with the exhaust valve One arm, namely dD, of the bell crank dDe, is connected by the rod du to the crooked crank qG. The bell crank is centred on a supporting shaft D, carried by the bracket B. The crooked crank is jointed to the enlarged part of the valve spindle. These links, namely, the cranks Dd, Gq, and the coupler dq, together with the frame form a four bar chain, the movement of which is determined by the connection of the arm De of the bell crank lever to the eccentric rod by the link ch. If the link Gg could vibrate, free from obstruction, about G as a fixed centre, the turning of the shaft A would merely cause the crink qti to execute vibrations about G as centre, and the exhaust valve G would always remain shut. Just below the lever gti, however, there is a bar, whose position is adjustable about the axis i by means of the bolt j. This is set up and clamped in position to act as a fixed fulcrum, so that the crooked crank at a certain instint in its downward movement is brought into contact with it, and then the crank acts as a lever and lifts the exhaust valve off its seat. In the skeleton diagram the fulcrum The actual arrangement is, however, equivalent to is shown at k a moveable fulcium since the curved under-surface of the crooked crank qG, during its downward angular motion, touches the fulcrum piece along a line which moves continuously to the left. The leverage is changing, but it is greatest just at the opening of the valve and least when it is fully open. Consequently the velocity of the valve is small when it is opening and when it is closing. In this way the valve is let down on to its seatings gently and is held there by the combined action of the steam and the spring seen in the drawing, after the crooked  $\operatorname{crank}\ gG$  leaves the fulcrum piece altogether in the course of its. upward angular movement

Consider now the connection to the steam valve. One end of a coupling rod is jointed to the eccentric rod at c and the other end to a crank Ll, L being a fixed axis. Thus the two cranks Cc, Ll, and the rod cl form with the framework a four bar chain deriving motion from the eccentric sheave. Mounted on the axis at l is a catch or trigger tlm, one end of which is jointed by means of the coupling rod win with a bell crank lever, whose central axis, c, is carried on the

eccentric rod itself. The other arm, op, of this bell crank is linked to the point F, which occupies a definite position when the governor is running steadily. The motion of the eccentric rod and the connection of the arm op to F fog ther cause an angular motion of the bell crank about its axis o which angular motion is transmitted by the coupler nm to the (rigger mlt). The motion of the trigger is thus made up of two components, one the movement of its axis l in the arc of a circle about L, the other an angular motion about the axis l. The angular component changes as the position of F changes. The position of F is controlled by the governor, any change in its configuration being accompanied by a change in the angular position of the shaft Q, which is directly connected to the governor. The several positions occupied by F for cut offs of zero 20 and 55 per cent of the stroke are shown in the figure.

The path of the inside edge t of the trigger consequent upon the combination of the motion of its axis t, with the angular motion about the axis when F is in the position for 55 per cent cut off, is shown in the enlarged detail Fig. 67. Also the path when F has moved into the

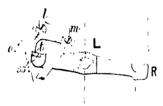


Fig. 67. Seezer Clark Detail of Thisoen

position where cut off takes place at the beginning of the stroke, that is at zero per cent. From these curves it will be clear that the downward motion of the trigger brings the inside edge t into contact with the lever LR, and opens the steam valve, when part of the curved path of t has inside the arc of the circle passing through the extreme edge of the lever LR, and also that the trigger slips out of contact when the path of t cuts this circular arc. When this happens, the steam valve is free from the control of the valve gear and passes under the control of the apring and dashpot, the combined action of which urges the valve back into its scatting gently, but at the same time sharply, so that there is little or no wire-drawing of the steam. The cut off may be thus varied from stroke to stroke according to the instantaneous position of

F, and since this position depends upon the slight fariation of the governor speed, which in its turn depends upon the fariation of the load against which the engine is working, the cut off is automatically adjusted to the variation of the load.

To set out a gear of this kind, with the object of drawing the path of the edge t, in order to find the cut off for a given position of the point F, the gear must be set out in a series of positions corresponding to, say, 24 equidistant crank positions, finding thus 24 points on the path of t. Joining these points by a curve, the intersection of the curve with the circular path of the edge of the lever RL is easily found, and by interpolation with the numbered points in the neighbourhood, the corresponding crank angle can be interred, and hence the piston position. The process of setting out the gear for a stated crank angle and given position of F is as follows —

- (1) Set out the given position of F, the positions of the fixed centres A, C, D L, G, and also the angular position of the eccentric radius corresponding to the given crank position.
- (2) With radius Cr and centre C draw an arc and with radius αc and centre a cut it in c.
- (3). Set out the points o, h, along the eccentric rod, and with centre o and radius op draw an are and cut it in p with an arc of radius Fp drawn from the centre F
  - (4) Draw the remain ag arm on of the bell crank
- (5) With centre L and radius Ll draw an arc, and cut it in l by an arc of radius cl and centre c. This defines the position of the axis of the trigger. With radius lm and centre l draw an arc, and cut it in m with an arc of radius nm and centre n, thus defining the angular position of the trigger with regard to its axis.
- (6) Set out the edge t of the trigger, and one point in the path is determined.

No difficulty will be found in setting out the position of the exhaust valve for a given position of the fulcrum piece y.

In the actual drawing of these curves the long coupling rods may be "suppressed" in the manner illustrated in detail below in connection with the setting out of a Joy valve gear, Art 126. In this way it is possible to draw the paths of the various points to a large scale without using an inconveniently large drawing-board.

# CHAPTER VI.

### THE ANALYTICAL METHOD.

70 The analytical method. A brief explanation may now be given of the method of working valve gear problems analytically. The nalytical method contains implicitly within its symbols all the geometrical methods for the solution of valve gear problems. The tools in his case are merely a table of sines and cosines, which need not give he values to more than four significant figures, and a table of four figure ognithms. A student who can use these with rapidity and accuracy vill find that problems connected with the simple valve gear may be leaft with as quickly by these means as with the tools of geometrical vork, namely, compasses, set squares, etc. with the advantage of greater recuracy, and often of greater speed. The most advantageous way of working is to combine the two methods, using one as a check on the other.

The work may be divided into two distinct parts --

- The calculation of the piston position for a given value of the crank angle θ, or vice versa.
- (2) Calculations regarding the valve geni in connection with the crank angle  $\theta$ .

Thus the crank angle  $\theta$  is made the independent variable, and, for any assigned value of it, there is one corresponding position of the piston, and one position of the valve.

71. Grank and connecting rod. Considering first therefore the position of the piston in relation to the crack angle  $\theta_i$  it will be observed from Fig. 68, where OQ is the crank radius R, and BQ is the length of connecting rod l, that if the connecting rod is infinitely long the displacement X from the central position is given by Op, which is

equal to  $R\cos\theta$ , but that the effect of obliquity is to increase this distance by the amount  $\rho q$ . From the figure it will be seen that with



Fig. 68. CRANK AND CONNECTING ROD - PEFFCH OF OBLIQUITY.

the cylinder to the left of the shaft pq is always positive, that is, for every crank position, the point q falls to the right of p, so that the effect of obliquity is the amount pq measured from p towards q. If the cylinder were to the right of the shaft, pq would be negative but all the diagrams in this book are drawn for the cylinder to the left, so that pq is always to be regarded as positive and is to be added to the quantity  $R\cos\theta$ , whether this be positive or negative. Hence for the piston displacement,

$$X = R \cos \theta + pq$$

By Euchd Book III 35,

$$pq(Bp + Bq) = (Qp)^2$$

But since pq is always small in comparison with Bp, very little error is introduced if Bq, which is the length of the connecting rod l, is written for Bp so that (Bp+Bq) becomes equal to 2l. And Qp is equal to  $R\sin\theta$ , therefore

$$pq = \frac{R^4 \sin^2 \theta}{2l}$$
 approximately,

and finally.

$$X = R \cos \theta + \frac{R^{\epsilon_{\min} 2} \theta}{2l} \dots \dots \dots (1)$$

Dividing through by R,

$$\frac{X}{R} = \cos \theta + \frac{R}{2I} \sin^2 \theta \dots \dots \dots \dots (2)$$

This gives the fraction of the half stroke at which the piston is distant from its central position, and is positive for all positions to the right of the centre, and negative for all positions to the left. The fraction of the whole stroke at which the piston stends from the dead point corresponding to  $\theta = 0$  is given by

$$\frac{1-X/R}{2}$$
 .....(3)

and from the dead point corresponding to  $\theta = 180$  degrees, by

$$\frac{1+X/R}{2} \qquad .... \tag{4}$$

 $\frac{X}{R}$  in each case may of course be positive or negative.

To find the angle  $\theta$ , for a given value of X R, equation (2) must be solved for  $\cos \theta$ . Writing  $(1-\cos^2\theta)$  for  $\sin^2\theta$ , n for the ratio of the length of the connecting rod to erank l/R, and f for X/R, (2) reduces to

$$\cos^2\theta - 2n\cos\theta + (2nf - 1) = 0.$$

the solution of which is

$$\cos \theta = n - \sqrt{(n^2 + 1)} - 2\sqrt{f}$$
 .... (5)

The minus sign is used before the root because the plus sign would give a value of  $\cos \theta$  greater than unity, which is inadmissible.

If the connecting rod is  $5\frac{1}{2}$  times the length of the crank, so that n=5.5, the equation becomes

$$\cos \theta = 5.5 - \sqrt{31.25 - 11} \hat{f} \dots$$
 (6),

from which the different values of  $\cos\theta$ , corresponding to assigned values of f, may be computed

It should be noted that the quantity to the right may come out either positive or negative. If positive, the angle  $\theta$  has between 0 and 90 degrees, or 270 and 360 degrees. If negative,  $\theta$  has between 90 degrees and 270 degrees. Which value of  $\theta$  to take in any particular case must be determined by the conditions of the problem

The piston curve, Fig. 38, is the graphical representation of (6) and could have been plotted from 15.

72 The valve displacement. The valve displacement x is given in terms of the crank angle  $\theta$  by (see Art 42) —

$$x = r \cos(\theta + \phi)$$
 for positive rotation of the crank with outside admission ......(1),

$$x = r \cos(\theta - \phi)$$
 for negative rotation of the crank with outside admission ..... (2),

$$x = r \cos(\theta - \lambda)$$
 for positive rotation of the crank with inside admission .......(3),

All these relations are expressed by equation (1), provided that the angular position of the eccentric sheave with regard to the crank is

always measured in the positive direction; and for analytical work this restriction of  $\phi$  to a positive value is very convenient. In what follows therefore it is to be understood that  $\phi$  may have any positive value between 0 and 360 degrees, and that for the conditions expressed by equation (1), the value has between 90 and 180 degrees, by equation (2) between 180 and 270 degrees, by equation (3) between 270 and 360 degrees, and by equation (4) between 0 and 90 degrees.

Considering equation (1), it is to be observed that, for a given value of  $\theta$ , the angular advance being known the corresponding value of x can be calculated without ambiguity.

For a given numerical value of i, however, there are four possible values of the angle  $\theta$ . Thus, equal numerical values of x, namely ab, cd, ef, gh, Fig. 69, correspond to the unequal angles, Oa, Oe, Oe, Og. To discriminate between these angles, observe, first, that two of the values of i are negative and two positive — condition that of the two negative values, one, namely ab is increasing in value as the angle increases, and the other, id is decreasing as the angle increases. Similarly, of the two positive values, ef is increasing, and gh is decreasing, with the angle

It a numerical value of r is assigned therefore the corresponding value of the angle cannot be fixed until we know

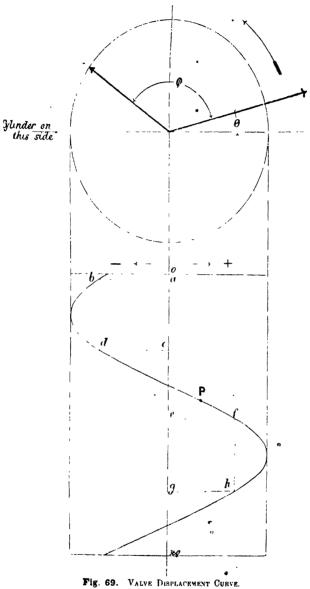
- (a) the sign of i,
- (b) whether x is increasing or decreasing with  $\theta$

In connection with the present subject however, it is generally unnecessary to examine formally whether x is increasing or decreasing, because the appropriate value can be determined by other considerations.

Table 1 shows the sign to be given to a for any particular event in the stroke, both for positive and negative rotation of the crank, and also the way to discriminate between the two angles which correspond with, either a positive, or a negative, sign

If the exhaust hap is negative in any particular case, the signs given in the table to release and compression must be changed.

With regard to negative rotation, it must be remembered, that although the crank is revolving negatively, no difference is made in the way of measuring the crank angle, that is to say, it is always measured in the counterclockwise direction, from the zero crank position. The crank in its negative rotation is therefore considered to go from 0 to 355, 358 degrees, etc., standing at 270 degrees when it has made one-quarter of a revolution, and at 90 degrees for three-quarters of a revolution.



### TABLE 1.

	or no	e given to	on of th	n crank 	Crank	angle #
	Instroke	Outstroke Cycle			Positive Relation	Negative Rotation
Admission	-	, +	+		Larger angle	Smaller angle
Cut off	· _	÷	+	_	${\bf Smallerangle}$	Larger angle
Releaso		-	-	ŧ	Smallerangle	Larger angle
Compression	+	_		+	Larger angle	Smaller angle

Equation (1) involves (we constants, r and  $\phi = \Omega$ ) the two constants are given, the corresponding displacement curve is completely determined. If these values are not given, the specimention of two points on the curve enables them to be found. The specimention of a point, P say, Fig. 69, requires that its distance r from the vertical axis be given, and also the corresponding value of the angle  $\theta = \Omega$  ence, to specify two points, the values  $r_{r}/\theta_{r}$  must be given for P and the values  $r_{r}/\theta_{r}$  for a second point Q. This ring these in the equation for the curve,

$$\begin{cases} r_1 = r \cos \left(\theta_1 + \phi\right) \\ r_2 = r \cos \left(\theta_2 + \phi\right) \end{cases} \qquad (5),$$

a pair of simultaneous equations from which x and  $\phi$  may be found

The equations in  $\alpha$  be written in a form which is sometimes useful Expanding equation (4)

$$x = A \cos \theta - B \sin \theta \dots (6)$$

where A and B are written for  $r\cos\phi$  and  $r\sin\phi$  respectively. A and B are connected by the relation

$$A' + B' = r^2$$
 .....(7)

and the numerical value of  $\tan \phi$  is given by

$$\tan \phi = \frac{B}{A} \qquad ... \qquad$$

The actual value of  $\phi$  depends upon the direction in which the crank shaft is to rotate and whether steam is to be admitted at the outside or mode of the value. When these data are given, the quadrant in which the eccentric radius stands, relatively to the crank, is known. In this form the pair of simultaneous equations (5) become

$$\begin{cases} x_1 = A \cos \theta_1 - B \sin \theta_1 \\ x_2 = A \cos \theta_2 - B \sin \theta_2 \end{cases} ....(9),$$

from which A and B may be found and hence r and  $\phi$ .

These equations may be used for the solution of valve gear problems, directly x is expressed in terms of the quantities concerned in the distribution of the steam. The next table gives simultaneous values of x and the crank angle  $\theta$ , each pair of values corresponding to a definite point on the displacement curve when the proper sign has been given to x, and the proper angle fixed upon from Table 1.

TABLE 2

Numerical value of v equal to	Correspondenz ungle	
Steam lap $+$ lead $= L + e$	$\theta = 0$ or 180 degrees	
Steam lap $\dots = L$	t - crank angle at cut off or admission	
Exhaust lap : t	θ - crank angle at release or compression	
Steam lap + maximum width of port opening for steam $= L + W = r$	$\theta + \phi = 180$ or 0 degrees.	
Exhaust lap + maximum width of port opening for exhaust = $l + w = r$	$\theta + \phi = 180$ or 0 degrees.	

For instance, find the value of  $\theta$  at "cut off" for the instroke cycle, in the case of negative rotation with outside admission, when the lap is 1 inch. In this case the angular advance,  $\phi$ , must have a value between 180 and 270 degrees. Let it be 260 degrees. Then, from Table 2,

$$1 = r \cos (\theta + 260)$$

From Table 1, the sign of x for this particular event is stated to be negative, therefore the minus sign must be prefixed to the figure 1, and the larger value of  $\theta$  will be the required result.

73. The valve velocity. The velocity, v, of the valve is found at once from the displacement by differentiating x with regard to the time. Thus

$$x = i \cos(\theta + \phi)$$

Therefore

$$v = \frac{dr}{dt} = -r \sin(\theta + \phi) \times \frac{d\theta}{dt} \dots (10),$$

When the crank is revolving uniformly, the angular velocity,  $\frac{d\theta}{dt}$ , is constant, and is equal to

$$2\pi n$$
,

where n is the number of revolutions per second. Hence for uniform rotation,

$$v = -r \sin(t^{\dagger} + \phi) 2\pi u$$
 . . . . . . . . . . (11).

When using this expression remember to express i in feet in order to get the velocity in feet per second

The last three articles contain the whole of the mathematical relations involved in the analytical freatment of a simple eccentric gear. A few examples are added, starting first with the examination of a given gear.

74. Example. A valve gear has the following dimensions:-

$$r=3$$
 mehes, 
$$\phi=120~{\rm degress},$$
 
$$L=1.375~{\rm mehes~for~both~cycles},$$
 
$$l=0.1~{\rm meh}$$

n, the ratio of the length of the connecting rod to the crank = 4.

Since  $\phi$  hies between 90 and 180 degrees, the crank shaft rotates in the positive direction with outside admission. Calculate the value of the lead, and the fractions of the stroke at which the several events of admission, cut off, release and compression take place, for the instroke and outstroke cycles respectively.

The equation to the valve displacement curve is

$$\alpha = 3\cos\left(\theta + 120\right)$$

To find the lead, calculate the value of x when  $\theta=0$ , and subtract the steam Lap. Thus, at the dead point,

$$x = 3 \cos 120$$
, from which  $x = -15$  inches.

The corresponding lead is therefore 0.125 inch

The lead for the outstroke cycle is also 0.125 inch.

For cut off and admission to the instroke cycle,

$$-1375 = 3\cos(\theta + 1.0),$$

from which

$$\cos(\theta + 120) = -0.458$$

This is the numerical value of the cosine of an angle of 62 degrees 42 minutes, but since the sign is negative, the two angles having this value of the cosine are

180 - 63 - 117 degrees = 
$$\theta_1$$
 + 120,

0

$$180 + 63 = 243 \text{ degrees} = \theta_2 + 120$$

The corresponding values of  $\theta$  are -3 or +357 degrees, and 123 degrees. From Table 4, the latter being the smaller corresponds to "cut off" and the larger to "admission".

Proceeding in an exactly similar way with the value of the exhaust lap, it will be found that release and compression take place respectively at 152 and 328 degrees

In this example, the steam and exhaust laps are assumed to be equal for the two excles. The crank angles for the four events of the outstroke cycle can be found therefore by merely adding 180 degrees to those angles just found subtracting 360 degrees when the sum is greater than 360 degrees.

To find the corresponding piston positions introduce the value for the ratio of the length of the connecting rod to the crank, u, given above, into equation (2). Article 71, obtaining

$$\frac{X}{R} = \cos \theta + \xi \sin \theta.$$

For convenience of retrience the details of this citeriation, and the summary of the preceding ones, are given in the next Table

The velocity of the valve at cut off for the instroke cycle, assuming the crank to make 3 revolutions per second, is found from equation (11) by introducing

$$r = \frac{1}{10}$$
 feet,  $\theta = 123$  degrees,  $\phi = 120$  degrees, and  $n = 3$ .

Thus 
$$v = -\frac{1}{3} \sin(243) \times 628 \times 3 = +42$$
 feet per second.

The + sign indicates that the valve is at the instant moving in the positive direction, that is from left to right.

Referring to Table 3, it will be seen that the effect of the obliquity of the connecting rod is to cause a difference of the point of cut off in the two cycles of about 8½ per cent and a difference in the compression of about 3½ per cent.

TABLE 3.

	Crank angle d	er s d	1 sin d	1	Corresponding percentage piston position
Instroke Uyele		-	-		1
Admission	357 3	+ 0.998	+ 0 0001	$\pm 0.998$	999
Cut off	1123	$\{-0.544$	+0.088	-0.456	728
Release	152	- 0.882	<0.028	-0.554	927
Compression	328	+0.48	+0035	+ 0.883	941
Outstroke Carle					
Admission	177	~ () 995	+0.0004	0.997	99.8
Cut off	303	+0.511	1.0.088	(0.632	816
Release .	332	0.882	0.025	+ 0.910	95.5
Compression	145	0.848	+0.035	- 0813	90 6

The compressions may be equalized at 944 per cent by decreasing the exhaust hap belonging to the outstroke cycle or at 906 per cent by increasing the exhaust hip of the instroke cycle. Take the former case, First, compute the value of  $\theta$  for a piston position of 944 per cent of the stroke, from equation (5). Article 74, substituting 4 for the ratio of the length of the connecting rod to the crank,  $n_e$  and the value = 0.883 for f obtaining.

$$\cos\theta = 4 - \sqrt{17} + 8 \times 0.883,$$

from which

$$\cos \theta = -0.9$$

The two angles corresponding to this are 154 degrees 10 minutes, and 205 degrees 50 minutes. The outstroke cycle is under consideration, which begins at 180 degrees, so that the smaller value of the angle does not come into the cycle unless 360 degrees be added. But the angle may be looked upon as belonging to the previous outstroke cycle, and it gives the point at which compression takes place. The other value of the angle is evidently an impossible one for the event of compression, since it would have to take place when the crank had turned through only 25 degrees 50 minutes from the 180 dead point position.

The valve displacement corresponding to this compression angle is

$$x + 3\cos(154 + 120)$$
  
=  $3\cos 86 = 0.21$  mch.

From Table 1, the sign of the valve displacement at compression in the outstroke cycle is negative when the exhaust lap is positive. Therefore, since the sign of the displacement is here positive the exhaust lap is negative and would be set out to the right of the vertical centre line in the salve diagram.

75 The design problem. Given the maximum port opening for steam, W, the lead, e, the position of the piston at cut off, and the ratio of the length of the connecting rod to the crank, find the eccentricity, r; the angular advance,  $\phi$ , and the steam lap, L. Assume positive rotation with outside admission.

First, find the crank angle corresponding to the given cut off from equation (5), Article 71, or read it from a piston curve drawn with the proper ratio of crank to rod

The problem is now reduced to the finding of r,  $\phi$ , and L, having given W, e, and  $\theta_{\sigma}$ .

In this case, the constants of the displacement curve have to be found, so that in the first instance the unknown quantities are A, B, and L. Examining the data it will be perceived that it is not possible to find A and B from equations (9), Article 72, but that there is a relation amongst the data, from which a third equation can be formed. This relation is obtained from the fact that the steam lap, added to the maximum port opening, is equal to the eccentric radius. Equation (3), below, expresses this in terms of the unknowns A and B.

Considering the instroke cycle, select the pair of values from Table 2 corresponding to the dead point where  $\theta = 0$  (since the engine is to work with outside admission and the crank shaft is to turn in the positive direction,  $\omega$  is of course negative), and insert these in equation (6), Article 72, thus forming equation (1)

Again select the values of the coordinates at cut-off from Tables 1 and 2 and insert these in equation (6). Article 72, writing p for  $\cos \theta_{\sigma}$  and q for  $\sin \theta_{\tau}$  and equation (2) is formed

 $\vec{A}$ , B and L may now be found from these three simultaneous equations

$$-L = Ap - Pq \dots$$
 (2),  
 $L + W = v A^2 + B^2 = v \dots$  (3).

Eliminating L from (3) and (1) and squaring

$$-2Ab = B^2 - b^2$$
, where b is written for  $(W - e)$  .....(4).

Eliminating L from (2) and (1) .

$$A(1-p) = -e - Bq \dots (5)$$

Eliminating A from (4) and (5), there results a quadratic in B, the solution of which is

A solution of this is Always possible, since from the nature of a valve genr e is always less than W and p is always less than unity, so that the product under the root is always positive

Having found B from (6), A can be found from (5)

Two values of B will be given by (6), but since by the given data  $\phi$  is between 90 and 180 degrees, B (that is  $\sin \phi$ ) must be positive, therefore the positive value must be taken and this inserted in (5) will give the proper value of A

The steam lap can now be calculated from equation (1)

The eccentric radius  $r_i$  is equal to  $\sqrt{A} + B$ .

The numerical value of  $\tan \phi$  is found from

$$\tan \phi = \frac{B}{A}.$$

Example -

Let the data be,

Lead = in inches

Maximum opening for steam = 1 inch

Crank angle  $\theta$  at cut off = 120 degrees, so that

$$\cos \theta = -0.5 \quad p_0$$

$$\sin \theta = 0.866 = q$$

Moreover, suppose the crank shaft is to turn in the positive direction, and that steam is to be admitted at the outside of the valve

Inserting the above values of p and q in (6),

$$B = +1.615 \text{ or } -0.576$$

Substituting the positive value of B in (5),

$$A = -0.995$$

Using A in (1), L the steam lap is found to be 0.895 inch.

With this value of L in (3),

$$0.895 + 1.0 = 1.895$$
, the eccentric radius

The numerical value of  $\tan \phi$  is found from

$$\oint tan \phi = \frac{1615}{0995} = 1624.$$

The angle corresponding to this is 58 degrees 24 minutes, but because rotation is to be positive, and steam is to be admitted at the

outside of the valve, the angle lies between 90 and 180 degrees (see Fig. 32), therefore its actual value is

180 - 58 degrees 24 minutes = 121 degrees 36 minutes.

These equations hold for positive or negative rotation with outside admission

If positive values of the displacement are used in equations (1) and (2), the sign of e in (5) is changed, and the sign of the first term in the numerator of (6) is changed to minus. The equations then hold for positive or negative rotation with inside admission. For "cut off" at a given fraction of the stroke it is only necessary to solve the equations for one setting, positive rotation with outside admission for instance, because the numerical values of A and B are the same for all four cases

**76 The Meyer gear.** So far as the main gear is concerned, the calculations are made in exactly the same way as for a simple gear. The new problem is to find the setting and the lap of the cut off blocks, or plates, so that cut off may take place at a stated fraction of the stroke. In order to do this, the distance,  $\xi$ , of the expansion plates from their central position with regard to the main valve must be found in terms of the crank angle.

Let  $r_i \phi_i$  be the eccentricity and the augular advance respectively, of the main eccentric sheave, and  $r_i$ ,  $\phi_i$  the corresponding quantities for the expansion eccentric sheave

Then  $\sigma$ , the displacement of the main valve from its central position, is given by

$$i = i \cos(\theta + \phi)$$
,

and  $x_i$ , the displacement of the expansion plates from their central position with regard to the cylinder, by

$$x_1 = r_1 \cos(\theta + \phi_1)$$

Expanding these and writing generally A for  $\tau\cos\phi$  and B for  $r\sin\phi$ , they become

$$a_1 = A_1 \cos \theta - B_1 \sin \theta.. \tag{2}$$

The displacement,  $\xi$ , of the expansion plates from their central position with regard to main valve, is given by

$$\xi = x_1 + x = C \cos \theta - D \sin \theta \quad .... \quad (3),$$

where

$$C = A_1 - A = r_1 \cos \phi_1 - r \cos \phi$$
 ... (4),

$$D = B_1 - B = r_1 \sin \phi_1 - r \sin \phi \quad \dots \tag{5}$$

Multiply and divide the right side of equation (3) by  $\sqrt{C^2 + D^2}$ .

Then the coefficient of  $\cos\theta$  is

$$\frac{C}{\sqrt{C+D^2}} = \cos \psi$$
, say,

and the coefficient of sm  $\theta$  is

$$\begin{array}{ccc} D & \sin \psi, \\ \chi & D & \\ \tan \psi & U \end{array}$$

and

which is equivalent to

$$\xi = V = D \cos(\theta + \psi) = \rho \cos(\theta + \psi) \dots$$
 (6)

In this equation  $\psi$  is the angular advance of an inerginary eccentric sheave of radius  $\rho$  = x C+4, D

When the dimensions of the generic given C and D can be calculated, and from them  $\rho$  and  $\psi$  may be found and introduced into equation (6). Then, by means of (6)  $\xi$  can be calculated for any given value of  $\theta$ . If  $\theta$  is given for the cut off angle of the crank, the lap of the cut off plates considered in relation to the ports in the main valve, is given by

This Pap is positive when  $x_i$  is numerically greater than  $x_i$  and negative when  $x_i$  is numerically less than  $x_i$ .

To make use of equation (6) in the design of the cut off-plates and adjusting gear, the process is first to educate the values of the crank angles for cut off at, say, 10, 20, 30, 40, 50, 60 per cent of the stroke, for both the cycles, and then using these in (6), find the corresponding values of  $\xi$ . These values are the respective laps required for cut off at the fractions of the stroke from which the different values of the crank angles were calculated.

Comparing these values of L, it will be found that to secure equality of cut off at a given percentage of the stroke the laps must be different. The gear can be set to allow this difference in the laps. It will also be found that this difference requires to be changed for each cut off, to secure equality all through the range taken. This of course cannot be arranged for, because the valve can only be set for one difference between the laps. An example will illustrate the way of using the equations.

77. Example. Meyer gear. The following are data from an engine fitted with the Meyer cut off valve.

Ratio of the length of the connecting rod to the crank, 5.5	n
Eccentricity of main gear eccentric, 15"	r
Angular advance of sheave, 130 degrees	φ
Eccentricity of cut off sheave, 15"	$r_1$
Angular advance of cut off sheave, 180 degrees	$\phi_1$

Find the lap of the expansion valve so that cut off may take place at 10, 20, 30, 40, 50, or 60 per cent of the stroke, for both the instroke and outstroke cycles, and deduce from these laps the best setting of the expansion valve.

The first step is to calculate the series of crank angles corresponding to these given fractions of the stroke. These are to be computed by means of equation (6), Article 71, the numbers there introduced being those for a connecting rod 5.5 times the length of the crank.

The details of the calculation are set out in the following table. It may be observed that when the crank angle corresponding to a stated

 $\label{eq:table 4}$  The crank angle  $\theta$  is found from  $\cos\theta = 5.5 - \sqrt{31.25 - 11} f.$ 

			•	l 	Actual Cr	ank Angle
Piston I	osition	ſ	co.#	0	Instroke	Outstroke
	Instroke	_	Dead Point		0	0°
	10 7	0.8	0762	40-18'	40 18	319^42
	20 1	0.6	0.535	57 36′	57 36'	302" 24
	30 ;	0.4	0.318	71 30′	71' 30'	288 30
60 %	40 '	0.2	0 109	83 42'	83 42	276° 18
50 °/。	50 7,	0.0	-0.090	84° 48′	95 ' 12'	264° 48
40 '/	60 %	- 02	-0.281	73 30	106 '30'	253° 30
30 <sub>\(\alpha\)</sub>		-04	-0471	61 54	118-6′	241° 54
<b>20</b> 1/		- 06	-0.652	49 18'	130 42'	229° 18
10 %		-08	-0.829	34~0′	146 0'	214° 0′
) itstroke		!		-		
				Dead Point	180	180°

piston position has been found for the instroke cycle, the angle in the outstroke cycle corresponding to this position is given by  $360-\theta$ . The angles found in this way are shown in the right-hand column of the table.

With the given data the respective values of C and  $D_i$  from equations (4) and (5), Article 76, are

$$C \cdot 15 (-1 - (-0.6427)) = -0.536$$
  
 $D = 1.5 (0 - 0.766) = -1.149$ 

and hence

$$\rho = \sqrt{C_1 + D_2} = 1.266$$
,

and the 
$$\psi \approx \frac{-1.149}{-5.36} \approx \pm 2.144$$
 .  $\psi$  therefore is equal to 64° 58′, say

65 degrees from the tables but the negative signs above prefixed to both the numerator and denominator show that the angle is in the 3rd quadrant, so that  $\psi = 180 \pm 65 \pm 245$  degrees

Therefore from (3) Article 76

$$\xi = 1.266 \cos(\theta + 245)$$

Introducing the values of  $\theta$  given in Table 4 successively into this equation, the results in the second column of Table 5 are obtained for the instroke cycle, and those in the third column for the outstroke cycle.

TABLE 5.

Laps						
Cut Off	Instroke	Outstrake	Difference			
10	- 034"	- 0.20 ′	014			
20 ,	- 0.68"	- 0.52 '	046			
30 1	- 0.92	$=0.76^{\prime\prime}$	0.16			
40 /,	- 1081	- 0.95"	043			
50 %	- 1 19"	110"	0.09			
60 /。	- 1 25"	- 1201	0.05			

The right-hand column gives the differences between the laps required to give equality of cut off at the stated fractions of the stroke. If the length of the valve spindle is adjusted so that when the cut off is at 20 per cent of the stroke the laps on the valve are 0.68 for the instroke cycle, and 0.52 for the outstroke cycle, the cut offs at 10 and 40 per cent will be nearly equalised, and at 20 and 30 per cent they will be exactly equalised. The inequality at 50 and 60 per cent must be accepted.

, א מ

The cut off by the main valve in the engine from which these data have been taken occurred at 70 per cent, of the stroke in the outstroke cycle, and 62 per cent in the instroke cycle. This inequality was of no moment, because the cut off for the normal conditions of working was between 20 and 30 per cent.

The main valve was set with unequal inside laps to equalise the compression points. Release by the main valve took place at 945 per cent for the outstroke, and 96 per cent, for the instroke.

The engine was indicated, and the pair of eards corresponding to any cut off between 10 and 40 per cent of the stroke were not sensibly different in area.

To find the velocity of cut off, the velocity of the expansion valve must be calculated with regard to the main valve. Thus, let  $v_1$  be the actual velocity of the cut off valve at any instant, and v the corresponding velocity of the main valve, then the velocity of the expansion valve relative to the main valve is

$$v_1 - v$$

This may be calculated by using expression (11), Article 73, to find the velocities separately but the most expeditions way is to differentiate expression (6) with regard to the time, obtaining

$$\eta = -2\pi n \rho \sin(\theta + \psi) \qquad . \qquad . \tag{7}$$

 $\eta$  being the velocity of the expansion valve with regard to the main valve

It is instructive to calculate the velocity corresponding to the several cut offs of the instroke cycle given in Table 4, which Table gives also the several values of the crank angle  $\theta$  required in the computation. The results are shown in the following Table 6. The factor with which the figures in the third column must be multiplied to give the result in fect per second, when the crank makes 2 revolutions per second, is  $\rho \, 2\pi n = 1.32$ .

The minimum lap on the inside of the blocks may also be calculated. Referring to Article 65, it will be remembered that the blocks having been adjusted to their maximum distance apart, the minimum inside overlap is given by the expression

$$u-z$$

u being the inside overlap when the blocks occupy their central position with regard to the main valve, and z the greatest diminution of u due to the motion of the blocks with regard to the main valve, z is in fact the maximum value of  $\xi$ . Hence the problem is reduced to finding for what crunk angle  $\theta$ .

$$\xi = \rho \cos (\theta + \psi)$$

is a maximum, and this is evidently solved by making  $\theta + \psi$  equal to 0 or 180, given  $\rho =$  the maximum value of  $\xi$ . Hence the minimum overlap is always given by

$$u - \rho$$

### TABLE 6

Velocities of cut off, in the example of the Meyer Gear - Instroke Cycle

Data  $r_1 = r = 0.125$  foot

 $\phi_1 = 180 \text{ degrees}$ 

 $\phi = 130 \text{ degrees}$ 

n=2 revolutions per second

Imaginary eccentric radius = 1.266/12 = 0.105 foot

Angular advance of imaginary eccentric = 245 degrees.

 $\eta = -0.105 \sin(\theta + 245) 2\pi n.$ 

Cut off	Crank Angle	8ιn (θ + ψ)	Velocity 1 t per sec when n 2
10 ,	40 18'	-0.964	1 27
20	57 36	-0.842	1 11
30	$71 - 30^{\circ}$	-0.688	0.91
4()	83 42'	- 0.519	0.69
50 🔩	95/12'	-0.339	0.45
60 /,	100-301	-0.148	0.19

78 Cut off plates. Constant lap Variable travel. In this case, the lap of the expansion valve is constant, and the cut off is varied by varying the travel of the valve in the way indicated in Article 67, Fig. 63.

Let  $r_1$ ,  $\phi_1$  be the eccentricity and angular advance of the expansion eccentric, and r,  $\phi$  the corresponding quantities for the main valve, as in the last article. Then the half stroke of the expansion valve is given by  $mr_1$ , where m is the ratio d/c. See Fig. 64. The expressions (4) and (5) of Article 76 become

$$C = mr_1 \cos \phi_1 + r \cos \phi = mE - F$$
.....(1),  
 $D = mr_1 \sin \phi_1 + r \sin \phi = mG - H$ ....(2).

Hence to find m so that cut off may take place at a given fraction of the stroke, calculate the corresponding value of the crank angle  $\theta$ , write L

for  $\xi$ , and find m from the equation

$$\pm L = (mE - F)\cos\theta - (mG - H)\sin\theta....(3);$$

the transformation of this equation into one giving the elements of the imaginary eccentric is carried out in the same way as for the Meyer gear, Art 76.

### CHAPTER VII

#### REVERSING GEARS LINK MOTIONS

Preliminary. If the crank shaft of a single evhider doubleacting engine is turned into one of the positions where the piston is at a dead point, the appropriate steam port will have a certain small breadth of opening which has already been defined as the lead. The motion of the piston from this dead point along its stroke, may correspond to a motion of the crank in either of two directions, namely, clockwise or counterclockwise. In which of these two directions the crank shaft will turn continuously when steam is admitted into the cylinder will depend upon the setting of the valve gear. It is easy to decide in which direction the steam will drive an engine by trying in which direction the crank shaft must be turned to increase the breadth of the opening for steam as the piston leaves the dead point. In other words, the direction of rotation of the crank shaft which causes the lead to increase, is that in which the engine will run continuously when steam is admitted to the cylinder. A more general way of discriminating between the two directions of rotation is to place the piston at a dead point and observe which way of turning increases the distance of the valve from its central position. The direction in which the steam will turn the erank shaft is that which produces an increase of the valve displacement from its central position when the piston is moving from its dead point

**Definition.** A valve gear whose setting can be readily altered so that it changes the distribution of steam by the valve in a way which reverses the motion of the crank shaft is called a **reversing gear**.

80. Hand reversing. Slow speed engines which run normally in one direction, but which occasionally have to be reversed for a few revolutions, are sometimes fitted with a valve gear which only determines the turning of the shaft in the normal direction. The valve gear is designed so that it can readily be disconnected from the valve

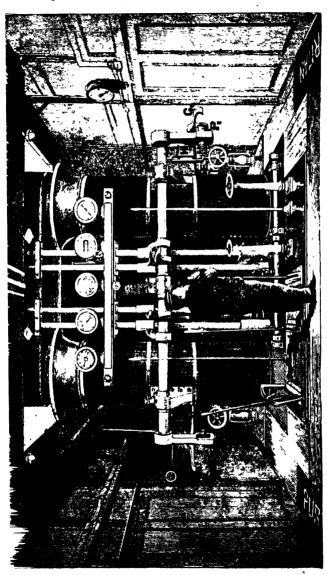


Fig. 70, Hand Reversing. Driving Platform of the S.S. "Puritan,"

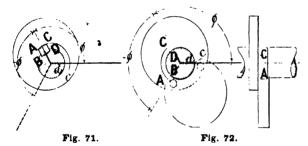
spindle, and arrangements are made whereby the valve spindle can be operated by hand. The engine-driver can then cause the engine to run in the reverse direction by giving a suitable motion to the valve. The speed must be slow enough to enable the engine-driver to follow the motion of the piston, either by watching the crosshead, or by watching an indicator placed near the driving platform showing the motion of the engine crank or the piston. Usually the valve is driven through a rocking lever, the valve spindle being connected to it at one end, and the end of the eccentric rod being hooked on to a driving stud at the other end. The end of the eccentric rod can be lifted off the stud and placed so that it slides backwards and forwards without moving the lever. The valve can then be operated by hand by means of the rocking lever. This is the principle of the method of reversing in general use on the large American river steamers which are fitted with beam engines. Fig. 70 shows the driving platform of the engines of the paddle steamer "Puritan," belonging to the Fall River line, running between New York and the Fall River. The engine is of the compound condensing type and can work at the rate of 7500 horse power. Each paddle wheel is 35 feet diameter and weighs 100 tons. The beam alone weighs 42 tons. The high pressure cylinder is 75 inches diameter and 9 feet stroke, the low pressure cylinder is 110 inches diameter and 14 feet stroke. A full description of the steamer and the engines will be found in Engineering, January 16, 1891. The illustration is reproduced here (by the courtesy of the editors of Engineering) in order to show that even large engines can be worked in the reverse direction by hand after lifting the eccentric rods out of gear with their respective rocking shafts. The valves themselves are actually lifted by a small supplementary engine whose action is controlled by hand levers which are seen at the centre of the driving platform Fig. 70

The gab ends of the eccentric rods  $G_1$  and  $G_2$  are both shown lifted out of gear with their respective pins  $P_1$ ,  $P_2$ . The mechanism by means of which the right rod is lifted off its pin and supported when out of gear is seen at H. The dial on the wall to the right shows the position of the crank and indicates to the engineer the proper time to operate the valves.

81. The loose eccentric sheave. A loose eccentric sheave is employed when an engine is required to run continuously in either direction and is to be reversed by hand.

The arrangement depends upon the fact that the crank shaft

drives the eccentric sheave so that the driving pressure, exerted by the shaft on the sheave, is transmitted through one face of the key for one direction of rotation. Thus, Fig. 71, so long as the shaft is turning in the direction indicated by the arrow, it drives the eccentric sheave through the face AB of the key. Suppose the part behind the face CDof the key to be cut away as shown, then, if the crank shaft is turned in the opposite direction, the sheave will not move until the face CD of the key comes into contact with the end ed of the curved slot, and if this length is so proportioned that in the new position of the sheave the angle between it and the crank is equal to the angular advance required for the reverse direction of running, the sheave will give a motion to the valve such that the engine will run continuously in the reverse direction To get the crank shaft to make this small reverse angular movement whilst the sheave is at rest the eccentric rod must be disconnected from the valve spindle and the engine reversed by hand Immediately CD is in driving contact with the sheave, the eccentric rod may be dropped into connection with the valve spindle again, and the engine will continue to run in the reverse direction. Fig. 71 merely shows the principle on which the loose eccentric is



THE LOOSE EC EXIMC SHEAVE

arranged. In the practical application of a loose sheave it is always desirable to add a balance weight so that the sheave will not tend to turn on the shaft by its own weight. It used to be the practice to form the driven faces on this balance weight as indicated in Fig. 72, where the weight is shown bolted to the sheave. ACDB is a circumferential key secured to the shaft, and it drives the sheave by contact with either of the faces AB and CD.

This method of reversing was used extensively on the oscillating engines of paddle boats. Several fine models of Marine Engines in the South Kensington Museum are fitted with this gear. A loose

eccentric was used on certain compound locomotives designed by Mr F. W Webb tor the express traffic of the London and North-Western Railway Company. One of these engines, "Jeanne Deans is described and illustrated in Engineering, July 25, 1890. The two high pressure cylinders of this engine drive one axle, and the valve distributing the steam to each cylinder is moved by a reversing gener of a type to be explained in a later chapter. The single low pressure cylinder drives a second axle, on which is placed a loose eccentric sheave for the purpose of operating the slide valve. The reversal of the engine is effected by the high pressure cylinders and valve gear, and a fraction of a revolution of the low pressure axle in the reverse direction brings it into contact with the sheave in the angular position necessary for continuous running in the reverse direction.

82. Reversing gears with two eccentric sheaves. An obvious way of constructing a reversing gear is to provide two eccentric sheaves, one keyed to the crank shaft at the angular advance proper for positive rotation, the other keyed at the angle for negative rotation, and to arrange the two corresponding eccentric rods so that the end of either can be coupled into driving connection with the v. Ive spindle, whilst the end of the other, free from any connection with the valve spindle, moves ally to and fro.

Fig 73, a diagrammatic sketch made from the model of the locomotive "Austria" in the South Kensington Museum, illustrates a form of gear used by Norris of Philadelphia in 1837.

There are two fixed eccentric sheaves, indicated by their centre lines only, keyed respectively in the positions required for positive and negative rotation. It may be noticed incidentally that the introduction of the rocking lever T, between the end of the eccentric rod and the valve spindle, requires that the eccentrics be keyed exactly 180 degrees with the positions for outside steam admission with direct connection. (See Fig. 85, below) The end of each eccentric rod is held up by a pair of suspension links, one of each pair, S and s, being seen in the figure. These links are free to swing about the centre U, thus guiding the points E, e, of the respective eccentric rods in circular paths, whose centres are at U. For long suspension links and small angular motions the paths of the points E and e are not greatly different from straight lines. The centre,  $U_i$  is at the end of an arm, forged solid with the shaft B, usually called the "weigh-bar shaft," which can be turned into either of two positions by the lever R, about the axis W, which axis is determined by bearings fixed to the engine frame. Thus, the axis U can be fixed in either of two positions at the will of the engine-

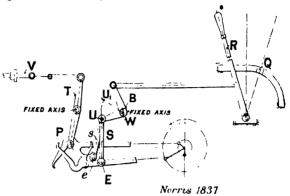


Fig. 73.

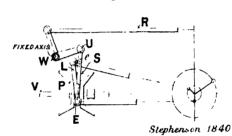
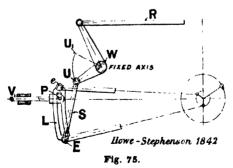


Fig. 74.



THE GENESIS OF THE LINK MOTION.

driver by means of the reversing lever R. The end of each eccentric rod is formed into a V, or gab, the bottom of which is shaped into a recess fitting the pin P round half of its circumference. The pin P is carried by one end of the rocking lever T, the other end being connected to the valve spindle V. In the figure the pin P is receiving motion from the upper eccentric rod. To reverse the motion, the lever R is disengaged from the slot holding it and pulled back into the slot Q, turning the weigh-bar shaft about the fixed centre W, so that the centre of suspension is brought to  $U_1$ , thereby lifting the upper eccentric off the pin P and bringing the lower eccentric in connection with it

Many forms of this kind of gear were in use about this time with many variations in the mechanical details by means of which the connection of the eccentric rods to the valve spindle was controlled.

About the year 1840 Stephenson introduced the form shown in Fig 74. Here the gabs are placed directly on the valve spindle, the ends of the eccentric rods are connected by the straight link L, and one pair of suspending links, one of which, S is seen in the figure, serve to hold up and to guide the motion of both ends of the eccentric rods. In the figure, W is the centre of the weigh-bar shalt, U, one of the two possible centres of suspension, P, the block which receives the motion from whichever eccentric rod is in gear with it, and R the rod leading to the reversing lever on the footplate.

83. The link motion. A slight change in the mechanical arrangement of the gear shown in Fig 75, made in 1842, resulted in a reversing gear of extraordinary fitness for locomotive working. The change, as will be seen from the figure, is merely the direct connection of the valve spindle with the link L which holds the ends of the eccentric rods apart, the link being now curved and slotted to permit one or other of the ends of the eccentric rods to be brought as nearly opposite the pin P as possible, by the turning of the weigh-bar shaft about its fixed axis W. This change is attributed to Howe, at the time a workman in Messrs Stephenson's employ at their locomotive works at Newcastle.. Both figures, slightly altered to show the suspension links S distinctly, are taken from Locomotive Engineering by Zerah Colburn. For some remarks relating to the invention of this motion, see Link Motions and Expansion Gears by N. P Burg, London, 1870. The arrangement was adopted by Stephenson and the gear has since gone by the name of the Stephenson Link Motion

This motion, in addition to being a reversing gear, is also a variable expansion gear, for if the point of suspension of the link is fixed at

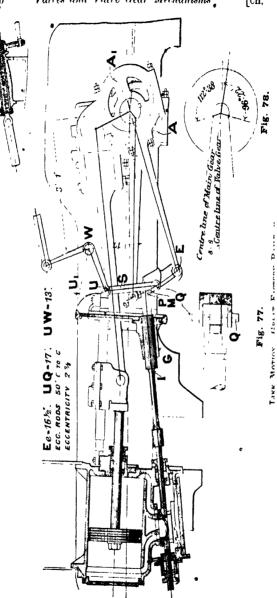
some intermediate point between U and  $U_1$ , as  $U_2$ , say, the point P will receive a motion compounded of the motion of both the ends of the eccentric rods: and this compound motion is very much the same as the point would receive if it had been connected directly to an imaginary eccentric rod, driven by an imaginary eccentric sheave having a greater angular advance than either of the actual eccentric sheaves and a smaller radius. Increases and a smaller radius increases a happens that the displacement curve of the point P in this intermediate position is such that with the same lap on the slide valve which is required for a proper distribution of steam in either of the extreme positions, a proper distribution of steam can be obtained for driving the engine with an earlier cut off, the point of cut off depending upon the position of the point of suspension U

Thus the link motion was a happy solution of the problem of arranging a convenient reversing gear, and a most happy, though fortuitous, solution of the greater problem of designing a simple gear by means of which expansive working was possible. There seems to be some doubt whether this enormously valuable property of the gear was discovered at once, or whether it dawned upon the users and constructors of the gear gradually. It was however thoroughly understood in course of time and engineers found themselves in possession of one of the most beautiful inchanisms ever invented.

Once its properties were known it was carefully examined as an expansive gear and other forms proposed varying to a greater or less degree from the original type, the most notable of these being the Gooch and the Allan types. There were several other forms brought out on the Continent, but most of them were more complex. The objects of these different inventions will be described more particularly below. It is remarkable that, at the present day, the majority of locomotives and marine engines are fitted with the link motion, almost in its primitive form, though on the Continent the Walschaert gear, described below, is displacing the link motion for locomotive work and is being gradually introduced on English railways.

The link motion shown in Figure 76 represents a standard motion designed by Mr Holden for the Great Eastern Railway Company. The only practical difference between this gear and the gear of Fig 75, is, that the suspending links S (there are two links one hiding the other) are jointed with the link at its centre Q. The point of suspension can be placed in any intermediate position between the extreme positions U and  $U_1$  by means of the reversing screw R. The valve spindle is connected to the link by the intermediate valve rod I, sliding in guides G, having ample bearing surface. The end of the valve rod is forked, and the pin P passes through the fork, and a guiding block M, called the



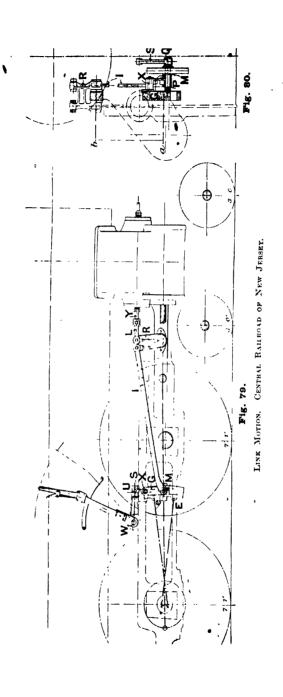


motion block, which shdes in the slot of the link. The link is shown in a position which determines positive rotation of the crank shaft, the motion given to the point e of the link by the eccentric sheave A predominating over the motion given to the point E by the sheave  $A_1$ .

The weight of the gear suspended from the point U is usually balanced by a choese weight carried on an arm forged solid with the weigh-bar shaft. In this gear however, the weight is balanced by the effort of a spring coiled on the weigh-bar shaft.

It will be observed that when the link is moved from one extreme position to the other by the turning of the weigh-bar shaft, the axis P of the motion block noist pass the axis Q at which the link is jointed with the suspending rods S. The way the link is constructed to allow this to take place, and at the same time to cusine that the centre line of the spindle I is central with the link, is shown in Fig. 77, which is a cross section of the link through the axis Q. The two side pieces carrying the pins for the jointing of the suspension links are usually rivetted to the link itself. By this construction the link and its suspension is made symmetrical with regard to a vertical plane which contains the axis of the spindle I.

An American design for a becomotive link motion, for the paticulars of which I am indebted to Mr McIntosh, Superintendent of Motive Power, Central Railroad of New Jersey is shown in Figs 79 and 80. In the general elevation the chain dotted frame is in front of the link gear full lines only being employed at the part near the cylinder which supports the rocking level. The end view is taken looking in the direction from the chimney towards the trailing end. The gear belongs to an engine of the Central Railroad of New Jersev and the engine is one of a number manufactured for that Company by the American Locomotive Company, Dunkirk, N.Y., who have kindly supplied the drawings. The engine is driven from a cab which is placed astride of the boiler, so that the reversing lever is attached directly to the weigh-bor shaft whose axis is W. The link is suspended from the centre U, by a single suspension rod S, which is seen better in the end elevation, and it is jointed to the centre of the link. The eccentric rods are jointed to the link at centres which are slightly displaced towards the driving axle, a construction which allows either rod to be brought in line with the centre of the motion block M, in the extreme positions. Steam is taken on the inside of the valve, so that the eccentric sheaves have to be placed as shown with regard to the main crank. The motion block, and with it the end of the intermediate rod I, is suspended from a fixed axis X, by the short link G, the pin which forms the common joint being clearly



seen in the end elevation. The axis of the motion block P is therefore constrained to move in the arc of a circle whose centre is at X. The other end of the rod I is jointed to a rocking lever R. This rocker is a heavy casting of substantial design, the two arms being well ribbed together. Its end elevation is shown in Fig. 80, displaced upwards through a distance ab in order to show the parts in end elevation clearly. It is placed astude the bar frame, the fixed pins on which it rocks being bolted to the frame. The second arm is connected by a short pair of links L, to the valve spindle Y. The links G, I, and one arm of the rocker, really form a four bar chain, of which the engine frame is the fixed bar. The introduction of the rocker enables the cut off to be equalised at a given fraction of the stroke in a way similar to that explained in Article 60. The New Jersey engines of the Chautauqua class to which this gear belongs, are a powerful type. The grate area is 82 square feet, and the total heating surface is 2967 square feet of which 174 square feet are provided by the fire box. The boiler is of the wagon top kind, working at a pressure of 210 lbs per square inch, and the barrel is telescopic, the diameter at the smoke box end being 6'8". The centre line of the boiler is 9'81" above rail level, and the total length of the engine over all is 39'84 %. These engines are used to work the service of fist expresses between New York and Philadelphia

Fig. 81 shows a general arrangement of a link motion fitted to a matine engine. It represents the gear for the intermediate cylinder of the port engine, looking aft, belonging to a cruiser of 22,000 horse power, built for the British Government by Messrs Humphry and Tennant The link Ee consists of a solid bar passing through the centre of a substantial motion block M, being jointed with it by means of the pin N, which is slotted to allow the link bar to pass through it The vertical motion of M is constrained by a single-guide bar securely held by the bracket G. The motion block in this case is formed with a cross-piece at the top so that it can be connected to two valves. This method of construction is peculiar to Messis Humphry and Tennant, the more usual way adopted by marine engine builders being to make the link up of two solid bars with distance pieces at the ends, the motion block being placed between them. The ends of the eccentric rods are forked to carry the respective ends of the link. Returning to Fig. 81, the link is suspended from the end s by the suspension link, or drag link as marine engineers sometimes call it, eU. The weigh-bar shaft, of which the cross section is seen at W, runs along the whole length of the frame and is common to the four sets of link motions belonging to the engine. In order to allow the point of suspension of each of the four link motions to be adjusted independently, the joint U

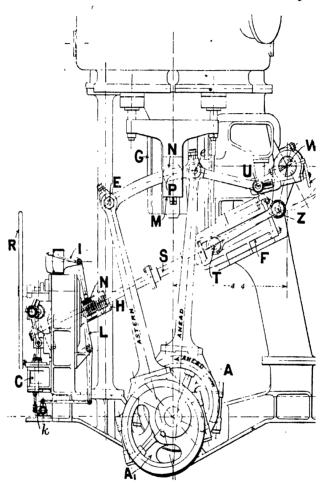


Fig. 81. Link Motion Marine Engine.

is carried in a slot formed in the end of the arm WU, the arm of course being keyed to the weigh shaft. The position of U in the slot is controlled by the hand wheel Y.

The weigh shaft is operated through the lever WZ by means of a small steam engine shown to the left. The rotation of the crank shaft of this engine is transferred through a worm and worm-wheel to the shaft S, the right-hand end of which passes through, and is supported by, journals in the frame F fixed to the engine standard. The part of the shaft S which is between the journals of the frame F is screwed, and engages with a nut T to which the frame F acts as a guide. The rotation of S therefore moves the nut, and by means of the connecting link TZ, turns the weigh-bar shaft. A wheel R is grared with the shaft S, so that the weigh-bar shaft may be operated by hand if necessary. The wheel R also acts as a flywheel to the small steam engine.

The reversing engine, which is itself reversible, is of the kind shown diagrammatically in Fig. 149 below, the principle of which is described in Article 130. After reading that article it will be understood that in addition to the slide valves used for the distribution of steam to the cylinders, a valve is required to interchange the steam with the exhaust passages when the small engine is to be reversed. This valve is indicated at C, Fig. 81, and is made of the piston type. It will be observed that the valve spindle from C projects below the cylinder, and is connected, through a bell crank lever k, with a lever L, the upper end of which is connected to a rod H lying parallel with the screw cut on the shaft S. A mit N on the shaft moves slowly in its guides as the shaft is turned, and in the extreme position at either end of its travel strikes a stop fixed to the rod, the distance apart of the two stops being so adjusted that when the large nut T has reached the end of its travel in either direction, the rod is struck through a small distance, sufficiently great however to move the valve ('over, so that the steam and exhaust passages are interchanged

In this way the reversing engine is automatically reversible. Hence when steam is turned into it, the effect is, that the nut T moves backwards and forwards in the guides F, thereby swinging the link continuously from the full ahead to the full astern position and back again, thus allowing steam to pass continuously through the main engines without driving them continuously in the same direction. The crank shaft merely makes oscillations, the engine is ready however to be started away at full speed ahead immediately the order is given, because to do this it is only necessary to stop the reversing engine when the link is in the proper position. An index I attached to the nut N shows the position of the link, and may of course be graduated • to give the cut off in the cylinder.

84. The general angular positions of the eccentric sheaves. The introduction of a rocking shaft reverses, or does not reverse, the

phase of the motion of the valve with regard to the piston, according as the arms of the rocker are on the opposite, of on the same, side as the axis of the shaft. Again, the phase may be reversed by taking steam on the inside of the valve. The following diagrams show the general arrangement of the gear in various cases. In these diagrams the observer is supposed to stand facing the eigence with the cylinder on his left, and the crank shaft on his right, and the crank is on the 0 degree dead point, that is, the piston is on the dead point where it is just going to begin the instroke.

Fig. 82 is the normal setting for English locomotives where steam is taken on the outside of the valve and the centre of the motion block is jointed directly to a continuation of the valve spindle.

Fig. 83 is the setting when inside admission is used, a method sometimes adopted with piston valves, because then the high pressure steam is kept away from the glands of the steam chest. Here the forward eccentric sheave is set with a lag  $\lambda_s$  and the backward with a lag  $\lambda_s$ .

If a rocking shaft is used in the gear, as in Fig. 79, which does not
reverse the motion, the setting of the eccentries is unaltered. If, however, the arms are on opposite sides of the axis, the settings corresponding respectively to inside and outside admission are shown in Figs. 84
and 85.

In all these settings the upper half of the link is used for positive rotation (forward running), and this necessitates the crossing of the rods in the two cases where the eccentries are set with lag

85 Examination of the distribution of steam effected by a link motion. To examine the distribution of steam effected by a link motion, displacement curves of the valve must first be obtained for different positions of the point of suspension, U, either by drawing or by means of a model of the gear. Each position of the point of suspension is determined by the angular position in which the weighbar shaft is locked by the reversing lever, reversing wheel, or reversing engine. The point P, Fig. 76, is rigidly connected to the valve, so that a displacement curve for P is the same as a displacement curve for the centre of the valve. Having obtained a set of displacement curves, the common vertical axis of the system may be fixed so that the respective leads for the two cycles are equal for a particular curve. Then add the lap lines and the piston displacement curve, and the valve diagram is complete.

86. Definition of u. A convenient way to distinguish between a set of displacement curves is to mark them with the numerical value of

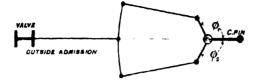


Fig. 82.

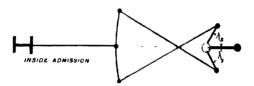


Fig. 83.

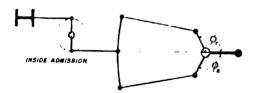


Fig. 84

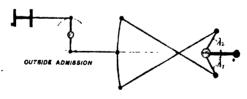


Fig. 85.

LINK MOTIONS AND LAR POSITIONS OF THE EXERTRIC SHEAVING IN VARIOUS ARRANGEMENTS.

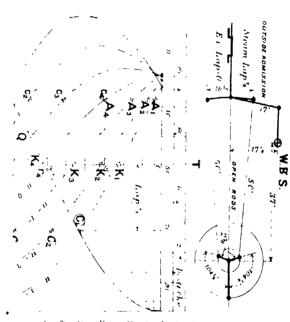
the quantity which will always be denoted by u. This quantity is the distance at which P, the centre of the motion block, stands from Q, the centre of the link when the crank is at 0 degrees, that is to say, when the piston is on the dead point at the beginning of the instroke cycle Moreover, since the block may stand above u below the centre of the link, let u denote a distance measured above the centre u0, and u1 a distance measured below the centre u2. When the motion block is at the centre of the link, u2 coincides with u3 and u4 has the value zero. In these circumstances the link motion is said to be in "mid-gear."

87. Valve displacement curves of the Great Eastern Railway link motion illustrated in Fig. 76. In this gear it will be noticed that the line of stroke of the piston is inclined to the line of stroke of the valve. As explained in Article 61, to find the angular difference between the crank and eccentric sheaves to be used in drawing the diagram, the two centre lines are to be brought into coincidence. In this example, Fig. 78, the angle between the centre lines is approximately eight degrees. When the centre lines are brought into coincidence the actual angular advance of the positive eccentric sheave (forward), namely 112½ degrees, will be diminished to 104½ degrees, and the actual angular advance of the negative sheave (backward) will be increased to 104½ degrees. Thus, in working out the distribution effected by this gear, equal positive and negative angular advances are to be used.

Displacement curves of the point P are shown in Fig. 86 for the following values of  $u_i$ 

$$4\frac{1}{2}$$
 3"  $1\frac{1}{4}$ " 0  $-1\frac{1}{4}$ "  $-3$ "  $-4\frac{1}{4}$ ".

The centre line is placed to bisect the horizontal distance between the points where the 4½" displacement curve cuts the horizontals through 0 and 180 degrees. The steam laps are each equal to ½ inch, so that the lap lines are drawn ½ inch respectively to the right and left of the central line. The exhaust lap is zero for both cycles, hence the intersections of the central line with the displacement curves determine the different release and compression points. Observe, that the displacements of the valve are now measured from a centre line which is common to the whole family of curves, but which does not correspond with the centre of oscillation of any one of them. If, therefore, the laps of the valve were measured according to the instructions of Article 47, namely, with reference to the centre of oscillation, they would be unequal for any one displacement curve; and this inequality would be different for different displacement curves. It is more con-



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venient to fix a common vertical axis in the way shown in the figure, and to consider that the valve has equal laps for the two cycles, than to refer the laps to a line drawn through the centre of oscillation belonging to each displacement curve.

The councetion rod is 5.85 times the length of the crisik, and the corresponding piston displacement curve is shown on the diagram

A careful examination of this valve diagram will place the student in possession of the chief characteristics of the distribution of steam effected by the link motion

First, fix the attention on the displacement curve marked  $n=4\frac{1}{2}^{n}$ . In general shape it is like the curves already considered in connection with the simple eccentric gen. Running the eye down it starting from the zero position of the crink, it will be observed that the lead is 0.17 inch, and that cut off release, compression and admission are respectively determined for the instrolle cycle by the points

$$c_1, r_1, k_1, a_1$$

Referring these points to the piston curve and from thence to the percentage scale, it will be found that the distribution of steam corresponding to the position of the point of suspension  $\ell$ , which makes  $u=4\frac{1}{2}\ell$ , is

Cut off, 75 per cent Release, 91 per cent Compression, 92 per cent. Admission, 99 per cent Maximum opening for steam, 142" Maximum opening for exhaust, 182"

These figures are tabulated in the top line of Table 7. Next look at the curve marked n=3". The lead has increased slightly, and the events of the stroke are determined by the points

$$c_1$$
,  $r_2$ ,  $k_2$ ,  $a_3$ ,

the percentages corresponding to which are shown in the second line of the table.  $\bullet$ 

When  $u = 1\frac{1}{4}$ " the lead has again increased, and now the points

fix the distribution

Examine next the curve marked  $u = -4\frac{1}{2}$ ". Starting from the top of the diagram and running the eye down, it will be seen that the opening for steam on the dead point 0 degrees is equal to the lead

when  $u=\pm 44\%$ , but that as the crank angle increases positively, the displacement curve almost immediately crosses the lap line, showing a cut off at  $A_1$ . From this point no steam can get into the cylinder until the curve reaches  $C_1$ , but then the pressure is acting to oppose the motion of the piston. It is evident, therefore, that the distribution is such, that the engine cannot be driven by the steam in the positive direction. But now start from the 350 degrees crank position and run the eye upwards along the curve. The lead is 0.17 and the points

$$C_1$$
,  $R_1$ ,  $K_1$ ,  $A_1$ 

determine a distribution which is practically the same as that determined by the displacement curve  $u=\pm 4\frac{1}{4}$ , providing the crank angle be reckened from 360 backwards up to 0 degrees, that is providing the crank turns in the negative direction. Thus, when steam is admitted to the cylinder, the crank shaft will turn in the negative direction. Similar considerations apply to the curves  $u=\pm 3$  and  $u=\pm 1\frac{1}{4}$ ".

Consider the curve corresponding to u = 0. Starting from the zero position of the crank and running the eye downwards, it will be found that the lead has a maximum value, and that cut off takes place very early, namely at 13 per cent of the stroke. Release occurs at 52 per cent. and compression at 52 per cent of the return stroke. Again, starting from the crank angle 360 degrees and working upwards along the curve, it will be found that the distribution effected is to all intents and purposes the same as found from 0 as the starting point. That is to say, the distribution is such that it is equally able to drive the engine in the positive or the negative direction, if it can drive the engine at all. If the cut off at mid-go a is not excessively early, there may be enough positive work done during the stroke to overcome a light load, such as the engine friction For instance, a locomotive running light and in the forward direction may continue to run forward when the link motion is brought into mid-gear. If the engine be reversed it may continue to run backwards when the link motion is brought into mid-gear as before. Thus, for this one position of the gear, the engine may be rinning either forwards or backwards.

For the outstroke cycle start the consideration of the displacement curves marked with positive values of u from 180 degrees, and work downwards. For the displacement curves marked with negative values of u, start also from 180 degrees, but work upwards. All the points giving the distribution of the outstroke cycle are similarly lettered to those of the instroke cycle, but are distinguished by having a circle drawn round the letters.

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The results for both cycles and for the seven values of u stated, are collected together in Table 7. Each horizont I line of this table corresponds to one definite indicator diagram. For positive values of u the crank shaft will rotate in the positive direction, and for negative values in the negative direction.

The transference of all the points concerned, to the piston curve horizontally, and then to the percentage scales vertically, is somewhat tedious. The labour may be considerably reduced by the use of one of Zeiss' glass'scales for the percentage scale, guiding it over the diagram by the T-square For instance the cut-off point  $c_2$ , projected horizontally on the piston curve, gives the point Q. Placing a glass scale, which is divided into 100 parts, across the diagram, its centre corresponding with the centre line and its extremities with the vertical boundaries of the piston curve, the percentage position of Q can be read off with reference to either dead point at will.

The maximum openings of the ports for steam and exhaust can easily be read off the diagram. Comparing these, it will be seen that there is considerable variation between the maxima for a given curve. In other words, the centres of oscillation of the several curves do not fall upon the centre line of the diagram. This is one of the defects of the link motion, and nothing can be done to remedy it without changing the type of the gear altogether. It is not a serious error practically. The drawing of the centre line to give equal leads corresponds with that method of setting of the valve where the valve spindle is adjusted in length until this equality of lead is secured.

It will be observed that the displacement curves (shown in full lines) relating to forward running, intersect one another approximately at a point just below the horizontal through 0 degrees. If a horizontal is drawn through the point corresponding to 5 degrees on the vertical axis, it will pass through this common intersection of the curves. If therefore the zero of the vertical scale could be moved down 5 degrees, the leads for varying positive values of u, could be made more nearly equal. This may be accomplished by increasing the angular advance of the forward eccentric sheave 5 degrees, at the same time decreasing the angular advance of the backward sheave by an equal amount, so that the angle between the sheaves themselves remains unchanged. The leads at the 180° dead point would also be equalised by this change. Hence, by setting the eccentric sheaves with slightly different angular advances, the leads may be approximately equalised for varying positive values of u. The leads for back gear, however, suffer by the change, the original inequalities between them being increased for varying negative values of u. This method of setting the sheaves was pointed out by Zeuner in his Treatise on Value Gears, it is however rarely employed.

The chief characteristics of the link motion may now be summarised:

- (1) The lead of the valve is not constant for all positions of the suspending point U. It increases from full gear, where u has a minimum positive or negative value, to a maximum at midgear, where u=0. In the diagram it will be seen that the lead increases from 0.17" at full gear to 0.31" at mid-gear.
- (2) The cut off takes place earlier in the stroke as  $\boldsymbol{u}$  is decreased, being a minimum when u=0.
  - (3) Release takes place earlier in the stroke as u is decreased.
- (4) Compression takes place earlier in the return stroke as u is decreased
  - (5) Admission takes place earlier as u is decreased
- (6) The centre of oscillation of the valve changes as u changes. This is shown on the diagram by the unequal openings of the ports both for steam and exhaust.

It may be stated with reference to locomotive working that, in general, all the events of the stroke require to take place earlier as the piston speed is mereased. Bearing this in mind it would be difficult to devise a more appropriate mechanism than the link motion for a locomotive gear. All the exacting conditions of the service are, if not exactly fulfilled, very nearly complied with. It is remarkable that the characteristics of the link motion which make it so valuable were, if tradition be true, unknown alike to the inventor and to the engineers who first used it, and that its subtler properties were only discovered in the use of it as a reversing motion.

88. Percentage and port opening diagrams. Having obtained a sufficient number of displacement curves, it is an easy matter to construct diagrams from which the distribution of steam and the port openings may be found for any assigned value of u. Such diagrams are shown in Figs. 87 and 88 for the Great Eastern Railway link motion. In Fig. 87 the percentages given in Table 7 are plotted vertically over the corresponding values of u set out horizontally, and curves are drawn through the points so obtained. Hence for a given value of u, positive or negative, the corresponding distribution of steam is fixed by the points where a vertical line through the given value of u, cuts the curves. The port openings are plotted in a similar manner in Fig. 88.

TABLE 7.

# Link motion. Great Eastern Railway.

The letters on the disgrams have the following significance

Instruke code Positive rolation Coronal)

a commission, e = cut off, r = release, k = compression

Acquire rotation (Backing I)

A -admission, C -cut off, R, release, K=compression,  $Outstroke\ egete$ . The same as above only with rings round them

# INSTROKE CYCLE (Back port)

u	Cut off	Release	Compression	Admission	Lend in inches	M (ximum opening, steam	Maximum opening, exhaust
+ 41"	753	91	923	99.7	$0.17^{\prime\prime}$	1 12"	1 82"
$+3^{\prime\prime}$	60 5	817	850	99.0	$0.25^{\prime\prime}$	0.71"	$1.50^{\prime\prime}$
+ 11/2	37.1	73.2	70.5	96.5	0.297	0.41"	$1~26^{\prime\prime}$
0	134	52.5	48.5	86.5	0.31''	0.31''	1 19"
0	13.2	51	47.5	86.5	$0.31^{\prime\prime}$	031''	1 19"
- 11 ′	37.0	720	69.5	96.5	0.29	0417	$1.26^{\prime\prime}$
3"	59.5	840	850	99.0	$0.25^{\prime\prime}$	0.70 ′	1 47"
- 41	750	91.0	92.5	997	0.17''	1407	177"
		Ot	ISTROKE CY	ctr (Fr	nt port	)	
+ 41"	723	92.3	91.0	99.7	0.17"	0.95"	199''
+ 3"	57.1	850	847	98.8	$0.25^{\prime\prime}$	$0.63^{\prime\prime}$	1 58"
+ 1½"	33.1	70.5	73.2	96.2	0.29''	$0.39^{\prime\prime}$	1 28"
0	125	48.5	52.5	880	031''	0.31"	1 19"
6	120	47.5	510	87.5	0.31''	0,31"	1 19"
- 11/2"	29.5	69.5	720	95.5	0.29''	0.39"	1 28"
- 3'	54.9	850	810	983	$0.25^{\prime\prime}$	0.60''	1 57"
- 41"	740	92.5	91.0	997	0.17"	0.90"	1.97"

The release points  $r_1r_2r_3r_4$  become the compression points for the Outstroke Cycle. The compression points  $k_1k_2k_3k_4$  become the release points for the Outstroke Cycle. The release points  $R_1R_2R_3R_4$  become the compression points for the Outstroke Cycle.

The compression points  $K_1K_2K_3K_4$  become the release points for the Outstroke Cycle

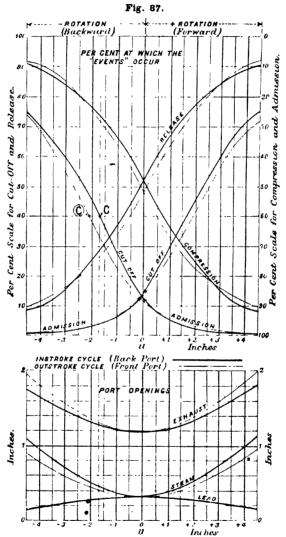


Fig. 88. Percentage and Port Opening Diagrams corresponding

The diagram may be used to find the value of u corresponding to a given cut off. For instance, suppose the value of u and the distribution of steam to be required when the cut off as 40 per cent, of the stroke, instroke cycle, in back gear. The point C fixes the place on the instroke cycle backward gear curve where the cut off is 40 per cent. A vertical through this point shows that u must be -1.7 inches, and that release, compression and admission occur respectively at 74,71, and  $96\frac{1}{2}$  per cent. Of the stroke Continuing the line through to the port opening diagram below, the corresponding lead, and port openings have the values 0.28%, 0.45% to steam, and 1.28% for exhaust. The quantities for the outstroke cycle can similarly be read off. If the 40 per cent had been given with reference to the outstroke cycle a vertical through 0 would have fixed the different percentages and port openings.

The displacement curves in Fig. 86 are sensibly influenced by small changes in the position of the weigh-bar shaft as will be understood from Article 99 below, where it is shown how to choose the position of the shaft to equalise the cut off at a given fraction of the stroke in both forward and backward gears. There will therefore be slight changes in the shape of the curves Figs. 87 and 88, corresponding with the changes in the shape of the displacement curves.

The curves, Figs. 87 and 88, also depend upon the setting of the valve gear. In these figures they correspond to the setting where the length of the valve spindle is adjusted to give equality of lead for u=41'', and this corresponds with the position of the common vertical axis TT, in Fig 86 A slight change in the length of the valve spindle would require a corresponding lateral change to be made in the position of the axis TT, relatively to the valve displacement curves, but the piston displacement curve and its attendant percentage scales would move with the axis. The leads, port openings, and the percentages of all the events given by the diagram would change slightly, and there would be consequent modifications of the shapes of the curves in Figs. 87 and 88. A point peculiar to link motions used with locomotives is, that on service the vertical distance between the centre of the weighbar shaft and the centre of the crank axle is always changing, because the weigh-bar shaft, and in fact the greater part of the valve gear, is carried by the spring supported frames of the engine, whilst the centre line of the crank axle is at an invariable distance from the rail level. When the engine is unloaded, as is the case when the valves are set in the erecting shop, it stands high on the springs, but when loaded for service it settles down on the springs. If therefore the valves are set in the erecting shop to give exact equality of lead at mid-stroke, or at full gear, the engine being unloaded, when the engue is loaded for service this equality would be destroyed, and the curves corresponding to those of Figs. 87 and 88 would be slightly modified. The changes are greater if the axis of the valve gear is inclined to the line of stroke. Also the expansion of the valve spindles when heated by the steam tends to decrease the lead at the front port and increase it at the back port. All these facts must be borne in mind when setting the valves and duly allowed for by so setting the valves in the unloaded and cold condition of the engine that in the average loaded and hot condition there is equality of lead at, say, full forward gear. One of the advantages of the link motion, including the modifications of it described below, is that the vertical movement of the spring supported part of the gear relatively to the crank axle, does not seriously interfere with the distribution of the steam or with the leads, and although curves like those of Figs. 87 and 88, which correspond to one setting of the gear, are modified in shape, yet the modification is slight.

It is to be understood then that the curves in Figs. 87 and 88 only represent conditions corresponding to the position of the weigh-bar shaft, and to the position of the axis TT, shown in Fig. 86.

89 Link motion with crossed rods. An alternative way of connecting the eccentric rods to the link is shown in the diagrammatic sketch at the top of Fig 89 forming what is called a link motion with crossed rods. In order to ascertain to which of the two types a particular link motion belongs, turn the crank into the position where both eccentric radii are pointing towards the link. If the rods are incressed in this position the motion belongs to the open rod type, if crossed, to the crossed rod type.

The peculiarities of the distribution of steam determined by a link notion of the crossed rod type may be studied from the displacement curves shown in Fig. 89, which were constructed from the Great Eastern Railway gear just considered after crossing the rods, everything also remaining the same.

Comparing the valve diagram with that for the same gear with open ods, Fig. 86, notice

- (1) The value of u is now negative for positive rotation and positive for negative rotation.
- (2) The lead decreases as u is decreased, being a minimum in mid-gear.
  - (3) The displacement at the dead points is reduced so much

that the lap must be reduced to 1 inch in order to get sufficient lead for the full gear curves, whilst for mid-gear, even with this reduced lap, the lead is nil.

- (4) The percentages at which the events of the stroke occur for corresponding values of u in the two valve diagrams are considerably altered.
  - (5) The travel of the valve is reduced

This comparison of the two diagrams will indicate that to get a workable motion giving a distribution of steam comparable with the open rod type, appropriate increases must be made both in the occentric radii and in the angular advances.

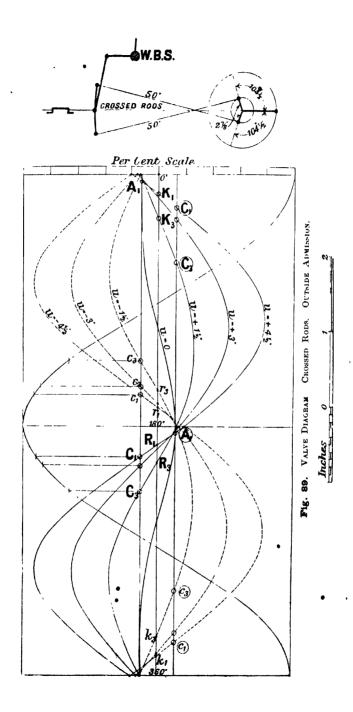
It should be understood that the valve diagram for the crossed rods, Fig. 89, does not represent an actual case. It is obtained from the Great Eastern Railway motion, which was designed for open rods, by crossing the rods without altering any of the other quantities except the lap, the object being to bring out the peculiarities of the types by contrasting the distributions of steam they respectively determine, when the only difference between them is that the one has open rods, the other crossed rods. Crossed rod motions may be designed to give equally good distributions of steam for various values of n as open rod motions.

The distinguishing characteristic of the crossed rod type is that the lead decreases as the motion is brought towards mid gear, being a minimum at mid-gear

90 Valve displacement curves of the Great Eastern Railway link motion, arranged for inside steam admission. A reference to Article 42 will recall the statement that it a simple valve gear is designed for outside steam admission having an angular advance  $\phi$ , then it may be set for inside steam admission by merely altering the angular advance to an angular lag  $\lambda$  such that

$$\lambda = (180 - \phi)$$
 degrees

This principle remains true for a Stephenson link motion. Consequently if the angular advance of 104½ degrees is changed to an angular lag of 75½ degrees the displacement curves of the valve will be such that steam requires to be admitted on the inside edge and released at the outside edge of the valve, the steam pipe and exhaust pipe being of course interchanged. This arrangement may be, and is





sometimes, adopted with piston valves, because the high-pressure steam inside the valve has no tendency to blow the valve off the face the ports, as would be the case with the ordinary slide valve.

A set of curves corresponding to angular lags of 75½ degrees for both the forward and the backward eccentric sheave, is shown in Fig. 90, and with the exception of the change in the angular advance, the other dimensions of the gear remain the same as those shown on the skeleton diagram, above the displacement curves for outside steam admission, Fig. 86.

Looking at the skeleton drawing above Fig 90, it will be noticed at once that the change from angular advance to angular lag results in the crossing of the eccentric rods, but an examination of the corresponding displacement curves will show that the lead increases as the link is moved from full gear towards the mid position. The reason is, that although the crossing of the rods results in a slight increase of the distance of the valve from its central position as the link is brought towards mid-gear, as in the case of the gear with angular advance and crossed rods, yet this increased distance corresponds to an increased lead because the lap is set out on the inside of the valve. The eccentric rods may of course be connected to the link so that they are "open," in which case the upper part of the link determines negative rotation, and the lead decreases from a maximum at full gear to a minimum at mid-gear.

Returning to the valve displacement diagram, Fig 90, the full curves are those for positive rotation, or forward running, and the dotted curves for negative rotation or backward running. The events of the stroke for the instroke cycle, when  $u=\pm 4\frac{1}{2}$  inches, are indicated by the letters

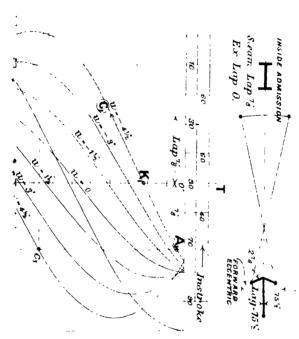
$$c_1, r_1, k_1, a_1,$$

and, remembering that  $r_i$  is the same point as  $(c_i)$ , and  $k_i$  as  $(c_i)$ , the corresponding events for the outstroke cycle, by the letters

①, 
$$k_1$$
,  $r_1$ , ②.

Referring these points to the piston curve, and from thence to the appropriate percentage scale, it will be found that the instroke cycle is specified by

Admission 99.7 per cent.
Cut off 69½ " "
Release 90 " "
Compression 93 " "



Inside Admissios

and the outstroke cycle by

Admission 997 per cent. Cut off 78 Release Compression 90

Comparing these figures with those for inside admission, Table 7, it will be seen that there is substantial agreement between them. The differences are due to the several obliquities of the rods influencing the results in different ways. No difficulty will be found in constructing a table corresponding to Table 7 from the diagram. The points determining the instroke cycle for the value of  $u = -4\frac{1}{2}$  inches are shown by

$$C_1, R_1, K_1, A_1,$$

the points for the outstroke circle being ringed,

A set of displacement curves for angular lag and open rods would be generally similar in character to those of Fig. 90, but the full curves would be dotted and the dotted curves full

To draw the valve displacement curves of a Stephenson link motion. The only correct way to obtain the displacement curve corresponding to a given value of u, is to set out the link motion in a series of positions, 24 say, obtaining thereby a series of corresponding values of the valve displacement and the crank angle. Plot these values and draw a curve through the points so obtained. The method is most easily explained in the form of the following problem.

Problem. Given the dimensions of a link motion, the position of the point of suspension of the link, and the crank angle,  $\theta$ , find the position of the link.

- (1) Set out the crank at the given angle  $\theta$ , Fig. 91; measure from it the two given angular advances  $\phi_1$  and  $\phi_2$ , and fix the centres a and b of the ends of the eccentric radii
- (2) From a and b respectively as centres, and with a radius equal to the length of the eccentric rod, draw the arcs  $e_1e_2$ , and  $E_1E_2$ . Then the end centres of the link must be respectively on these two arcs. Set out W, the centre of the weigh-bar shaft, and the given . position of the point of suspension U.
- (3) From U as centre, with a radius equal to the length of the suspension link, draw the arc CiCi. Then the point of attachment of the link to the suspension link must lie on this outve.

Thus, the three centres of the link must be severally on these respective arcs.

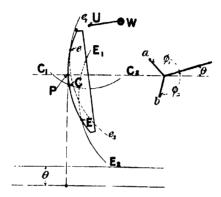


Fig. 91. THE DITERMINATION OF A LINK POSITION BY "FITTING" A TEMPLATE TO THREE ARCS.

- (4) Make a template, curved to the radius of the link (this radius is usually equal to the common length of the eccentric rods), and mark on its edge the three points e, E, and C, where the eccentric rods and the suspension rod are respectively attached. Then "fit" these centres to the three curves as shown in the figure, thus fixing the position of the centre line of the link. The point P, where the centre line of the link cuts the line of stroke of the valve, fixes the corresponding position of the valve. This point may be projected down to the horizontal line corresponding to the angle,  $\theta$ , of the crank, giving one point on the displacement curve corresponding to the given centre of suspension.
- (5) Repeat this process for the 24 positions of the crank and then sketch in the displacement curve
- If a value of u is given instead of a position of the centre U, place the crank at 0 degrees and find the position U must occupy so that the centre of the link stands at the given distance u from the line of stroke of the valve.

Fig. 92 shows the link in 12 positions, and the corresponding displacement curve for the Great Eastern Railway motion already considered, when u=0.

Repeat this construction for different values of u, or U, getting in

this way a complete family of valve displacement curves. Then add the vertical axis TT so that a stated condition of valve setting is satisfied, as for instance, that the leads shall be equal in full forward gear.

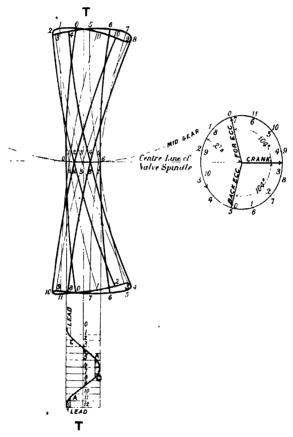


Fig. 92. Link Motion, illustrated in Fig. 76. Twelve Link Positions and the Valve Displacement Cury's for Mid-Gear

The eccentric circle is divided into 24 parts, starting first from the end of the forward eccentric, and then from the end of the backward eccentric, so that the points of the two series of divisions do not

necessarily coincide as they appear to do in the figure. The points 1 and 8, for instance, are not coincident, but are very nearly so in the case taken.

92. The suppression of the eccentric rods. The valve displacement is small compared with the size of the parts forming the gear. If the gear is set out to scale, therefore, the displacement to be measured off becomes too small to obtain a valve diagram from which the distribution can be inferred with much accuracy. Consequently, it may be taken as a cardinal rule that the gear should be set out full size so that the valve displacement curves may be obtained full size. The setting out of a link motion, full size in 24 positions for each value of u taken, is tedious and troublesome. The labour may be considerably lightened by using a template to draw the curves  $e_i$ ,  $e_i$ , and  $E_i$ ,  $E_2$ , in which the ends of the cecentric rods are located. Referring to Fig. 93,

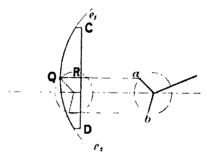


Fig. 93. Use of a Template 10 draw the Locus of the end of an Eccentric Rod for a given Crank Angle

it will be seen that if a template curved to the radius of the eccentric rod (the template already made for the centre line of the link will usually do for this purpose providing its edges are finished true with the curve in the way explained in Article 35 and shown in Fig 28) be placed as shown, it will fit the path  $e_1e_2$ , and its radial line QR will be parallel to the line of stroke of the valve or what is the same thing, its long edge CD will be at right angles to the line of stroke of the valve. If the eccentric circle is brought towards the link a distance equal to the length of the eccentric rod, the point a will coincide with the point Q. Hence, in setting out the construction, Fig 91, draw the centre of the crank shaft nearer the weigh-bar shaft by a distance equal to the common length of the eccentric rods, and set out the curved

paths  $e_1e_1$  and  $E_1E_2$  by means of the template, placing the point Q successively at a and b, and working with the edge CD against the edge of a T-square, in the way illustrated in Fig. 28.

If the gear is to be set out in 24 positions of the crank, there will be 24 points corresponding to a and 24 corresponding to b. It is advisable to first draw all the curves passing through the 24 positions of a in red, and the curves passing through the 24 positions of b in blue, clearly numbering each curve with the number of the corresponding crank position. Then the link template may be fitted in succession to the several pairs of paths and to the curve  $C_1C_2$  and its 24 positions drawn in. The several intersections of the link with the line of stroke of the valve then fix 24 positions of P from which the displacement curve can easily be drawn

It is also advisable to draw the set of link positions for a given value of u on a sheet of tracing paper, taking a fresh sheet for each value of u.

93 Slip. The axis of the motion block M, Fig 76, is guided in a straight line by the intermediate spindle I.

Any point in the centre line of the link is compelled to move in a path determined jointly by the oscillation of the link about its axis of suspension, due to the action of the eccentric rods, and to the swinging of the link as a whole about the fixed axis of suspension *U*.

Thus, when the axis of the motion block is brought to coincide with a definite point on the centre line of the link by the turning of the weigh-bar shaft into a definite position, the coincidence is only momentary, since each point moves away from the position of coincidence along a different path as the crank rotates. Hence there must be slight relative sliding between the block and the link in order that the axis and the point may each be able to describe their respective paths. This relative sliding is called "ship". It will be remembered that the quantity u was defined in Article 86 to be the distance of the axis of the motion block from the centre of the link when the crank was in the zero position. Owing to the "slip," u changes continuously in value during the rotation of the shaft, returning to its stated value each time the crank passes through its zero position.

The distance from a curve showing the actual path of a point on the centre line of the link corresponding to a stated value of u, measured along the link, to the corresponding point on the path of the centre of the motion block, is the slip for that particular link position. Various methods of suspending the link and constraining the motion of the intermediate spindle or link have been used from time to time with the object of reducing the slip to a minimum. Good general results for all positions of the gear are obtained by guiding the intermediate spindle in a straight line and by swinging the link from its centre as shown in Fig. 76. Better results for one or two particular positions of the gear can be obtained by varying the method of suspension and constraint.

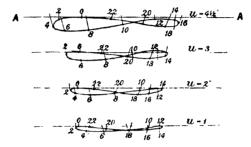




Fig. 94. Link Motion, Fig. 76. Paths of Points on the centre line of the Link specified by the given values of u.

A series of link point paths for the Great Eastern Railway motion already considered is shown in Fig 94, the values of u to which they correspond being written against them. Consider the curve for which  $u=4\frac{1}{4}$ ". The horizontal straight line AA represents the path of the axis of the motion block. At the point 0, the axis is  $4\frac{1}{4}$ " from the centre of the link, and the crank is in the zero position. The other figured points on the curve mark the successive positions occupied by the point on the centre line of the link,  $4\frac{1}{4}$ " from the centre, as the crank passes through the corresponding positions. The distance from any one of these points to the corresponding position of the axis of the motion block, measured along the link, is the instantaneous value of the slip.

The point path for mid-gear is an arc of the circle described by the centre of the end of the suspension link.

Fig 95 shows the point paths corresponding with the various values of u indicated, and at the same time the corresponding paths of the ends of the link, to a small scale.

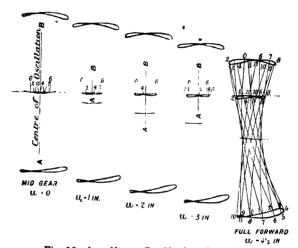


Fig. 95. Link Motion, Fig. 76. Link Point Paths

94 Apparatus for drawing valve displacement curves mechanically. The labour involved in drawing out a set of displacement curves is considerable. Many drawing offices are provided with a skeleton link motion, the different parts of which are adjustable, so that it may be arranged to represent any link motion in course of design. Parts representing the connecting rod and piston are combined with the valve gear, so that when the crank is placed at any angle the corresponding position of the piston and the valve may be observed, and thus all the peculiarities of the distribution effected by the gear may be studied. In some cases apparatus is added by means of which displacement curves may be drawn, usually in the form shown in Fig. 39.

Fig. 96 represents an apparatus of a simpler kind than that usually employed for the purpose of investigating the properties of a link motion, which was designed by the author for the Mechanical Engineering Department of the City and Guilds of London Technical College, Finsbury. The eccentricities, angular advances, lengths of the eccentric rods, position of the weigh-bar shaft, and the length of the arm of the

weigh-bar shaft which fixes the point of suspension, are all adjustable within reasonable limits. Simplicity is obtained by omitting the connecting rod and piston altogether, a graduated ring being used in order to fix the crank angle corresponding to a given valve position.

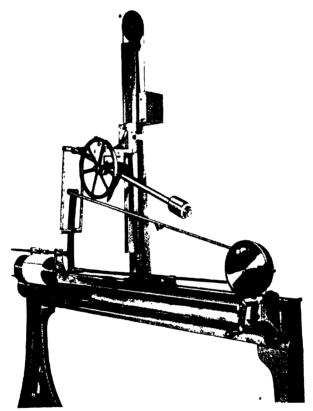


Fig. 96. Adjustable Apparatus for drawing the Valve Displacement Curves.

What is obtained from the apparatus is a family of rectangular displacement curves, like those for example shown in Fig. 86. These curves are drawn on the drum seen to the left of the figure. The piston displacement curve can be quickly and accurately drawn on the

diagram, and then the additions of a common vertical axis and the lap lines convert the drawing into a valve diagram from which all the circumstances of the distribution can be found.

95. Approximate valve displacement curves. Equivalent eccentric. For a given value of u, the agual movement of the valve is nearly the same as it would be if the valve spindle were connected directly to a long eccentric rod driven by a sheave on the crank shaft, having a certain eccentric radius  $\rho$  and being set at a certain angular advance  $\psi$ ,  $\rho$  and  $\psi$  being found by the following rule, due to Mi Macfarlane Grey

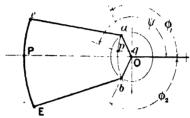


Fig. 97. Macfarlane Grey's construction for the Equivalent Eccentric

Let Oa, Ob represent the centre lines of the two sheaves driving the link motion,  $\phi_i$  and  $\phi_i$  being the angular advances. Draw an arc of a circle through the points a and b, using the radius, R, found from the formula

$$R = \frac{s \times l}{2\lambda},$$

where s is the distance between the points a and b, l is the common length of the eccentric rods, and k is the length of the link eE

Take a point p in the arc ab so that it divides the arc in the same proportion that the axis of the motion block divides the distance between the end centres of the link. That is,

$$ap pb = eP : PE.$$

Then Op is the radius, p, of the "equivalent" eccentric, and  $\psi$  is its angular advance. From these data the corresponding displacement curve may be set out. It is of course a cosine curve, having the value pq when the crank is in the zero position.

The dotted curve, Fig. 98, is the approximate displacement curve found by this method for the value of  $u_1 + \frac{4}{3}i'$ , the data being those of the Great Eastern Railway motion. It is shown full size.,

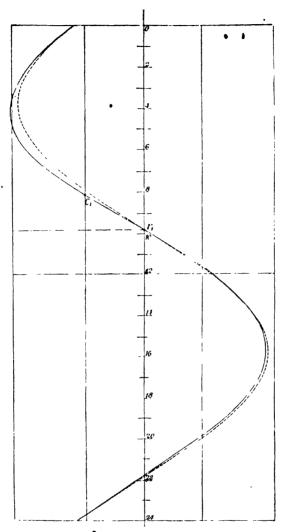


Fig. 98. Link Motion, Fig. 76. Comparison of the actual Displacement Curve, shown full, with the approximate Displacement Curve,
shown dotted, cohersponding with the "Equivalent Eccenteig"
found by Macparlane Grey's construction, for  $u=4\frac{1}{2}$ ".

The radius used for drawing the arc is in this case 8.47". The corresponding equivalent eccentric is defined by

$$\rho = 1.86$$
",  $\psi = 124\frac{1}{2}$  degrees.

The full line shows the actual displacement curve and is of course the same as the corresponding curve of Fig 86. A comparison of these curves shows that at the beginning of the strokes, when the crank angle is either 0 or 180 degrees there is almost coincidence. The greatest error occurs in the maximum openings. If the piston displacement curve be added it will be found that the cut off given by the dotted curve is within 3 per cent of the actual cut off, whilst the release, compression and admission events are within less than 1 per cent.

96 General theory of the link motion. Simplified form of gear and its equivalent eccentric. The theory of the link motion and its derivatives, the Gooch and Allan gears, will be more easily understood if the simpler form of gear shown in Fig. 99 is studied first. This form, though not practicable, yet retains the fundamental principles of the actual arrangement and allows these principles to be developed without mathematical complication.

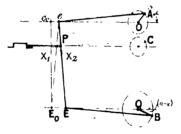


Fig. 99. SIMPLIFIED FORM OF LINK MOTION.

In the figure the link is represented by the straight line Ee, the eccentries by the cranks OA, QB, now rotating about separate axes, O and Q. The valve is connected to the link Ee at the point P, and it is presumed that the valve and rod can be moved bodily up or down so that P can be placed in any assigned position on Ee. Finally, the respective ends of the link are assumed to move along the straight parallel lines eO, EQ, and the eccentric rods are supposed to be so long that the respective motions of e and e are not sensibly different from the horizontal projections of the circular motions of e and e.

Each crank is supposed to revolve with equal angular velocity, from which assumption it follows that the angle between the cranks will remain constant. Let  $\kappa$  be this constant angle, and let  $\overset{\bullet}{\alpha}$  be the angle between the crank OA and the centre line. The movement of the point P is compounded of the movement of the points e and E. This movement may be analysed into its separate components by examining the motion P receives from the crank OA, assuming the crank QB to be at rest, and then the motion it receives from QB assuming OA to be at rest. The points  $E_n$  and  $e_n$  indicate the respective central positions of the ends of the eccentric rods.

First, assume the point E to be at rest in its central position  $E_0$ . Then when the eccentric OA, whose radius is  $r_i$ , is turned so that it makes the angle  $\alpha$  with the centre line, the distance,  $e_0e_i$  of the point e from its central position is

and since the link is turning about the point  $E_{\gamma}$  the corresponding distance of P from its central position is, assuming the angular motion of the link Ee to be small

$$\frac{PE}{Ee} \leq r_1 \cos \alpha = X_x \cdot \sin \alpha$$

Again, assume the point e to be fixed in its newly acquired position, e, whilst the eccentric QB, whose radius is r is turned so that it assumes its proper position relative to QA. Then the distance,  $E_aE_b$  of the point E from its central position is

and P moves from the position into which it was brought by the turning of OA by the amount

$$\frac{Pc}{Ee} \times r_1 \cos(\alpha - \kappa) = X_2, \text{say}$$

The total movement of P from its central position when the eccentries have the configuration shown in the figure is therefore.

$$X_1 + X_2 = \frac{PE}{Ee} r_1 \cos \alpha + \frac{Pe}{Ee} r_2 \cos (\alpha - \kappa)$$

From this expression the distance of P from its central position can be calculated for any value of the angle  $\alpha$  when the position of P is assigned in the link and  $r_1, r_2$ , and  $\kappa$ , the angle between the desenties, are known. The graphical interpretation of this expression readily exhibits the characteristics of the motion of P

From any point O, Fig. 100, draw OA, OB paralled to the respective eccentries in Fig. 99, and make  $OA = r_1$  and  $OB = r_2$ .

On 
$$OA$$
 take  $Oa = \text{to} \frac{PE}{Ee} \wedge r_1$  Then  $Ox_1$  is equal to  $X_1$ .

On OB take  $Ob = \text{to} \frac{P_{\theta}}{E_{\theta}} \times r_2$ . Then  $Or_2$  is equal to  $X_2$ .

Complete the parallelogram OaCb, and draw the diagonal OC. Then the distance dC = the distance  $Ox_3$ , and therefore  $Ox_3$  is equal to  $X_1 + X_2$ . But  $Ox_3$  is the projection of the line OC. Therefore the displacement of P from its central position is represented by the projection of the diagonal OC. Now since the cranks revolve so that the angle  $\kappa$ -remains constant in value, the angle AOB will remain constant whatever be the value of  $\alpha$ . Also, since during the revolution of the cranks the point P divides the link Ee in a constant ratio, the respective distances Oa, Ob, remain constant. Therefore the diagonal remains constant. Hence, as the eccentries revolve, the parallelogram OaCb revolves about O without changing its shape, or its angular position relatively to the lines OA and OB. Hence, since the projection of the diagonal always gives the distance of the point P from its central position, OC, it is the "equivalent eccentric" for the motion of the point P.

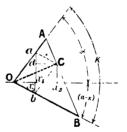


Fig. 100. EQUIVALENT ECCUPERIC CORRESPONDING WITH THE SIMPLIFIED GEAR, FIG. 99.

Again, the point a divides the line OA in the same proportion that the point P divides the link Ee. Also b divides the line BO in the same proportion that P divides the link Ee. Therefore

$$Aa:aC=Cb:bB$$

and the angles AaC and CbB are equal. Therefore the triangles AaC and CbB are similar. Since, therefore, aC is parallel to bB, AC is parallel to CB, but C being a common point, the lines AC and CB are in the same straight line, and this line is divided by the point C in the same ratio that a divides OA, that is in the same ratio that P divides the link Ea. Hence to find the equivalent eccentric for a given position of P:—

Set out the two eccentrics from a common point O, making the

constant angle  $\kappa$  with each other. Join the ends with a straight line and take the point C so that it divides AB in the same ratio that the assigned position of P divides the link Ec. Join OC Then OC is the equivalent eccentric for the motion of P.

The equivalent eccentrics shown dotted in Fig. 99. It will now be understood that, if the equivalent eccentric be made a real eccentric, and if the point P is connected to it by a real eccentric rod, and both the actual eccentrics and the link be taken away, P, being constrained to move in a straight line, will receive the same motion from the single eccentric that it actually received from the combined action of the two actual eccentries and the link

The link in Fig 99 will receive the same motion if it is driven by the equivalent eccentric and either of the actual eccentries, the other being suppressed

For instance, suppose OA to be connected to the link as before, the dotted equivalent eccentric gear to be made into a real gear and the eccentric QB and its gear to be suppressed altogether. Every point in the link will move in exactly the same way as it did under the joint action of the cianks OA and QB.

Examining the motion of the point E, it will be found that it may be considered due to an imaginary eccentric QB found by joining the points A and C and taking B so that

$$AC \cdot CB = eP \cdot PE$$

- 97. Approximate theory of the Stephenson link motion. Equivalent eccentric. Passing from the simplified form, Fig 99, to the actual form, Fig 101, the main differences in the conditions of motion of the link are.—
  - (1) The point P is compelled to move in an exact, or in some cases an approximately horizontal line so that when its position is changed relatively to the link, the link itself must be raised or lowered.
  - (2) The point e moves nearly in a line, passing through the central position e, and the centre of the axle, and E moves nearly in a line, passing through its central position E, and the centre of the axle.

Now, the motion of P can only be approximately represented by an equivalent eccentric, because although for any one configuration of the gear it is theoretically possible to construct the parallelogram OaCb of Fig. 100 and obtain the diagonal OC, the combined effect of the changes in the configuration of the gear, requires, that the parallelogram be

slightly changed in shape for each change of the value of  $\alpha$ , if the projection of its diagonal is to accurately represent the motion of P. Thus, during the rotation of the cranks the shape of the parallelogram is continuously varying about some one mean shape. The length of the equivalent eccentric is therefore continuously changing slightly both in length and in its angular position relatively to the real eccentrics for a given value of u.

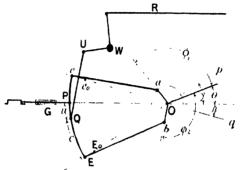


Fig. 101. CENTRE LINE DIAGRAM OF STEPHENSON LINE MOTION

Since the link motion is to be used as an expansion goar, a necessary condition which must be fulfilled is that the raising or lowering of the link shall not seriously interfere with the lead of the valve for all the possible positions of P in the link. The geometrical problem may be stated as follows —

Place the crank at the zero position and find the form of link so that it may be moved from one extreme position to the other, by the weigh-bar shaft without moving the point P.

This problem presents no difficulty theoretically, because it is easy to find the shape to which the link must be curved to fulfil the given condition, by drawing the several configurations of the gear corresponding to a series of positions of the point of suspension U, whilst the crank is kept at zero. Practically, however, the problem cannot be solved for the Stephenson link motion, because the theoretical shape of the link must necessarily be of varying curvature, whilst in practice the link must be made of constant curvature to enable a motion block having surface contact with the link to be used in the slot. Hence, the link must be curved to the arc of a circle. The usual practice is to make the radius of the link equal to the common length of the eccentric rods.

The motion of the point P may now be examined in order to fix the equivalent eccentric corresponding to a given position of P in the slot, that is corresponding to a given value of u.

It is assumed in the investigation that :-

- (1) The point e moves with simple harmonic motion in the straight path e<sub>0</sub>O , and E with simple harmonic motion in the straight path E<sub>0</sub>O
- (2) The inclinations, β and γ, of the two paths to the line of stroke of the valve are so small that, t being the common length of the eccentric rods, the sines of the angles are given respectively by

$$rac{Pe}{l}$$
 and  $rac{PE}{l}$  ,

that is by

$$\frac{c-u}{l}$$
 and  $\frac{c+u}{l}$ ,

where c represents half the length of the link, and that the cosines of the angles are so nearly unity that  $\cos \beta = \cos \gamma = 1$  may be written without introducing sensible error

(3) The value of u remains constant during rotation of the crank. The method followed is the same in principle as that used for the simplified form, only now the displacement of P is to be expressed in terms of the main crank angle, the eccentric cranks being fixed relatively to the main crank by their respective angular advances.

Let the gear have the configuration shown in Fig. 101. U is fixed, and u is assumed to have a constant value. The only variable angle is  $\theta$ .

The angles made by the eccentries Oa, Ob, with their respective lines of stroke, are aOq and bOp. Expressing these in terms of  $\theta$ , the angular advances, and the inclinations of the lines eO and EO,

$$qOa = (\theta + \phi_1 + \beta)$$
 measured counterclockwise from  $Oq$ ,  $pOb = 360 - (\gamma + \phi_2 - \theta)$  measured counterclockwise from  $Op$ .

The displacement of e from its central position in its line of stroke is,  $r_1$  being equal to Oa,

$$r_1 \cos (\theta + \phi_1 + \beta)$$

and since  $\cos \beta$  is taken equal to unity this also represents the displacement in the direction parallel to the direction of motion of P

The corresponding displacement of P relative to the point E is

$$\frac{c+a}{2c}\times r_1\cos(\theta+\phi_1+\beta).$$

D. V.

Again, the displacement of E from its central position is,  $r_2$  being equal to Ob.

$$r_2 \cos{(\gamma + \phi_2 - \theta)}$$
.

and since cosy is taken equal to unity, this also represents the displacement parallel to the direction of motion of P.

The corresponding displacement of P relative to the point e is

$$\frac{c-u}{2r} < r_z \cos{(\gamma + \phi_z - \theta)}$$

Hence the displacement x, of P, from its central position, given by the sum of these separate displacements, is

$$x = r_1 \frac{c + u}{2c} \cos \left[ \theta + (\phi_1 + \beta)_1 + r_2 \frac{c - u}{2c} \cos \left( \gamma + \phi_2 \right) - \theta \right] . \quad (1).$$

The displacement  $\tau$  can be calculated from this expression for any assigned value of u and  $\theta$ .

Expanding this expression, dropping the suffixes for r and  $\phi$ , since these quantities are usually made respectively equal, and writing the terms as factors of sin  $\theta$  and  $\cos \theta$ , (1) becomes

$$x = r \cos \theta \frac{(c+u)}{2c} \cos(\phi + \beta) + \frac{c+u}{2c} \cos(\gamma + \phi)$$

$$+ r \sin \theta \frac{(c+u)}{2c} \sin(\gamma + \phi) - \frac{c+u}{2c} \sin(\phi + \beta)$$
..... (2)

Expanding the cosines and sines in the brackets and writing

$$\{c+n,\ldots,c-n,\ldots\}$$

• 
$$\vec{x} = r \cos \theta \left[ \cos \phi - \sin \phi \left\{ \frac{c + u}{2c} \sin \beta + \frac{c - u}{2c} \sin \gamma \right\} \right]$$
  
+  $r \sin \theta \left[ \cos \phi \left( \frac{c - u}{2c} \sin \gamma - \frac{c + u}{2c} \sin \beta \right) \right] - \frac{u}{c} \sin \phi \right] \dots (3)$ 

Substituting the value  $\frac{c+u}{l}$  for  $\sin \beta$  and the value  $\frac{c+u}{l}$  for  $\sin \gamma$ 

this expression further reduces to

$$x = r\cos\theta \left\{\cos\phi - \frac{c^2 - u^2}{cl}\sin\phi\right\} - r\sin\theta \left\{\frac{u}{c}\sin\phi\right\} \dots (4)^{\bullet}.$$

This is the simplest form to which it can be reduced.

• If  $\cos{(90+\delta)}=-\sin{\delta}$ , and  $\sin{(90+\delta)}=\cos{\delta}$  are respectively introduced into this equation in place of  $\cos{\phi}$  and  $\sin{\phi}$ , it reduces to

$$-r\cos\theta\left[\sin\delta+\frac{c^2}{cl}\frac{u^2}{-\cos\delta}\right]-r\sin\theta\frac{iu}{lc}\cos\delta$$

Changing the signs all through, this is the form in which the equation was originally given by Zeuner.

The coefficients of  $\cos\theta$  and  $\sin\theta$  in expression (4) are constants for a particular value of u, neglecting the small variations of u discussed in Article 93. Hence the displacement of the valve from its central position may be written

$$a = A\cos\theta + B\sin\theta \dots (5),$$

where  $\boldsymbol{A}$  and  $\boldsymbol{B}$  are constants, having the values

$$A = r \left\{ \cos \phi - \frac{e^t - u^t}{ct} \sin \phi \right\} \quad \dots \quad (6),$$

$$B = i \left\{ \frac{u}{c} \sin \phi \right\} \dots \qquad (7)$$

No restriction was put upon the magnitude of the angle  $\phi$  in the preceding investigation, so that the expressions are true for all values of  $\phi$  between 0 and 560 degrees. The expressions apply therefore to all arrangements of the link motion, whether with crossed or open rods, providing always that the angle  $\phi$  is measured in the positive direction from the crank to the eccentric radius which is coupled to the top of the link. The following Table shows the quadrant in which the eccentric radius falls for several cases.

TABLE 8

	$\phi$ fulls between		
Open rods - Outside Steam Admission - Figs - 82 and 86	90 and 180 degrees		
Crossed rods Inside Admission Figs 83 and 90	270 " 360 "	•	
Open rods with a rocking shaft. Inside Admission. Fig. 84	90 ,, 180 ,,		
Admission Fig 85	270 , 360 ,	•	
Crossed rods Outside Admission Fig 89	180 " 270 "		

To illustrate the general character of the expressions (5), (6), (7), take the data corresponding to Fig. 86, and calculate the values of A and B for tull forward gear, where  $u=4\frac{1}{2}$ ", also l=50", c=8.25", and r=2.875"

In this case,  $\phi = 1044$  degrees, and therefore

$$\cos \phi = -0.25$$
, and  $\sin \phi = 0.968$ .

Substituting these values in equations (6) and (7) it will be found that

$$A = -1042,$$
  
 $B = 1517.$ 

Hence expression (5), for the displacement, becomes

$$x = -1.042 \cos \theta - 1.517 \sin \theta$$

Again, consider the same gear when arranged for Inside Steam Admission with crossed rods, as shown in Fig. 90

The angle  $\phi$  is now 2844 degrees, and therefore

$$\cos \phi = 0.25$$
, and  $\sin \phi = -0.968$ .

Therefore

$$A = 1042,$$
  
 $B = -1.517$ 

and these, introduced in expression (5), give for the displacement

$$x = 1.042 \cos \theta + 1.517 \sin \theta$$
.

Finally, suppose the gear arranged with crossed rods but Outside Steam Admission, as shown in Fig. 89.

The eccentric coupled to the top of the link is now the one which determines negative rotation. Nevertheless, the angle  $\phi$  is to be measured from the crank to it, giving  $\phi = 255\frac{1}{2}$  degrees. Therefore

$$\cos \phi = -0.25$$
,  $\sin \phi = -0.968$ ,

and

$$A = -0.395$$
,

$$B = -1.517$$

The expression for the displacement therefore becomes

$$x = -0.4 \cos \theta + 1.517 \sin \theta$$
.

Comparing equations (5) and (7) with equations (6) to (8), Article 72, it will be seen that the quantities A and B may be looked upon as the rectangular projections of a crank of radius  $\rho$  and angular advance  $\psi$ . That is

$$A = \rho \cos \Psi \dots \dots (8),$$

$$B = \rho \sin \psi$$
 .....(9),

$$\tan \psi = \frac{B}{A} \quad \dots \tag{10}$$

The quantities  $\rho$  and  $\psi$  define the "equivalent eccentric" for the particular value of u taken. The series of equivalent eccentrics corresponding to a series of values of u, may be used to examine the distribution of steam effected by a given link motion, the results being of course approximate only. The calculation of a series of values of  $\Delta$ 

and B for this purpose may be avoided by using an equivalent geometrical method.

When u=c, A, eq. (6) page 179, becomes equal to  $r\cos\phi$  and B, eq. (7), becomes equal to  $r\sin\phi$ . The equivalent eccentric then coincides with the actual eccentric which is coupled to the top of the link. When u=-c, the equivalent eccentric coincides with the actual eccentric which is coupled to the bottom of the link. When u=0,

$$A = r \left\{ \cos \phi - \frac{c}{t} \sin \phi \right\},$$

$$B = 0,$$

$$\tan \phi = \frac{B}{A} = 0.$$

Therefore  $\psi = 0$  or 180 degrees, according to the arrangement of the gear

Let the gear be arranged with open rods and for outside steam admission as illustrated in Figs. 82 and 86. Then  $\phi$  falls between 90 and 180 degrees, and A will be negative, consequently when u=0,  $\psi=180$  degrees. Starting from u=0 and calculating the values of  $\rho$  and  $\psi$  for a

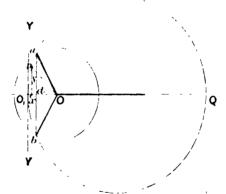


Fig. 102. Equivalent Eccentric. Open Robs. Outside Admission series of positive and negative values of u, it will be found that the radius of the equivalent eccentric increases in length from  $r \left\{ \cos \phi - \frac{c}{l} \sin \phi \right\}$  when u = 0, to r when  $u = \pm c$ : the angular advance decreasing meanwhile from 180 degrees when u = 0 to  $\pm \phi$  when  $u = \pm c$ .

It these equivalent eccentries be plotted their ends will be found to he on a parabolic curve instead of on a straight line as in the case of the simplified form of gear examined first. This is easily proved as follows:

Let the curve aph, Fig. 102, represent the locus of the end of the equivalent, eccentric. Take any point p on the curve. Take a vertical line through  $O_1$  for the axis of Y, and let the coordinates of the point be x and y. Then x is equal to the difference between the values of A when u = 0, and when u has the value  $u_i$  corresponding to the particular equivalent eventure Op. That is

$$x = \frac{m_1^2}{J} \sin \phi$$

The ordinate y is given by the value of B corresponding to the value  $u_1$ , that is

$$y = \frac{i u_1}{c} \sin \phi$$

Eliminating  $u_1$  from these two equations,

$$y = a + \frac{h}{a} \sin \phi - a \times a \text{ constant.}$$

Therefore the curve is a parabola, whose vertex is at  $O_1$ 

The parabola through the point  $O_1$  and the ends a and b of the eccentric radii would not differ sensibly from the arc of a circle in any practical case. The radius of this circle may be found by means of the Theorem, that the products of the segments of any two chords in a circle arc equal. Applied to this particular case it gives, Fig. 102,

$$O_1d \times dQ = (da)^2$$

The distance  $O_i d$  is the difference between the values of A when u=0 and when u=c, that is  $\frac{ic}{l} \sin \phi$ . The distance da is the value of B when u=c, that is  $i \sin \phi$ .

The radius of the large circle being represented by  $R'_i$  the distance dQ is strictly equal to  $(2R + O_i d)$ , but for the present purpose may be taken equal to  $(2R + O_i d)$ , since  $O_i d$  is always small compared with dQ.

Substituting these values in the above equation and solving for  $R_s$ 

$$R = \frac{lr \sin \phi}{2c}.$$

'Multiplying numerator and denominator by 2 this becomes

$$R = \frac{2r\sin\phi \times l}{4c} = \frac{8 \times l}{2k},$$

which is (see Article 95, page 170) Mr Macfarlane Grey's rille so far as the radius is concerned.

The actual position in the arc of the end of the equivalent eccentric corresponding to a given value of n, is given by calculating the value of B, or what amounts to practically the same thing, taking the point p so that the arc is divided proportionally with the link.

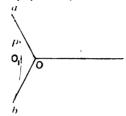


Fig. 103. Polivalint Lounding Crossed Robs. Outside Admission

In the case of crossed rods with outside steam admission, as arranged in Fig. 89, the locus of the end of the equivalent eccentric is a parabola but it is convex towards the centre of the shaft as shown in Fig. 103. The circular are is to be drawn with the same radius as before, but convex towards the crank shaft as in the case of the parabola it replaces.

- 98 The design of a link motion. The different steps in the course of a design may be arranged in the following order
  - (1) Make a preliminary drawing of the gear, adapting the general dimensions to the space available. This drawing settles the length of the link 2c, the length of the eccentric rod I, and the maximum value of u - Keep the eccentric rods as long as possible and the ratio of the length of the rods to the length of the link reasonably large.
  - (2) Neglect the effect of the obliquity of the connecting rod and (assuming proper values for the cut off, lead, and maximum opening for steam in full gear) find the equivalent eccentric ρ, ψ, and the steam lap either
    - (a) geometrically, by the Bilgram deigram, as in Fig. 50, page 77, or
    - (b) analytically as in Article 75 page 124
  - (3) From the preceding Article, equations (6) to (9),

$$\rho\cos\psi = A = r\left(\cos\phi - \frac{c^2 - u^2}{cl}\sin\phi\right).....(1), \quad \bullet$$

$$\rho\sin\psi = B = r\left(\frac{u}{c}\sin\phi\right).....(2),$$

a pair of simultaneous equations in r, the eccentricity, and  $\phi$  the angular advance of the eccentric to be coupled to the top of the link.

Calculate the value of  $\frac{c^2-u^2}{cl}$ , using the maximum value of u, and denote it by p.

Calculate the value of  $\frac{u}{c}$ , using the same value of u, and denote it by q.

Using these values in (1) and (2) and dividing (1) by (2) to eliminate  $r_*$ 

$$\cot \phi = q \cot \psi + p \quad ... \quad (3),$$

from which  $\phi$  can be calculated.

Then r can be found from equation (2)

If the actual eccentrics are made with the eccentricity r and set with respective angular advances  $+\phi$  and  $-\phi$  the gear will give approximately the distribution specified in full gear. The distribution for values of u other than the maximum, and the actual distribution in full gear, must be found from a drawing of the actual displacement curves.

**Example.** Design a link motion so that cut off in full gear occurs at 70 per cent, of the stroke, the lead and maximum port opening being respectively 0.1 inch and 1 inch. Following the above instructions:—

- (1) Assume the motion to be of the general character shown in Fig 76. The motion block cannot be brought exactly opposite the end of the eccentric rod in full gear, so that the maximum value of u will be less than c. Let this maximum value be 5 inches, and let the length of the link be 16 inches, so that c = 8 inches, and let the length of the eccentric rod, l, be 48 inches.
- (2) It will be found that with the data given

$$\psi = 124^{\circ} 50',$$

 $\rho = 2.1$  inches, Steam lap = 1.1 inches.

Crank angle at cut off=113° 35', neglecting the obliquity of the connecting rod.

(3) Calculating the values of p and q,

$$p = 0.101, \qquad q = 0.625.$$

Using these values in equation (3),

$$\cot \phi = -0.333.$$

from which

$$\phi = 108 \ 27'$$
.

With this value of  $\phi$  in equation (2), r=2.92 inches. Hence the eccentricity of the actual eccentrics must be 2.92 inches, and they must be set on the shaft at the respective angular advances,  $108^{\circ}$  27' and -108 27'.

99. The design of a link motion, continued. The weighbar shaft. Having obtained the general dimensions of the gear, the centre of the weigh-bar shaft, and the length of its arm, may be chosen within certain limitations so that the inequalities of cut off due to the obliquities of the connecting and eccentric rods may be diminished, and in particular cases may be quite corrected.

The way to do this is to find geometrically a number of positions of the point of suspension U, each position of U being fixed so that the small vertical movement which the suspending rods, vibrating about it as centre, give the link, combines with the horizontal movement the link receives from the eccentries, to bring the valve to the left of its mid position, by a distance equal to the steam lap, at the instant the piston is at a given percentage of its stroke in the instroke cycle; and to the right of its mid position, by a distance equal to the steam lap, at the instant the piston is at the same percentage of the stroke in the outstroke cycle

When a number of points have been found for equalising the cut off at a series of percentages of the stroke, the weigh-bar shaft may be designed so that the arc described by the end of its arm passes through one or two of them, or has a suitable mean position with reference to the whole group. Since the locus of U must be made an arc of a circle, any three of the positions of U fix both the length of the arm and its centre uniquely, but it seldom happens that the solution found in this way can be practically used. Working the problem in this way, however, generally leads pretty quickly to the most appropriate compromise in the dimensions of the weigh-bir shaft and the position of its axis.

The details of the construction for fixing one position of U in order to equalise the cut off at 60 per cent, of the stroke, positive rotation, are as follows, the data being —

Suspending rods, 12 inches long, jointed to the link at the centre.

Connecting rod = 6 cranks

l = 48 inches.

c = 8 inches

r = 2.84 inches.

 $\phi = \frac{108}{4} \text{ degrees}$ 

r and  $\phi$  are the values found in the problem of the last orticle.

(1) Draw a circle of any radius OK, to represent the path of the

erank pin,  $h_1^{\bullet}$  Let  $s_1Os$  be the line of stroke so that  $s_1s$  represents the stroke of the piston. Take the point  $c_1$  so that  $sc_1=\frac{a}{10}$  of  $ss_1$ , and the point  $c_2$  so that  $s_1c_2=\frac{a}{10}$  of  $s_1s$ 

Find the corresponding crank pin positions  $K_1$ ,  $K_2$ , and from them set out the centres of the eccentrics,  $a_1$ ,  $b_1$  from  $K_1$ , and  $a_2$ ,  $b_2$  from  $K_2$ , the angles  $K_1Ob_1$ ,  $K_1Oa_1$ ,  $K_2Oa_2$  and  $K_2Ob_2$  being each equal to 1081 degrees

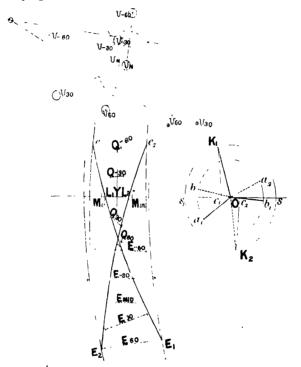


Fig. 104. The setting of the Weigh Bar Shift.

(2) Draw the link in the mid-gear position when the crank is respectively at 0 and 180 degrees. The points at which the link cuts the line of stroke are marked  $M_0$  and  $M_{100}$  on the diagram, Fig. 104. Bisect the distance  $M_0M_{100}$  in Y. Then a vertical through Y represents the common axis of the displacement curves. Set out  $YL_1$ , the

steam lap for the instroke cycle,  $YL_z$ , the steam lap for the outstroke cycle.

(3) With radius equal to the length of the eccentric rods, and centres  $a_1$ ,  $b_1$  and  $a_2$ ,  $b_2$  respectively, draw indefinite arcs which are shown on the drawing passing through the respective points  $e_1$ ,  $E_1$ ,  $e_2$ ,  $E_2$ . Then at the instant of cut off in the instroke cycle, the centre line of the link must pass through the point  $L_1$ , and the ends of the link must be on the respective curves  $e_1$  and  $E_1$ . The link is shown in the figure fitted to its proper position. Similarly for cut off in the outstroke cycle, the centre line of the link must be fitted to the position  $e_1L_1E_2$ 

The line joining the respective positions of the point of the link at which it is jointed to the suspension rods may be regarded as the base of an isosceles triangle, the equal sides of which are the respective positions of the suspending rods whose lengths are assumed known. The point of suspension U is therefore fixed by the apex of the triangle.

In the present case, the link being jointed with the suspension rods at the centre, the short line indicated by  $Q_{\alpha}$  is the base of the isosceles triangle, and  $U_{\alpha}$  is the corresponding position of the centre of suspension

Other positions of U are found in a similar manner. In the diagram four positions of U are shown, namely those equalising cut off at

The position U must occupy at mid-gear is shown also and is found from the base  $M_0M_{\rm ps}$ 

The bases of the triangles, of which these points are the apexes, are shown by full lines and are indicated by  $Q_m$ , etc. It is obviously impossible to fix the weigh-bar shaft so that the end may be turned successively into all these positions. The best that can be done is to arrange the centre so that the end of the arm describes a circular path passing through  $U_M$ , and as near as may be to the other positions.

In the figure the five positions of U which are surrounded by large circles have been found on the supposition that the link is jointed to the suspension rods at the lower end E. The dotted lines  $E_{\infty}$ , etc., show the bases of the triangles from which these points were found. It will be seen that the five circled positions of U he more closely to a mean circular are through the mid-gear position,

This method of considering the design c. the weigh-bar shaft is due to Mr W. H. Maw, and was published in 1871\*.

It will be clear from the foregoing that, when the link is suspended from the centre, the weigh-bar shaft may be fixed by the following rule. Find the point U for mid-gear, and draw a line through it parallel to the line of stroke. Take W the centre of the weigh-bar shaft on this line, choosing an arm long enough to avoid too much angular motion.

made to an essential condition that a link motion must fulfil if it is to be used as an expansion gear, namely, that the changing of the position of the motion block in the link should not seriously interfere with the lead. It has also been shown in the case of the Stephenson link motion, that although for a given position of the motion block in the link the lead may be made practically equal for both cycles, yet when the position is changed, the lead increases towards mid-gear with open eccentric rods, and decreases towards mid-gear when the rods are crossed in the way illustrated in Fig. 89.

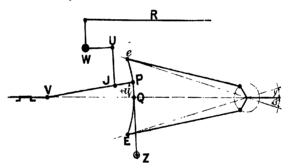


Fig. 105. CENTRE LINE DIAGRAM OF THE GOOCH LINK MOTION

In the Gooch link motion the lead remains constant for all positions of the motion block in the link, but this is not secured without making the gear more complex, as will be seen from the centre line sketch, Fig. 105. The centre of the link, Q, is compelled to move in an arc of a circle by the supporting link QZ, which vibrates about the fixed centre Z. The valve rod, now jointed with the valve spindle at V, is held by the assignmenting link UJ, U being the centre of suspension. The position of P in the link is controlled by the turning of the weigh-bar shaft

\* See Locomotive Engineering, Zerah Colburn. H. Collins & Son, London and Glasgow.

about its fixed axis W, by the reversing rod R. In this gear the displacement of the point V represents the displacement of the valve.

The displacement curves may be drawn by the same method as that detailed for the Stephenson link motion. In this case, however, in addition to fitting the link to the arcs through the points e, E, and Q, the valve rod must be fitted to the centre line of the link, the arc through J with radius UJ, and the line of stroke through V. The positions of the link are however independent of the value of u, and once they are drawn for say 24 positions of the crank, they will serve over and over again for the various positions of U dealt with.

Approximate displacement curves may however be obtained by the use of equivalent eccentries as in the Stephenson link motion, the investigation of their elements following the same course as that for the Stephenson motion

The initial geometrical problem in connection with the gear, in order to secure constant lead for all values of u, may be stated as follows:—

Place the crank at the zero position and find the form of link, so that the valve rod may be moved from one extreme position to the other without moving the point V.

The obvious solution of this problem is to curve the link to the arc of a circle whose radius is equal to the length of the valve rod and whose centre is V. Then, whether the ciank is at 0 or 180 degrees, the valve rod may be moved from one extreme position to the other without moving V, providing that the point Z is chosen so that Q has in the line of stroke in each of these two positions.

The investigation for finding the mean equivalent eccentric for the motion of V, is based upon the following assumptions.—

- The points e and E move with simple harmonic motion in the straight lines joining their respective middle positions with the centre of the crank shaft.
- (2) The inclinations of these lines to the line of stroke are so small that the sines of the angles in each case are given by  $\frac{\sigma}{l}$ , and that  $\cos \beta = \cos \gamma = 1$ , where c is half the length of
- the link and l is the common length of the eccentric rods.
  (3) The quantity u remains constant during a revolution of the crank for a given position of the centre of suspension, U.
- (4) The inclination of the valve rod to the line of stroke is so small that the horizontal motion of P is the same as the horizontal motion of V.

The working out is exactly the same as in the Stephenson link motion down to equation (3), Article 97. Here the value  $\frac{r}{l}$  is to be substituted for  $\sin \beta$  and for  $\sin \gamma$ . After this substitution the equation at once reduces to  $\frac{r}{l}$ .

$$x = r \cos \theta \left[ \cos \phi - \frac{c}{l} \sin \phi \right] - r \sin \theta \left[ \frac{a}{l} \cos \phi + \frac{a}{c} \sin \phi \right] . \quad . \quad . (1).$$

Hence in the form

$$x = A \cos \theta - B \sin \theta$$
,

$$A = r \left[ \cos \phi - \frac{c}{l} \sin \phi \right] = \rho \cos \psi \qquad ... \qquad (2),$$

$$B = i \left\{ \frac{u}{t} \cos \phi + \frac{u}{c} \sin \phi \right\} = \rho \sin \psi \qquad \dots \tag{3},$$

 $\rho$  being the radius and  $\psi$  the angular advance of the equivalent eccentric

When the crank is in the zero position the expression for the horizontal projection of the equivalent eccentric, namely  $\frac{1}{4}\cos\phi-\frac{c}{l}\sin\phi$ , does not involve  $u_i$  therefore it is constant. The ends of the equivalent eccentrics therefore he on a straight line at right angles to the centre line, but distant A from the centre of the crank shaft. The vertical distance of the end of the equivalent eccentric in this line, corresponding to a given value of  $u_i$  is found by calculating the value of B. If the value of B be calculated for u=+c and u=-c, two points a and b will be fixed in the vertical locus, which define the ends of the equivalent eccentric for the extreme positions. Then since B varies as  $u_i$ , the end of the equivalent eccentric in the locus, for a given position of P in the link, is found by taking  $\rho$  so that it divides ab in the same proportion that P divides the link

Fig 106 shows a Gooch motion as it was fitted to the Sinclair 7' 0" single wheel passenger engines of the Great Eastern Railway

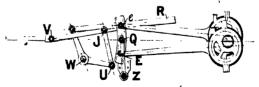


Fig. 106. Gooch Link Motion

Although the Gooch link motion was extensively used for locomotives in earlier days on account of its then peculiar possession of constant lead for all values of u, it has dropped out of use in the present day.

101. The Allan straight link motion. As its name implies, the characteristic feature of this gear is that the link is straight. At the time link motions were introduced the making of a curved link was more difficult than it is now, and probably this fact determined the endeavour to design a motion with a straight link. Fig. 107 shows a centre line sketch of the gear. The fixed axis of the weigh-bar shaft is at W, and the angular position of the shaft is controlled by the reversing rod R. There are two aims forged solid with the weigh-bar shaft, namely, WU and WZ, connected respectively with the straight link at e and with the valve rod at U. The turning of the weigh-bar shaft in the clockwise direction, lowers the link and at the same time raises the valve rod, the latter turning about the joint V. Thus the distance of the centre P, of the motion block from the centre, Q, of the link, that is the quantity u, now depends jointly upon the position of the two "points of suspension," Z and U.

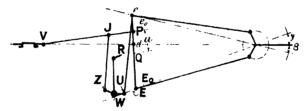
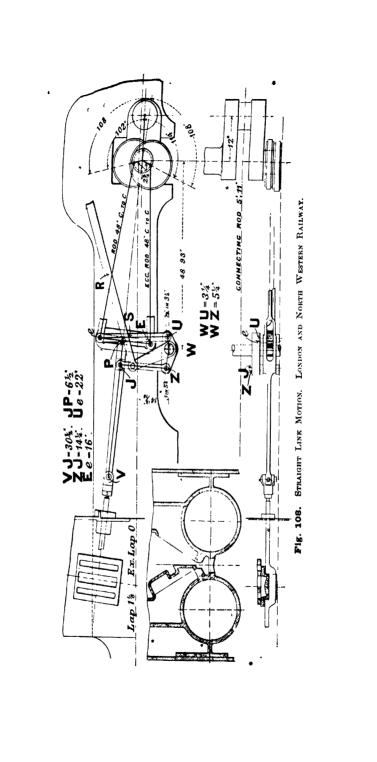


Fig. 107. Centre Line Diagram of the Aflan Straight Link Motion

The gear is similar to the Stephenson link motion in the respect that the link is raised or lowered when the position of P is altered, and it is similar to the Gooch motion in the respect that the valve rod is raised or lowered for the same purpose. This combination of the mechanical peculiarities of both motions makes it possible to use a straight link.

Fig. 108 illustrates the Allan gear fitted to the 6' 6", four-coupled passenger engines of the London and North Western Railway—the famous "Precedent" class. The success of these engines in connection with the express traffic of the railway is too well known to need comment. As will be seen from the illustration, the gear is compact; the centre line of the gear is inclined to the line of stroke of the piston allowing ample room for the steam chest, which lies wedge shaped, above and between the cylinders, the ports are formed in the inclined faces



of the steam chest, and the valves work between them. The way of the steam to the cylinder is made easy, and the way out is also free and unobstructed.

A large number of engines on the London and North Western Railway were fitted with this gear, though not all belonging to the 6'6" class. The advantage of this gear coer the Stephenson form of the link motion is that less room is required vertically to accommodate the link in the two extreme positions since the vertical motion of the link is smaller. Also a smaller angular motion of the weigh-bar shaft is required to change the link from one extreme position to the other, and no balance weights are required on the weigh-bar shaft. I am indebted to Mr. F. W. Webb for the drawings from which Fig. 108 has been prepared.

102 The Allan motion. On the proportion between the arms of the weigh-bar shaft. The initial geometrical problem is more complex in this gear than in either of the two kinds preceding It may be stated thus —

Place the crank in the zero position and find the ratio between the lengths of the arms WU and WZ, so that when P is moved relatively to the link from one extreme position to the other, the point V shall remain at rest

An exact solution is impossible, but an approximate solution, which makes the variation of lead considerably less than the variation in a Stephenson link motion, can be readily obtained

Consider the gear in its central position, Fig. 109. The central point Q, of the link, now coincides with the central point of the motion block. Referring to Fig. 107, it will be seen that when the weigh-bar shaft is turned in the clockwise direction, the centre of the link moves from the position shown in Fig. 109, downwards, to a position Q, shown in Fig. 109 a. At the same time the centre of the motion block P, moves up into a new position P, Fig. 109 a. The distance PQ is the corresponding value of u assuming that the movement has taken place when the crank was at the 0 degree dead point, as indicated in Fig. 109. The path described by Q during this movement has a varying curvature, because the link, as it moves away from the central position, moves about two centres, namely, the ends of the eccentric radii. The curvature of the path of Q may however be considered constant, its radius being equal to the common length of the eccentric rods. Thus in

Fig. 109 a, Q is assumed to have moved down in a circular path whose centre is A, and AQ is the length of an eccentric rod. Also during the movement, the link remains sensibly at right angles to the line AQ.

With these assumptions, the angle PQR, Fig. 109 a, is equal to the angle QAs, so that the sine of both angles is  $y_s AQ$ 

The problem now is, given a position of Q to find what position P must occupy in order that the distance AV may remain constant.

Let AQ=l, VP=a, VJ=b, the angle QAc= the angle  $PQR=\beta$  and the angle  $PVm=\gamma$ .

Then, in the central position,

$$A V = a + b$$

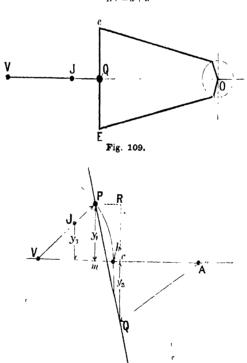


Fig. 109 a. Allan Gear Proportion of the Weigh-Bar Shaft Arms.

In a new position

$$AV = l\cos\beta + PQ\sin\beta + a\cos\gamma$$

In order that AV may be constant

$$a + l = l \cos \beta + PQ \sin \beta + a \cos \gamma$$
.

Expressing the cosines in this expression as sines and using the approximate method  $\sqrt{1+q^2}=(1-\frac{1}{2}q^2)$  for the extraction of the square root after introducing the values

$$\sin \beta = \frac{y_2}{t}$$
 and  $\sin \gamma = \frac{y_1}{a}$ ,

and writing  $PQ = u = y_1 + y_2$ , since the inclination of PQ is small, the expression reduces to

$$a+l = \left(l - \frac{\eta_1^2}{2I} + \frac{(\eta_1 + \eta_2)\eta_2}{I} + \left(u - \frac{\eta_1^2}{2\eta_2}\right) ...$$
 (1).

Put  $y_1 = ny_1$ , and this reduces to the quadratic

$$an^2 + 2an - l = 0$$
 .....(2)

from which

$$n = -1 + \sqrt{1 + \frac{l}{a^{1}}}$$
 .... (3)

The quantity under the root will always be greater than unity, so that if the + sign is taken a positive value of n will be obtained as required by the assumption

In the mechanical arrangement of the gent the upward displacement,  $y_i$ , of the point P is obtained by giving a smaller displacement,  $y_i$ , to a point J in the valve red, taken nearer to V,  $y_s$  being found from  $y_t$  by the proportion

$$y_{\mathbf{s}} = \frac{VJ}{VP} \times y_{\mathbf{t}} \qquad \dots \qquad (4).$$

The ratio between the lengths of the arms of the weigh-har shaft is given by the ratio between y and  $y_{ij}$  neglecting the effects of the obliquity of the links ZJ and Ue, Fig. 108. That is,

For instance in the North Western gear,

$$VJ = 301''$$

$$VP = 37' = a$$

• 
$$QA = 48'' = l$$

From (3)

$$n = (-1 + \sqrt{1 + 1})^2 - 0.514$$

Using this in (5)

$$\frac{WZ}{WU} = 1604.$$

The actual value measured from the engine is 1.614.

When the maximum value of u is fixed, the distance,  $y_1$ , which the point P must rise or fall from its central position is found by combining the relations

$$y_1 + y_2 = u,$$
  
$$y_2 = uy_1.$$

From these

$$y_1 = \frac{u}{1+n}$$
 ......(6).

The distance  $y_i$  which the centre of the link moves above or below its central position is found from

$$y_2 = ny_1 \dots \dots (7),$$

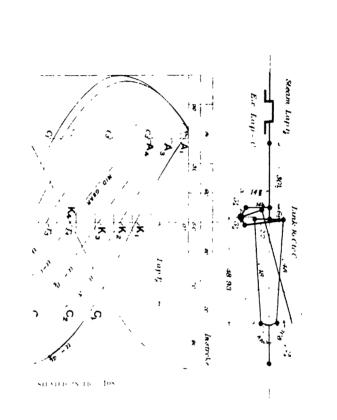
both the quantities on the right side now being known. In the case of the North Western motion, taking u = 4]",

$$y_1 = 2.97$$
",  $y_2 = 1.52$ ".

103. The Allan link motion, continued. Valve displacement curves of the London and North Western Railway straight link motion illustrated in Fig. 108. Since the line of stroke of the piston is inclined 6 degrees to the line of stroke of the valve, the actual angular advance of the positive (forward) eccentric sheave must be diminished by this amount, and the actual angular advance of the negative (buckward) sheave increased by the same amount in order to find the angular differences between-the crank and the sheaves to be used in the drawing of the displacement curves.

A set of displacement curves for values of u,

is shown in Fig. 110, together with the piston displacement curve and the lap lines, the combination forming the valve diagram for the gear. A detailed explanation of the Eagram is unnecessary since it is lettered in a similar way to, the valve diagram, Fig. 86, of the Great Eastern Railway link motion.



The most noticeable feature of the Allan gear brought out by the diagram in comparison with the Stephenson link motion is that the lead is nearly constant, otherwise the properties of the gear are much the same. The percentage diagram, Fig. 111, is drawn by plotting data obtained from the displacement curves on a "u" base. From these curves the distribution in the two cycles, together with the maximum port openings both for steam and exhaust, may be found for any assigned value of u.

It should be clearly understood that, as in the case of the Stephenson link motion (see Article 88), a slight change in the position of the axis, W, of the weigh-bar shaft, slightly changes the shapes of the displacement curves, and a slightly different setting of the valve places the vertical axis of Fig. 110 in a different position relatively to the displacement curves so that the percentages of the stroke at which the several events occur are also changed, with a consequent modification of the curves, Fig. 111. Settings of the gear can be arrived at which give a better result in forward gear but only at the expense of greater mequalities in back gear. The setting shown in Fig. 111 is one which gives about equally good results in forward and backward gear. The percentages at which the several events take place are also influenced slightly by changes in the vertical position of the spring supported part of the engine, because whilst the centre of the crank axle always stands at the same vertical distance above the rails, the centre of the weighbar shaft and in fact all the rest of the gear moves slightly as the engine rises or falls on the springs

The respective paths of the centre of the link and the centre of the motion block are shown in Fig. 112 for the case where  $u=\pm 4\frac{1}{4}$ ". The distance between the curves, measured along the link for the position marked 0, is the value of u, for this is the position occupied by the link when  $\theta=0$ . The slip in any position of the link is the difference between u and the distance between the curves measured along the link. Fig. 113 shows similar curves when u is  $\pm 4\frac{1}{4}$ ".

The drawing of the displacement curves is carried out in the following manner:-

- (1) Set out, Fig. 114, the centre line of the valve motion, the centre of the crank shaft U, and the centre of the weigh-bar shaft W.
- (2) Bring the centre line of the piston gear into coincidence with the centre line of the valve gear, the positive and negative angular advances then being +108 degrees and -108 degrees.
- (3) Assume that a displacement curve is to be drawn for a definite value of u. Draw the weigh-bar shaft in the angular

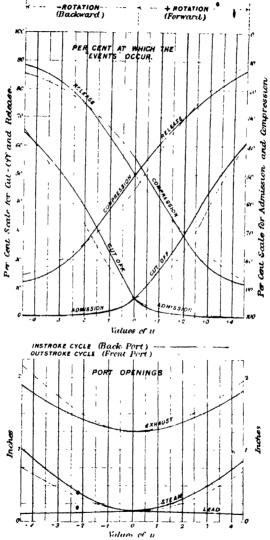


Fig. 111. Percentage and Port Opening Diagnams corresponding with the Valve Diagram, Fig. 110.

position corresponding to the given value of u. The approximate positions of U and Z may be found by setting out the values of  $y_t$  and  $y_t$  obtained by calculation from equations (6) and (7), Article 102, and the actual positions which U and Z occupy may then be found quickly by trial. For example in the case of the London and North Western gear, where n = 0.514,  $y_t$  is equal to 2.97", and  $y_t$  is equal to 1.52 inches when u is equal to 4.4".

- (4) A series of points have now to be found on the displacement curve for 24 equidistant crank positions. Let  $\theta$  be the angle defining one position. Set out the crank at this angle, and from it measure out the angular advances of the two eccentrics and fix the centres, a, b, of the ends of the eccentric radii.
- (5) From a and b respectively as centres and with a radius equal to the common length of the eccentric rods draw the ares ε<sub>i</sub>ε<sub>i</sub> and E<sub>i</sub>E<sub>i</sub>

From U as centre with radius equal to the length of the supporting rod Ue draw an arc cutting  $e_1, e_2$  in  $e_3$ .

With radius equal to the length of the link and from centre e cut the arc  $E_1E_2$  in E. Then eE is the position of the link when the crank angle is  $\theta$ 

(6) Mark off the centres of the valve rod VJP on a straight edge and place the strip on the drawing so that when V has on the line of stroke, J has on an arc struck from the centre Z with radius ZJ, and P has on the centre line of the link eE.

This fitting of the valve rod is much facilitated if a thin wooden rod of length ZJ is jointed to the straight edge so that the point J is constrained to move in its proper path by pinning down the end of the link ZJ at the centre Z.

This construction determines the position of the valve for the given value of the crank angle  $\theta$ . Project this position vertically on to a horizontal line corresponding in vertical position to the given angle  $\theta$ , thereby fixing one point on the displacement curve for the value of u taken in section (3).

Repeat this construction for the 24 positions of the main crank and sketch in the displacement curve.

Assume different values for u, and draw the corresponding displacement curves in like manner. Finally add the vertical axis TT to satisfy some stated condition of valve setting.

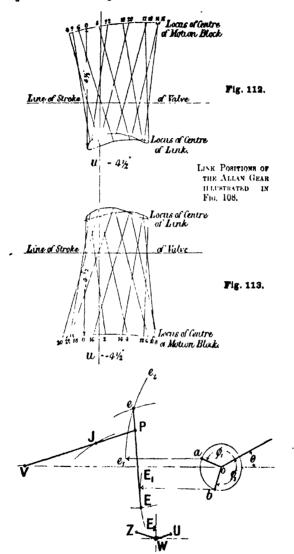


Fig. 114. Setting out an Allan Gear to pind the position of V confessionling with a given value of  $\theta_c$ 

104. The Allan motion, continued. Approximate theory. Equivalent eccentric. The motion of the point V, Fig. 107, may be investigated by an approximate method from which an equivalent eccentric may be obtained for a given position of P in the link.

It is assumed in the investigation that

- (1) The points c and E move with sample harmonic motion in straight lines drawn through their respective mean positions and the ofnire of the crank shaft.
- (2) The inclinations of the two paths to the line of stroke of the valve are so small that the sines of the angles are given by

$$\frac{ed}{I}$$
 and  $\frac{Ed}{I}$ ,

when l -length of the eccentric rod, and that the cosines of the angles are so nearly unity that

- (3) The value of n remains constant during a revolution for a given angular position of the weigh-bar shall.
- (4) The inclination of the valve rod to the line of stroke is so small that the horizontal motion of P is the same as the horizontal motion of V

The working out is exactly the same as in the Stephenson link motion down to equation (3). Article 97. Here the value  $\frac{ed}{t}$  is to be

substituted for  $\sin \beta$ , and  $\frac{Ed}{t}$  for  $\sin \gamma$ 

Now 
$$ed = (Qe - QP + Pd) = (e - u + u_s)$$

and

$$Ed - (EQ + QP - Pd) = (c + u - y_1)$$

But  $y_1 = \frac{n}{1+n}$  from equation (6) of the last article

Hence

$$\sin\beta = \left(c - u + \frac{u}{n+1}\right) - l,$$

$$\sin \gamma = \left(c + u - \frac{u}{n+1}\right) - l.$$

Substituting these values in equation (3), Article 97 at reduces to

Hence in the form

$$J = A \cos \theta - B \sin \theta,$$

$$A + i \left[ \cos \phi - \frac{(n+1)e^2 + nu^2}{c!(n+1)} \sin \phi \right] - \rho \cos \psi \dots$$
 (2),

$$B = \frac{m}{\epsilon} \left[ \frac{c}{I(n+1)} \cos \phi + \sin \phi \right] = \rho \sin \psi \quad .... \quad ..(3),$$

 $\rho$  being the radius and  $\psi$  the angular advance of the equivalent eccentric so that

$$\rho = \sqrt{1 + B}$$

and the numerical value of  $\tan \Psi$  is found from

$$\tan \psi = \frac{B}{4}$$

Example. In the London and North Western gear, Figs. 108 and 110,

 $\phi = 108$  degrees so that  $\cos \phi = -0.31$  sin  $\phi = 0.951$ . The value of n has been extended and Article 102 for this engine, and is 0.514.

Assuming a = 44 inches expressions (2) and (3) above reduce to

$$A = -1.26$$
,  $B = -1.42$ .

so that

$$\sigma = -1.26 \cos \theta - 1.42 \sin \theta$$

for this particular value of #

The radius of the equiv dent eccentric is

$$\rho = \sqrt{1.59 + 1.42} = 1.9$$

and the numerical value of  $\tan \psi$  is

$$\frac{142}{126} = 1126$$

The corresponding angle is 48–24 – the value of  $\psi$  is therefore  $180-48^{\circ}24'=131^{\circ}36'$ 

Corresponding calculations must be made for each separate value of a. The equivalent eccentric may however be found by a geometrical

process depending upon the fact that the locus of the end of the equivalent eccentric radii is a parabola, which for all practical purpose may be replaced by an arc of a circle passing through the three point fixed by

$$u=0$$
,  $u=c$ , and  $u=-c$ .

When u = 0,

$$A_a = r \left( \cos \phi - \frac{c}{l} \sin \phi \right) \dots \quad (4),$$

$$B_a = 0.$$

When  $u = \pm c$ ,

Let  $Oa_b$ , Fig. 115, represent the value of  $A_b$ ,  $Oa_b$  the value  $A_1$ ,  $a_bb_b$  the positive value of  $B_b$  and  $a_bb_b$  the negative value of  $B_b$ 

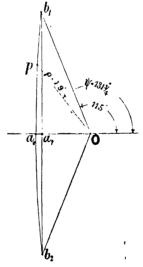


Fig. 115. ALLAN GEAR. EQUIVALENT ECCENTRIC

The problem is now to find the radius, R, of a circle passing through the points  $b_1a_2b_3$ .

The relation  $2R \times a_n a_1 = (a_1 b_1)^n$ 

may be used for this purpose.

where

To draw the locus therefore find the point  $a_s$  by calculating the value of  $A_s$ . Then calculate the value of R from (6) and draw the arc through the point  $a_s$ . The values of  $B_1$  set out above and below the centre line will then fix the extreme points on the locus  $b_1b_2$ . Then for any given position of P in the link the end of the equivalent eccentric p, divides the arc  $b_1b_2$  in the same proportion that P divides the link.

**Example.** Taking the data of the previous Example,

$$m > 0.11,$$
  $q = 0.113$   
From (6)  $R = 24.8$  inches  
From (5)  $B_1 = 2.52$  inches  
From (4)  $A_9 = -1.29$  inches

The arc corresponding to these quantities is shown in Fig. 115 by  $b_1a_bb_2$ .

The equivalent eccentric op is drawn for the value  $u = +4\frac{1}{2}$ . The point p is taken so that  $a_*p$  represents  $4\frac{1}{2}$  on the same scale that  $a_*b_1$  represents 8". From this by measurement

$$\rho = 1.9$$
 inches,  
 $\psi = 1314$  degrees.

These values are practically the same as those found for the equivalent eccentric in the previous example.

The displacement curve corresponding to these values is chain dotted in Fig. 110, from which the difference between the actual curve and the curve obtained by means of the approximate theory can be seen

- 105 The design of the Allan gear. This is carried out in much the same way as for the Stephenson link motion, the steps being as follows
  - (1) Make a preliminary drawing of the gear fixing thereby the length of the link  $2e_i$  the length of the executive rods  $l_i$  the length of the valve rod  $a_i$  and the maximum value of  $a_i$
  - (2) Calculate the ratio between the lengths of the arms of the weight-bar shalt, first computing n from equation (3) of Article 102 and then using n in equation (5) of the same Article.
  - (3) Neglect the effect of the obliquity of the connecting rod and assuming suitable values for the cut off, lead, and maximum opening for steam, in full gear, find the equivalent eccentric  $\rho$ ,  $\psi$  and the steam lap say by the Bilgiam diagram
    - (4) From Article 104, equations (2) and (3),

$$\rho\cos\psi = A = r \left[\cos\phi - 1 \frac{(n+1)\,c^2 - nn^2}{cl\,(n+1)} \sin\phi\right] \tag{1},$$

$$\rho \sin \psi = B \left\{ \begin{array}{l} n + c \\ c \\ d = l + 1 \end{array} \right\} \cos \phi + \sin \phi \left\{ \begin{array}{l} \dots \\ \dots \end{array} \right.$$
 (2),

 $\alpha$  pair of simultaneous equations in r -the eccentricity of the actual eccentrics, and  $\phi$  their respective angular advances

$$\frac{(n+1)e - nn^{2}}{el(n+1)} = p,$$

$$\frac{e}{l(n+1)}$$

$$\frac{u}{a} = v$$

Divide (1) by (2) and solve the resulting equation for obtaining

$$\cot \phi = \frac{(p + r \cot \psi)}{(1 - mr \cot \psi)} \cdot \dots (3),$$

from which  $\phi$  can be calculated

When this is known r can be calculated from either (1) or (2).

If the actual eccentrics are made with the eccentricity r and set with respective angular advances  $+\phi$  and  $-\phi$  the gear will give approximately the distribution specified in full gear. What the actual distribution will be for full gear must then be found by drawing the actual displacement curves

If the line of stroke of the piston is inclined to the line of stroke of the valve, an angle  $\alpha$  say, as for instance in Fig. 108, the angles at which the eccentrics are to be set on the crank shaft will be

Positive eccentric sheave (forward)  $\phi = \alpha$ . Negative eccentric sheave (backward)  $\phi + \alpha$ 

If the line of stroke of the juston is above the line of stroke of the valve the signs before 2 must be changed.

106 The Velocity of the valve of a link motion. The velocity of the valve can be found for a given crank angle and value of u from the displacement curve by the geometrical method of Article 49. For any practical purpose however the velocity can be found with sufficient accuracy from the displacement equation in terms of the equivalent eccentric

The displacement of the valve in all the gears considered can be expressed approximately by the equation

$$r = \rho \cos(\theta + \psi)$$

where  $\rho$  and  $\psi$  are respectively the eccentricity and angular advance of the equivalent eccentric, these quantities being calculated from the dimensions of the gear, and a particular value of u.

Then the velocity of the valve v is

$$v = \frac{d\tau}{dt} = -\rho \sin{(\theta + \psi)} \frac{d\theta}{dt},$$

and when the angular velocity  $\frac{d\theta}{dt}$  is constant it is equal to  $2\pi n$  where n is the number of revolutions of the crank per second. Hence for a given speed

$$v = -\rho \sin (\theta + \psi) 2\pi n.$$

Be careful to express  $\rho$  in feet in order to get the result in feet per second

In the case of a locomotive running at a given speed this expression for the velocity gives the speed of the valve relatively to the valve face.

107 Controlling mechanisms for reversing gears. Some of these have already been mentioned incidentally. It is proposed to conclude this chapter with a few articles specially devoted to this subject.

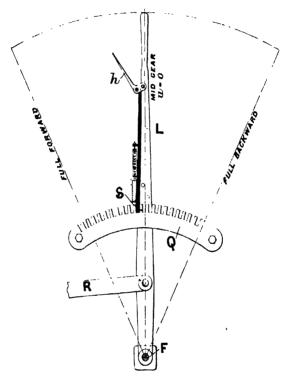


Fig. 116. CONTROLLING LEVER AND QUADRANT.

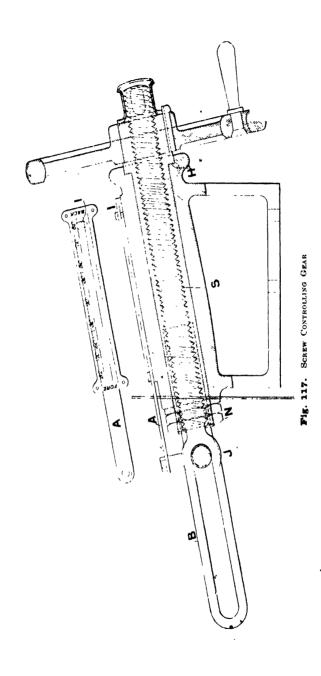
A controlling mechanism should fulfil two conditions. First, it should be able to hold the weigh-bar shaft securely locked in any one position. Secondly, it should allow the shaft to be moved quickly

from one position to another so that the engine may be reversed without delay.

The earliest form of mechanism used for this purpose with link motions is shown in Fig 116. A lever L having a fixed fulcrum pin at F, is connected with the reversing rod R. The lever is locked in any one of the positions corresponding to the notches shown on the fixed quadrant bar Q by means of a spring catch S. By grasping the small handle h and the handle of L together the catch S is withdrawn from the notch and held clear of the quadrant allowing the lever to be turned quickly into another position where on releasing the grap of the handle, the catch is forced into the notch by a spring. The central upright position of the lever corresponds to the central position of the block in the link. The extreme notches correspond to full forward and full backward goar respectively. In locomotives the goar is so arranged that the lever L is pointing over in the direction in which the engine is running. Each of the notches shown on the quadrant Qin Fig. 116 determines a definite position of the motion block in the link above or below the central position that is to say each notch corresponds to a positive or negative value of -nThe change from one notch to the next corresponds to a considerable change in the horse power of the engine as a rule. In order to obtain a finer graduation of power and at the same time to retain substantially formed notches two spring catches may be provided, both being connected to the rod controlled by the small handle h, but arranged on opposite sides of the lever L. The two bars, which holted together form the quadrant bar Q between which the lever L moves, may then have the notches cut so that those in the one bar are displaced relatively to those in the other bar through a distance equal to half the pitch of the notches. Then one or other of the catches will always be in, whilst the other will be out of gear. In this way the number of possible positions in which the lever may be locked is doubled for a given pitch of the notches

As the reversing lever L is brought towards the centre from either of the extreme positions, the cut-off is reduced, and the link motion is said to be "notched up," a term originating with this contrivance, but which has been extended to denote a reduction in the cut-off with almost any kind of controlling gear.

The serew controlling goar shown in Fig 117 is more powerful than, but cannot be so quickly handled as, the quadrant goar. There are two typical forms of this goar. In the one, the boss of the casting carrying the screw is provided with a circular plate, the circumference



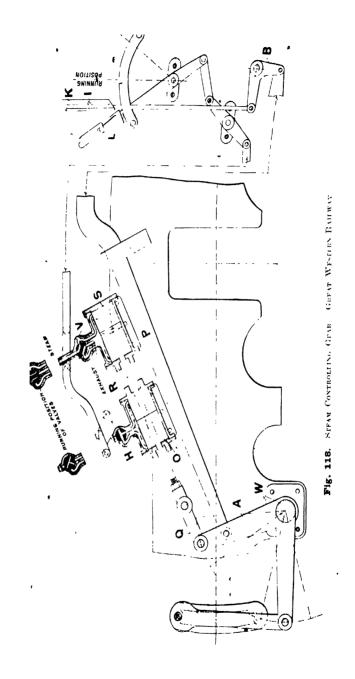
of which is divided into notches, and a spring catch on the handle or wheel by means of which the screw is turned locks the gear in position. In the other type, the one shown in the figure, a long nut and screw are used and a special locking device is dispensed with. It will be seen from Fig. 117 that the nut is a long sleeve, turned on the outside to fit the main easting, and held from end motion by the lock nuts N at the one end and the shoulder H at the other end. The reversing wheel is keyed to the sleeve. The inside of the sleeve is screwed the whole way along to take the screw S, which is jointed to the reversing rod at J. The screw is 2 inches diameter, and is left hand, treble thread, and 1 inch pitch. The pin J is extended into the slot of the bar B, which is bolted to the side of the main casting. The slot therefore serves two purposes. It limits the extent to which the screw can travel out of the nut and it holds the screw from turning. A small index I, carried by the flat bar A, travels over a graduated scale of "cut off" as the serew is moved in a nut. The cut off can be very finely graduated by this gear.

Power controlling gears are fitted to all large marine engines, and from time to time power reversing gears have made their appearance on locomotives, but have never been generally adopted, the screw or the lever and quadrant being almost universally used. Two of the most recent types of power reversing gears for locomotive work are described in the following articles, together with two well-known marine types.

108 Power reversing mechanism. Great Western Railway. A power reversing mechanism, used on some of the engines of the Great Western Railway and which was designed by Mr Dean, is shown in Fig. 118. Two cylinders, S and O, are belted to the inside of the engine frame, and the pistons corresponding to them are fixed to a common piston rod, R, connected by a link, Q, to an arm, A, forged with the weigh-bar shaft whose axis is W. The cylinder, S, is a steam cylinder, the entry and exit of steam to and from it being controlled by the plug valve V.

The second cylinder, O, contains oil, and it is fitted with a by-pass plug valve, H, which establishes or cuts off communication between the two compartments into which the piston divides the cylinder. When the valve H is open, the piston is free to move, the oil displaced from one compartment passing through the passage in the valve to the other compartment. When H is closed, this passage of oil cannot take place, and the piston is therefore locked in position.

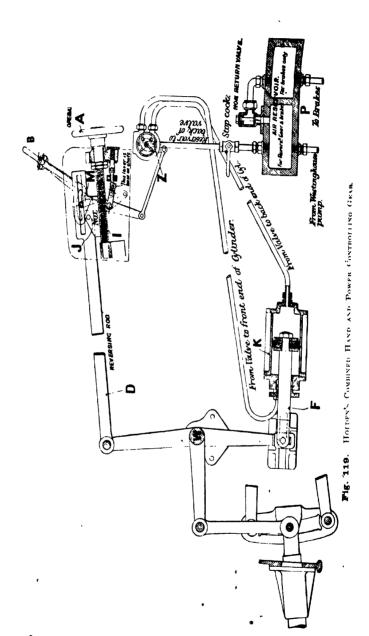
The valves H and V are coupled together by a rod leading to



a controlling lever L fixed in the cab. A rod P, jointed to the arm A, moves an index I, by means of the bell crank lever B. The scale K, over which the index moves, is fixed to the boiler front, and it is graduated for tent off." When the index is at the middle of the scale the motion block is at the middle of the link.

The gear is shown in the position where steam is acting to push the piston S from its central position corresponding to mid gear, so that the weigh-bar shaft is being turned in the direction of forward gear Steam is passing through the valve 3' to the right-hand side of the piston, the left hand side being open to the exhaust The way is also fice for the oil to pass from the left-hand computment of the cylinder  $O_i$  to the right, through the valve H . When the index I shows that the gear has the proper configuration for the cut off desired by the driver the controlling handle L is brought to the centre of the quadrant, where it is held tast by the spring eatch. This movement of L to the centre, sets the valves V and II in the way shown in the separate drawing of them above the main drawing, where the steam valve, V, is shut, and the by-pass valve H is closed thus locking the piston O, and therefore the weigh bar shaft. This central position of the lever  $L_i$  and the corresponding positions of the valves, is the normal running To reduce the cut off in forward gear configuration of the gearthe lever L is pulled back to the right of the centre thereby bringing the piston of S back towards its central position. It will be understood that the lever L does not correspond with a reversing lever of the usual type. It merely operates a steam valve and has three positions, namely, the mid or running position and the extreme positions in the quadrant corresponding to the steam valve being open to one or other end of the cylinder S. This gear works very well so long as the oil and the steam valve are kept perfectly tight. A leaky oil valve allows the piston to gradually creep away from a set position, the creep being accelerated if the steam valve leaks also,

109 Holden's combined hand and power reversing mechanism. In this gear the wheel and series for hand reversing is retained, and extra gear is combined with it for utilising power derived from the compressed air used for operating the Westinghouse brake. Either the hand or the power method can be used at will and the act of using one automatically cuts the other out. A good idea of the apparatus will be formed from a consideration of the general arrangement shown in Fig. 119. The hand gear consists of the wheel A.

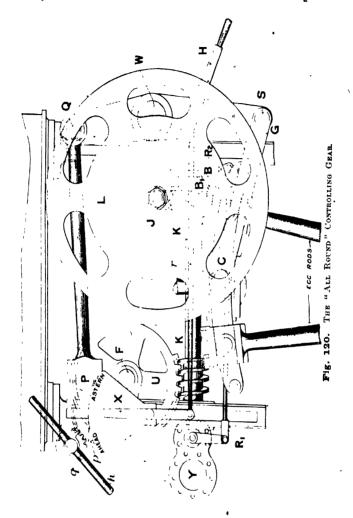


connected to the screw I, which by means of the nut J, moves the reversing rod D, and through it the weigh-bar shaft W. The power gear consists of a cylinder K operated by compressed air from the reservoir P, which is kept charged by the air-pump used in connection with the Westinghouse brake. To reverse by power the handle B is used, and the turning of it controls the entrance and exit of air to and from the cylinder K, through the valve Z. The connection of the hand and power gear with one another is made by means of a cam M formed with the handle B . Immediately the handle B is moved, the cam M lifts the nut, or half nut rather, since the lower half is entirely cut away, clear away from the screw  $I_i$  and then moves the valve  $Z_i$  thereby distributing air to the cylinder K, so that the weigh bar shaft is turned in a direction determined by the direction in which the handle B was originally moved. When the desired position of the shaft is obtained the handle is brought back to its central position, thereby gearing the half nut with the serew again. When running with B in its central position both ends of the cylinder K are in communication with the air reservoir P, through the valve Z. The piston rod F is designed so that the difference of areas between the two tices of the piston multiplied by the air pressure furnishes a force along the piston rod sufficient to balance the weight of the motion hanging from the suspension link Q. The half nut is prevented from jumping out during running by means of the ratchet j and pawl r.

110 The "all round" steam reversing apparatus. The principle of this apparatus is illustrated in Fig. 120, which shows the general arrangement in sufficient detail for the purpose of explaining the reversing mechanism fitted to the engines of some twin series torpedo boats built by Messrs Yarrow and Co for the British Government. Each of the two engines has four cylinders and four corresponding link motions. The handles, reversing wheel, etc., are arranged so that the link motions can be controlled by the engineer standing at one end of the engine.

Referring to Fig 120, and considering one engine, the weigh-bar shaft W runs the whole length of the engine, and each of the four link motions is connected to it by a drag link, coupling the centre of the link C to the end S of a corresponding arm, keyed to the weighbar shaft. One drag link G and the corresponding arm WS, on the weigh-bar shaft is shown in the figure.

The weigh-bar shaft has an arm WQ, keyed to it at about the middle of its length. (The arms WS and WQ are in different planes though they appear continuous in the figure.) Placed opposite to this



arm is a worm wheel U, carried on a shaft F which is supported in suitable bearings attached to the engine framework. A crank pin P in the worm wheel is coupled to the end of the arm WQ by the coupling

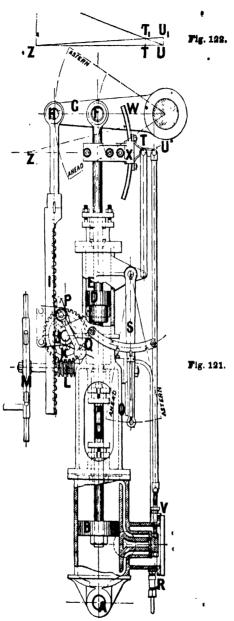
rod QP—A shaft KK placed across the engine, and supported in bearings attached to the frame, carries a worm, graining with the wheel U, a crank (not seen in the figure) at the left end, which may be turned by a small steam engine, of which the back covers Y only are seen, and a bovel wheel B—A longitudinal shaft J, slightly inclined in the vertical plane, carries at one end a bevel wheel  $B_i$  gearing with the wheel  $B_i$  and at the other end a wheel L, which is heavy enough to act as a flywheel to the engine A, and shaped so that it may be used as a hand wheel also

A handle,  $H_i$  operates the vulve of the engine Y through rods and levers  $R_i$ ,  $R_i$ , etc., at the same time moving the index X by means of the rod r. Thus the weigh-bir shaft may be turned either by turning the hand wheel L or by admitting steam to the cylinder  $Y_i$ , the wheel L in the latter case simply revolving as a flywheel. If steam is admitted to Y continuously, the engine drives the worm wheel U continuously in one direction, whilst the end of the arm Q reciprocates to and fro, the length of the reciprocation being so arranged that the links are moved backwards and forwards between the extreme positions of full gear ahead and full gear astern

It is not absolutely necessary therefore to provide the engine Y with reversing gear, but it is usually made reversing so that the links may be moved from a given position to any other position with the smallest possible angular motion of the worm wheel

Reversal of Y is effected by turning the steam valve about its valve spindle by the handle H. The valve is evaluation in form, and is provided with ports so that in one angular position on the spindle it works as an ordinary slide valve with outside steam admission and inside exhaust, but when turned into a second position about the valve spindle it works with inside steam admission and outside exhaust. In this way reversal is easily effected

The method of reversal by the interchange of steam and exhaust passages is more fully discussed in Article 130 in connection with the steam steering engine. When the links have been brought into any desired position, the weigh-bar shaft is locked by clamping the worm wheel U against one of the vertical standards of the engine by means of a T-headed bolt which passes through the standard, the T-head lying in a suitably formed groove inside the rim of the worm which. The clamping is done by turning the handle  $h_i$  which by means of a longitudinal connecting shaft, turns the wheel  $q_i$  which is in gear with the spur wheel p. The boss of p is seriously to form the nut of the T-headed bolt. The wheel p and the worm wheel U are of course on opposite sides of the column seen in the figure to the left.



THE BROWN STEAM CONTROLLING GRAR.

A model of the "all round apparatus" can be seen at the South Kensington Museum fitted to the model of the engines of the s.s. Flamboro. In this case the engines are worked from the front and the design of the gran is modified accordingly

111 Brown's power reversing mechanism, Fig 121 The piston rod C, of a cylinder, continued through a small hydraulic cylinder E, is coupled directly to the arm of the weigh-bar shaft at F. The joint Fmust therefore move in a circular are, and the necessary angular freedom is obtained by connecting the main casting of the mechanism to the frame of the main engines by a single pin joint A. When steam is admitted into the cylinder the piston rod pushes or pulls the weigh-bar shaft into a new angular position, the speed being innited by means of the hydraulic cylinder E = A block piston Dis cottered to the piston rod and a small hole is drilled through it, and, the cylinder being filled with water, every movement of the piston rod is accompanied by a transference of water from one side to the other of the piston D through the small hole, the hydraulic resistance to this transference acting as a brake. The cylinder is kept filled with water in an ingenious way. The water which collects in the bottom of the valve chest is forced by the steam pressure in the chest through the non-return valve R, and into the hydraulic cylinder which is connected to R by a small copper pipe, which can be seen in the

The interesting feature of the gear, however, is the way the position of the piston in the cylinder, and therefore the angular position of the weigh-bar shaft, is controlled by the reversing lever, the piston starting to move when the lever is moved in the quadrant, and continuing to move until it stops in a position which places the weigh bar in the definite angular position corresponding with the notch in the quadrant to which the reversing lever is moved.

The mechanism for doing this is simple. An arm X is bolted rigidly to the piston rod. The end of this aim is grooved to the curve of the bar W, which can move easily up or down through the groove. The curved bar carries a shank TU, so that U-T-W is one piece. The valve rod is jointed with this piece at U, and the bell crank end of the reversing lever is connected to it at T. Consider the motion of the piece U-T-W relatively to the arm X. When it is pushed up or down, the curved part W is compelled to slide in the slot, and the motion of the points T and U is the same as though they were points on a bar centred at the centre of curvature Z of the piece W, as indicated in Fig. 121 and above in Fig. 122. So that in considering the motion

of the piece U-T-W, so far as the motion of the points T and U are concerned, the actual mechanism may be replaced by a bar, carried on a centre Z formed in the arm X, the arm of course being supposed extended to the left for this purpose. The valve is set so that when Z-T-U is horizontal the piston is at the centre of its stroke and the valve is in its central position, so that no steam can get into the cylinder

Suppose now that the reversing lever is pulled into the astern position. The point T is moved upward to  $T_{ij}$  as indicated in the centre line drawing of the bar, Fig. 122, the bar turning about the centre  $Z_i$  and hence the point U is moved upwards to  $U_i$ , causing the valve to open the lower port of the cylinder. Steam is admitted and the piston at once begins to move up, but in doing so it carries the point Z upward also, the bar now turning about  $T_1$  as a fixed point, and when Z arrives at  $Z_1$  the point  $U_1$  has moved downwards to its original position, thus bringing the valve back to the central position and shutting off the steam. The distance moved through by the piston depends upon the amount of the vertical movement originally given to T, and this depends upon the angle through which the reversing lever is turned. Hence if the quadrant is divided up into notches, the movement of the reversing lever from one notch to another corresponds to a definite vertical movement of the piston, and to a definite angular position of the weigh-bar shaft. It will be seen from the drawing that the end of the weigh-bar shaft carries a rack I gearing with a pinion J, the shaft of which carries a worm wheel K, operated by a worm L. which is keyed to a shaft on which the hand wheel M is fastened. When steam control is used the worm is thrown out of gear with the wheel by means of a cam. By throwing this cam in, the engine can be reversed by hand. A locking arrangement is provided so that the main engines can be linked up to, and locked in, any position in the ahead gear. A pawl P, weighted to disengage automatically by the weight Q, may be thrown into gear with the rack where it is held in gear by the downward pull of the piston, a pull which is always maintained by setting the slide valve so that it stands slightly open in ahead gear

## CHAPTER VIII.

## WALSCHALRU GEAR RADIAL GEARS

112 Resolution of the valve displacement curve into two components. The actual motion which the slide valve receives from the eccentric of a simple valve gear may be resolved into two component motions which motions may be considered as derived from eccentric crinks which are themselves components of the eccentric which produces the actual motion.

The case of most practical interest is that where the eccentric crank is resolved into two components respectively at right angles to and at 180 degrees with, the main crank, it being understood that if the line of stroke of the valve is inclined to the line of stroke of the piston the two are brought in a coincidence before beginning the resolution.

In Fig. 123, Od is the 180 degree component and Oh is the 90 degree component of the eccentric Ou. The corresponding component displacement curves are shown in Fig. 124 tegether with the resultant displacement curve due to the eccentric Ou. Points on the curves are obtained by projecting the successive positions occupied by the points h, g and d as the enables placed in different positions.

In the diagram, any horizontal distance  $O_t a_t$ , measured to the resultant curve, is equal to the algebraical sum of the components,  $O_t d_1$  and  $O_t h$ .

Neglecting the effect due to the obliquity of the eccentric rods, the displacement curve corresponding to the component eccentric Od is a cosme curve whose maximum ordinate is

$$Od = r\cos\phi = A,$$

and points on the curve may be calculated from

$$x = A \cos(\theta + 180) = -A \cos\theta$$

The displacement curve corresponding to the component eccentric Oh is a sine curve whose maximum ordinate is

$$Oh = r \sin \phi - B$$
,

and points on the curve may be calculated from

$$x = -B \sin \theta$$
.

It should be carefully borne in mind that the quantity A is the displacement of the valve from its central position when  $\theta=0$  degrees and is therefore equal to the steam lap plus the lead; and that B is the displacement of the valve when  $\theta=90$  degrees

If the angular advance is changed to an equal negative value in order to obtain negative rotation of the crank, the 180 degree, or the A component, as it may be called, remains unchanged, whilst the 90 degree, or B component, changes its sign. This will be seen at once from Fig. 123 where Ob represents the eccentric when  $\phi$  is changed to a negative value, and Od and Og are the respective A and B components. The B component may now be conveniently described as the 270 degrees component, or -90 degrees component. The sine curve corresponding to the negative value of B is shown with fine dots and the resultant curve due to Ob, or what is the same thing, the combination of the A component curve with the dotted curve, is shown with thick dots.

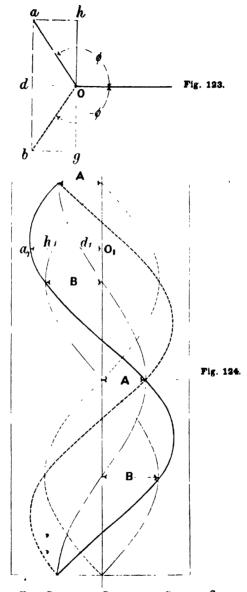
Thus the combination of the A component curve with a 90 degree component curve gives a resultant displacement curve corresponding to positive rotation, and the combination of A with a 270 degree component will give a curve corresponding to negative rotation

If A, still constant in value; be combined with either a 90 or 270 degree component of smaller maximum value, the resulting displacement curve will have a smaller maximum value and the cut off will be eather.

There are two limiting cases, first when B=0, secondly when A=0. When B=0 the distribution is done by the A component eccentric alone and it will be recognised that this corresponds to a mid-gear distribution of the link motion, where the cut off is so excessively early that the distribution of steam cannot work the engine against a load. When A=0, a steam distribution is only possible if the valve has no steam bap and works without lead, the corresponding indicator diagram being a rectangle.

With a fixed value of A and a value of B varying between a positive and a negative maximum, families of displacement curves are obtained which determine various cut offs.

The family of curves, Fig. 86, illustrate this point. Each curve may be looked upon as the combination of an approximately constant A curve, the displacement curve at mid-gear, with a B curve whose



Analysis of a Valve Displacement Curve into two Component Curves.

maximum value is proportional to the quantity u, where of course u ranges between a positive and negative maximum value.,

This principle of combining two displacement curves may be extended to include the combination of any pair of periodic curves roughly following the shape of sine and cosine curves whose values are a maximum and zero respectively both when the crank angle is 0 and when it is 150 degrees.

Thus, any periodic curve of the general shape of a cosine curve whose maximum value is A (the lap plus the lead), when the crank angle is 0 or 180 degrees may be combined with a curve of the same period, the general shape following a sine curve whose value is zero when the crank is 0 or 180 degrees to give a resultant curve which will represent the movement of a slide valve capable of producing a distribution of steam which will drive the engine

113. The reversing gear known either as the Heusinger von Waldegg or the Walschaert gear. This is a gear, Fig. 125, constructed on the principles discussed in the previous article. The 180 degree or A component, of the valve motion, which it will be remembered is 180 degrees from angular agreement with the crank, is obtained by means of a lever VJD, connected to the valve spindle at V, and to the crosshead at D . In the usual arrangement of the gear the point V is compelled to move in a straight line by substantial guides, consequently the connection between the end D and the crosshead must either be slotted, or the link DH may be interposed to allow a small amount of vertical freedom to D as it swings about the point V. The point J must be so chosen that, considering it to be a fulcium at rest, the maximum movement of V to the right or left of its central position is equal to the steam lap plus the lead. The lever VJD thus has two functions one, the reversal of the motion of the crosshead so that the motion of V is equivalent to the motion it would receive from a ciank placed at 180 degrees with the main crank, this is secured by placing the point J between V and D the other, the reduction of the stroke of the crosshead to the amount 2.4, which is accomplished by properly choosing the position of the point Jin relation to the points V and D

The 90 degree component of the valve motion is obtained by connecting the fulcium J to a link Ee, curved to the radius of the valve rod JP, and driven by a single eccentric sheave so placed with regard to the crank that the link Ee passes through the position where J is its centre of curvature, at the instants when the crank is passing through either of the dead requirement is E.

180 degrees. The angular position of the sheave is in consequence  $\pm$  90 or  $\pm$  90 degrees with the main crank if F is on the line of stroke of the piston, but if for constituctive reasons it is found convenient to place F nearer to Q, the angle is slightly changed. The point Q, about which the link oscillates, is a fixed axis, hence, when the point P is brought into coincidence with Q, by the turning of the weigh-bar shaft whose fixed axis is at W J receives no motion from the link, that is B=0, and the motion is in and gear.

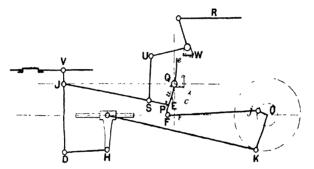
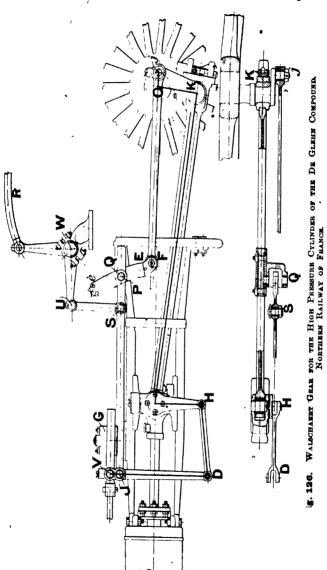


Fig. 125. WALSCHAERT VALVE GEAR.

Variation of the value and sign of B is obtained by placing the point P in a position either above or below the fixed axis Q. The position is controlled by the suspending link SU and the weigh-bar shaft

Which half of the link will determine the sign of B for positive rotation (forward running) depends upon which end of the link is connected to the eccentric sheave, and again, whether the eccentric sheave is 90 degrees approximately, in front of or behind the crank. To ascertain which is the half for positive rotation in any given case with outside steam admission, imagine the crank placed at 0 degrees, and then to be turned slightly in the positive direction. Then that half of the link will determine positive rotation which mofes away to the left of the vertical centre line.

The radius of the eccentric sheave Oj must be so chosen, that the motion V receives through the link Ee and the lever DJV, D being now the fulcrum about which the lever turns, has a stroke equal to  $2B_0$  when P is at its greatest distance either above or below Q, B itself having the value corresponding to full gran.



Thus the link Es has two functions, one, the changing of the sign of B, which is brought about by placing P either above or below Q, the other, the changing of the magnitude of B, which is accomplished by holding P at a definite distance from the fixed centre Q by the weighbar shaft gear

When the crank is at 0 or 180 degrees the valve will be open by the amount of the lead. In order that the lead may remain constant, whilst the gear is changed from full forward to full backward, the point J must remain at rest whilst this change in the configuration takes place. This condition is secured by curving the link Ee to the radius JP. The initial geometrical problem in connection with the design of all reversing gears is thus exactly fulfilled. The distinguishing characteristics of this gear are therefore that the lead is constant for all positions of P in the link Ee, and that only one eccentric sheave is required.

114. Walschaert gears, Northern of France Railway, and Belfast and Northern Counties Railway. The good record of the De Glehn four cylinder compounds on the Northern Railway of France in connection with the express service between Paris and Calais is well known in this country. It is interesting to notice that the De Glehn compounds are fitted with the Walschaert gear for both the inside and outside cylinders, the general arrangement of the gear for the outside cylinders being shown in Fig. 126 and for the inside cylinders in Fig. 127.

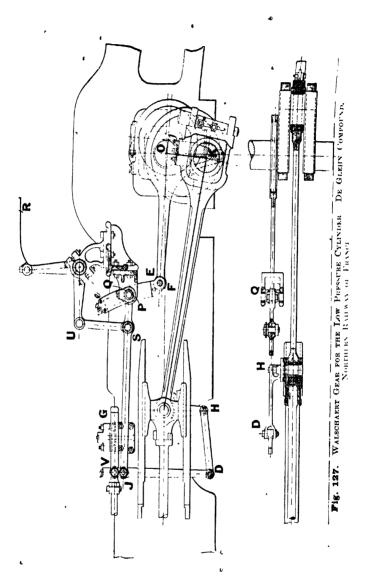
Both drawings are lettered similarly with the centre line sketch, Fig. 125, so that there will be no difficulty in following the several parts. It will be observed that the eccentric sheave giving the 90 degree component, has been replaced by a return crank in the case of the outside gear. Fig. 126. This is the usual arrangement when the gear is applied to outside cylinder engines.

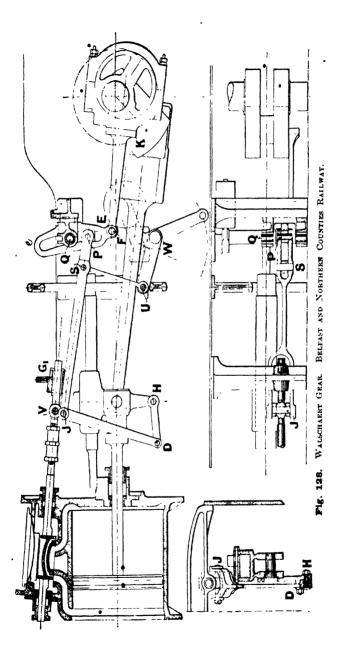
Another point to notice is, that the return erank, though equivalent to an eccentric placed at 90 degrees with the crank, is connected by its eccentric rod to the lower end of the link Ee, so that the lower half of the link determines positive rotation. Therefore u is to be considered negative when measured from Q, upwards, and positive when measured from Q downwards.

The valve spindle is constrained to move in a straight line by the guide G, which is fixed to the slide bar

The slide valve worked by this gear is of the balanced type and \*\* has already been illustrated in Fig. 16.

The gear for the inside cylinders, Fig. 127, is generally similar in





design to that for the outside cylinders. An eccentric sheave drives the link, being coupled by its eccentric rod so that the lower half determines positive rotation. The bracket guiding the valve spindle is bolted to the engine frame. I am indebted to Mr Bosquet of the Northern Railway of France for the drawings from which Figs. 126, 127, 16 and Fig. 132 below have been prepared.

Fig. 128 shows the arrangement of the Walschaert gear used by Mr Malcolm on some inside cylinder four coupled locomotives, belonging to the Belfast and Northern Countries Railway.\* It will be noticed that the centre line of the cylinder is inclined to the line of stroke of the valve. The general arrangement of the parts can easily be made out from the drawing.

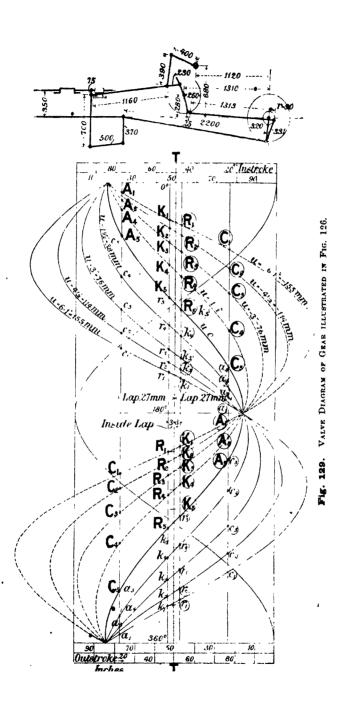
The Walschaert gear is extensively used in locomotive practice on the Continent, in fact it is so rapidly displacing the link motion there that it may be considered the standard form of reversing gear for locomotive work

It has been used to a limited extent on manne engines, Messis Denny of Dumbarton having littled a modification of it, designed by Mr Walter Brock, to about 70 sets of engines, including those of the Dover, Calais Lord Warden and other vessels which are running on the cross channel and other services. A fine model of the engines of the Princess Hemiette fitted with this gear can be seen in the South Kensington Museum.

115 Walschaert gear continued. Valve displacement curves of the high pressure gear fitted to the Northern Railway of France engine illustrated in Fig. 126. The symbol u means, in connection with this gear, the distance between the points P and Q when the crank is in the zero position, u being reckoned positive when it is measured from Q, downwards, and negative when measured from Q, upwards

A set of displacement curves for values of u,

 $64.''=155\,\mathrm{mm}\,,\qquad 4\frac{1}{2}''=114\,\mathrm{mm}\,,\qquad 3''=76\,\mathrm{mm}\,,\qquad 1\frac{1}{2}''=38\,\mathrm{mm}\,,$  zero,  $-641''=-155\,\mathrm{mm}\,,\qquad -4\frac{1}{4}''=-114\,\mathrm{mm}\,,\qquad -3''=-76\,\mathrm{mm}\,,\qquad -1\frac{1}{2}''-38\,\mathrm{mm}\,,$  is shown in Fig. 129 together with the piston displacement curve and the lap lines, the combination forming the valve diagram for the gear. In this case there is negative inside lap so that the points of release, marked generally by the letter r, and the points of compression, marked generally by the letter k, do not fall on the vertical centre line of the diagram. It will be seen from the diagram that the lead is constant for all values of u.



The common vertical TT is placed to secure equality of lead in the two cycles. The centre line diagram at the top of Fig. 129, shows all the dimensions, and the setting of the weigh-bar shaft for which the displacement curves were drawn. A small vertical movement of the weigh-bar shaft centre relatively to the crank axle has a negligibly small effect on the distribution. In the actual engine the valve was set so that there was a slight difference in the leads for the two cycles.

The drawing of the displacement curves may be carried out in the following manner.—

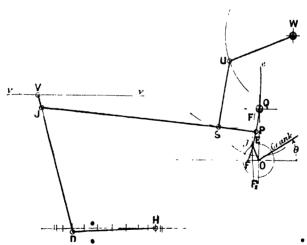
- Set out, Fig. 130, the centre line of the valve spindle vv, the centre of the ciank shaft O, the centre of the weigh-bar shaft W, and the fixed centre about which the link oscillates, Q.
- (2) Assume that a displacement curve is to be drawn for a given value of u. Draw the weigh-bar shaft in the angular position corresponding to the given value of u, thus fixing the position of the point of suspension, U.
- (3) A series of points have now to be found on the displacement curve for 24 equidistant crank positions. Let  $\theta$  be the angle defining one position. Set out the crank at this angle and measure out from it the position of the eccentric, obtaining thereby the position of the point j. With radius equal to the length of the eccentric rod jF, draw an arc  $F_iF_2$  from j as centre. Or suppressing the eccentric rod, this arc may be set out with a curved template. Fig. 130 is arranged on the assumption that this method has been used. (See Article 90, Fig. 93.) With radius equal to QF and centre Q cut the arc  $F_iF_2$  in F. This fixes a position of the link. To draw it, use a template, shaped to the curve Ee, having the points Q and F correctly marked on it.
- (4) Draw the path of the point H and fix the position of H in the path for the given value of θ.
- (5) Make the chain of links HD, DJV, JSP, SU out of thin wood, letting in small transparent celluloid windows at V and P, pierced with a fine hole to define the points V and P, and arranged that the under surface of the celluloid is in contact with the surface of the paper. Fix points to the links at the centres corresponding to U and H and finish them, to a fine needle point.
- (6) Then placing one centre at U, and the other at the position found for H, move the chain into the position where the point P is on the centre line Ee whilst the point V is on the line

of stroke of the valve. This position can be found with accuracy since the fine centre lines can be brought easily to the centre of the needle hole in the windows. Then prick through the position V. This fixes the position of the valve corresponding to the crank angle  $\theta$ . The remaining 23 positions can be found in a similar manner, and the disp'acement curve for the given value of uis then found by projecting or transferring these positions to the horizontals of the displacement diagram corresponding to the several crank angles, thus fixing the 24 points through which it passes

(7) Repeat the process for different positions of the point of suspension U corresponding to stated values of u and having drawn the family of curves place the vertical axis TT, to satisfy some stated condition of valve setting

Walschaert gear continued. Approximate theory. First Approximation. In this investigation the several obliquities of the connecting rod, of the eccentric rod and of the suspension link, US, are neglected, and the value of u is supposed to remain constant

Consider first the 180 degree component of the motion point J. Fig. 130, is the fulcrum about which the lever VJD turns under the action of the crosshead, and when the B component is equal



Pig. 130. WALSCHARRY GEAR. CENTRE LINES AFTER "SUPPRESSING THE ECCENTRIC ROD.

to zero this point is at rest, except for the small vertical motion consequent upon the constraint of V in a straight line.

The point J must be chosen between the points V and D so that the stroke of V is equal to 2A, that is to twice the steam lap plus twice the lead

Let R be the radius of the main crank, then

$$TJ \quad JD = A \quad R \quad . \qquad ... \qquad .(1)$$

is a relation from which the proportions of the lever may be found when A and R are known

The displacement X, of the point H, from its central position, in terms of the crank angle, which is of course the same as the displacement of the crosshead centre, is given by

$$X = R \cos \theta$$
 . . . . . . . . (2).

Hence, neglecting the obliquity effect of the link HD, the value of the 180 degree component displacement is given by

$$-\frac{VJ}{JD} \times R\cos\theta \qquad \dots \dots (3).$$

Secondly, consider the 90 degree component.

Let 
$$QF = c$$
,  $QP = u$ ,  $O_{I} = r$ .

Neglecting the obliquity of the eccentric rod, the displacement of the point F, from its central position, is given by

$$r\cos(\theta + 90) = -r\sin\theta$$

and the displacement of any point P, distant u from Q, will be given by

$$-\frac{u}{c}r\sin\theta, \text{ if } P \text{ is below } Q, \dots \dots (4).$$

For positive rotation of the crank the negative expression must be taken. In this u may be supposed positive. Therefore by changing the sign of u to minus when it is measured out above Q, the expression will be adjusted for negative rotation without further consideration.

Neglecting the effect of the suspension link, and assuming the rod JP to move always parallel to itself, the point J will have the same horizontal movement as the point P. Hence equation (4) represents the displacement of the point J from its central position. So far as the lever VJD is influenced by the motion of the link it

turns about D as a falcrum. The motion of J must be increased in the ratio VD:JD to find the value of the 90 degree component at the valve spindle. Therefore the displacement of the point V, due to the action of the eccentric and the links through which the action is transmitted, is thus

The whole displacement of the valve, to a first approximation, is then given by

$$\sigma = -\frac{VJ}{JD} \times R\cos\theta - \frac{raVD}{cJD}\sin\theta \qquad . \tag{7}$$

So that

$$A = \frac{VJ}{JD} + R \qquad (8),$$

$$B = \frac{ra\, VD}{cdD} \qquad . \qquad . \qquad . \qquad (9)$$

**Second Approximation.** By taking into account the obliquity of the connecting and eccentric rods an expression giving a near approximation to the actual displacement of the valve can be obtained. The assumption that the value of u remains constant must still be made. This assumption can be maintained sensibly true for either fore gear or back gear by properly choosing the position of the weigh-bar shaft. In engines designed for express work, and which therefore run usually in forward gear, the position of the weigh-bar shaft should be chosen to make the variation of u a minimum in forward gear. The result of that adjustment is generally to increase the ship in back gear.

Referring to Article 71 it will be seen that equation (1) gives the displacement of the piston from its central position in terms of the crank angle  $\theta$ . Neglecting the effect of the link DH, this is also the displacement of D, Fig. 130, from its central position. Hence the 180 degree component of the valve displacement is given by

$$-\frac{VJ}{JD} \times R\left(\cos\theta + \frac{R\sin^2\theta}{2L}\right) \quad ..... (10),$$

where L is the length of the connecting rod and R is the crank radius.

If r is the eccentric radius, and l is the length of the eccentric rod, the displacement of the point F from its central position is given by the expression

$$T\cos(\theta + 90) + \frac{t^2 \sin^2(\theta + 90)}{2t} \dots \dots (11),$$

which is equivalent to

$$-\left\{r\sin\theta-\frac{r^2\cos^2\theta}{2l}\right\} \qquad (12).$$

The displacement of the point P, corresponding to a positive value of u, is

$$-\frac{ru}{c}\left\{\sin\theta - \frac{r\cos^2\theta}{2l}\right\} \qquad (13).$$

Assuming u to remain constant in value, and neglecting the effect of the obliquity of the rod JP, the point J has the same horizontal motion as the point P.

Multiplying expression (13) by  $\frac{VD}{JD}$  to obtain the value of the 90 degree component at the valve spindle, and adding the expression for the 180 degree component given in equation (10), the actual displacement of the point V is given by the expression

$$\omega = -\frac{VJ}{JD} \times R \left\{ \cos \theta + \frac{R \sin^2 \theta}{2l} \right\} - \frac{VD}{JD} \times \frac{n}{c} \left[ \sin \theta - \frac{r \cos^2 \theta}{2l} \right]$$
 (14).

This expression gives the displacement of the valve, reckoned from its central position, or centre of oscillation.

The position of the centre of oscillation changes as the value of u is changed. In order that the expression may give the displacements from a common axis, as the axis TT in the valve diagram, Fig. 129, for all values of u, a constant term must be added to the equation, whose value is to be adjusted to each change in the value of u.

Thus, let  $f(u, \theta)$  represent the right side of equation (14). Therefore general

$$x = f(u, \theta) + \ell^{*} \quad . \tag{15}$$

Let a definite value,  $u_i$ , be given to  $u_i$  then any value may be assigned to C. If the assigned value is zero, the equation gives the displacements from the centre of oscillation corresponding to  $u_i$ . For greater generality let the constant have the arbitrary value  $C_a$ 

When another value is given to u,  $u_n$  say, the constant  $C_a$  changes to  $C_x$ . If the gear is set so that the lead is constant, the values of x at the dead points are the same for all values of u. Hence when the displacements are measured from a common axis, the axis determined by the initial value  $C_a$  assigned to the constant,  $C_x$  can be found from the equality obtained by putting  $\theta = 0$ , in the general equation obtaining x, the displacement at the dead point  $= f(u_1, \theta_0) + C_1 = f(u_n, \theta_0) + C_x$ , from which

$$C_x = f(u_1, \theta_0) + C_4 - f(u_n, \theta_0)$$
 .....(16).

In order that the lead may remain constant for all values of u, the link must be arranged so that the point J is its centre of curvature when the crank angle is either zero or 180 degrees. The eccentric rod

and link must therefore have the configuration indicated in Fig. 131 for the cank angles 0 and 180 degrees. Unless this condition is realised, the point P cannot be moved from its extreme upper position

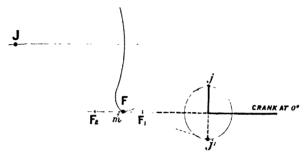


Fig. 131. WALSCHAFRY GEAR. THE SETTING FOR CONSEAST LEAD.

to its extreme lower position without changing the lead. The point m marks the mid-position of F, and it will be at once understood from the figure that the link does not occupy its mid-angular position when the crank is at either dead point.

**Example.** The dimensions of the several quantities in equation (14) in the case of the high pressure gear of the Northern of France engine illustrated on page 226 are —

VJ = 75 mm.

JD = 700 mm , therefore VD = 775 mm.

 $R=320~\mathrm{mm}$ 

L = 2200 mm.

i = 90 mm

 $t = 1313 \, \text{mm}$ .

c = 260 mm

Introducing these values in equation (14) and adding the arbitrary constant  $C_{\bullet}$ ,

$$x = -34.25 (\cos \theta + 0.0727 \sin^2 \theta) - 0.383u (\sin \theta - 0.034 \cos^2 \theta) + C_a$$

Table 9 exhibits the result of applying this formula to calculate points on the displacement curve for mid-gear, where u=0. The value assigned to the arbitrary constant is zero. This value corresponds with the position of the common vertical axis TT, Fig. 129, which is there drawn so that at corresponds with the centre of oscillation of the valve

for mid-gear. From the Table it will be seen that the results, compared with the actual displacement, measured from displacement curves, are within about half a millimetre. There may of course be small errors in the drawing, so that so far as mid-gear is concerned, the formula may be considered fairly accurate.

The results of calculating points on the displacement curve with values of  $u_i^* \pm 114 \,\mathrm{mm}$ , are given in Table 10. The corresponding measurements from the actual displacement curves are also tabulated. The differences between the measured and the calculated displacements are greater than in the case of mid-gear, chiefly because the suspension link keeps u in a continual state of change. In tore gear, however, where u has positive values, the differences are not great.

TABLE 9. Walschaert Valve Gear.

Comparison of the calculated values of the displacement with the values measured from the artual displacement carces. Mid-gear.

	τ	J.	
Value of $\theta$	Calculated value mini	Actual value mm	Difference mm
0	-3425	-342	0.05
30	- 30 2	- 30 9	070
60	-1897	- 193	033
90	- 249	- 26	011
120	15 2	156	0.40
150	29 1	289	0.20
180	$34\ 25$	340	0.25
210	29 1	29 2	0.10
240	15 2	157	0.50 *
270	- 249	- 28	0.31
300	- 18 97	- 190	0 03
330	- 30 2	- 306	04
360	-3425	- 342	0 0 5

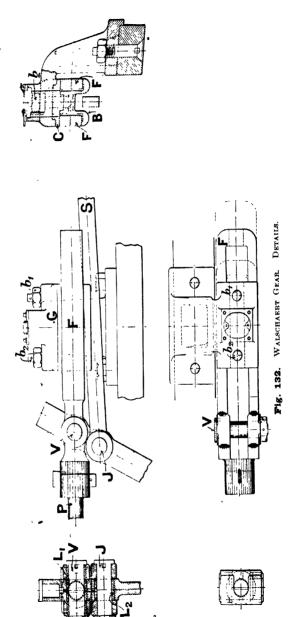
TABLE 10.

Comparison of the calculated values of the displacement with the values measured from the actual displacement curves when u is equal to +114 and -114.

	<b>u</b> = +1	14 mm		u	114 mm.	
Angle	Calculated mm.	Measured mm.	Difference mm	Calculated mm	Measured min	Difference mm
0	-3425	- 34 20	0.05	- 34 25	34 20	0 05
30	-5248	-5260	012	- 807	8 20	0.13
60	-57.91	-5860	0 69	19 94	21 00	1.06
90	- 47 63	- 49 00	1 37	4266	44 30	1 64
120	-2266	25 00	131	54 19	55 50	1:31
150	6.83	7 00	0 17	51 24	51 20	004
180	34.25	34 20	0.05	34  25	34 20	0 05
210	50 50	50 00	0.50	7.58	5 50	2.08
240	51.95	53 00	1 0 5	- 21 50	27 50	6 00
270	39 68	41 00	132	- 44 67	53 00	8:33
300	17 70	18 50	0.80	- 55 69	61 50	5.81
330	- 882	- 900	0.18	- 5174	53 00	1.26
360	-3425	- 34 20	0.05	- 3125	34 20	0.05

## 117. The design of a Walschaert gear. Proceed as follows:-

- (1) Make a preliminary drawing of the gear, adapting the general arrangement to the space available, and for greater generality suppose the point F, Fig. 125, to move in an arc which is above the line of stroke. This drawing fixes provisionally the length of the connecting rod, the position Q, of the centre of the link, the position, W, of the centre of the weigh-bar shaft, the distance QF = c, and the maximum value of u. It is generally convenient to connect the end of the eccentric set at 90 degrees, the value of u will be positive, when measured out below the centre Q, and negative, when measured above the centre. The signs of u must be reversed if the eccentric is set 90 degrees behind the crank.
- (2) Assume suitable values for the cut off, lead, and maximum port opening for steam, for full gear, and find the equivalent eccentric, whose constants are ρ. Ψ.



(3) From Article 116, equations (8) and (9),

$$\rho\cos\psi = A = \frac{VJ}{JD} \times R \quad . \quad (1),$$

$$\rho \sin \psi = B = \frac{VD}{JD} + \frac{\tau u}{c} \qquad (2)$$

(4) Design the link V.ID. Equation (1) may be written in a more convenient form for this purpose, namely

$$JD = \frac{R}{A} \times VJ \qquad ... (3)$$

Then take a value of VJ large enough to obtain proper joints at V and J, substitute the known values of A and R, and calculate the length JD.

The design of the joints at V and J is an important matter A drawing of these joints for the gear illustrated in Fig. 126 is shown in Fig. 132. The actual distance between the joints is 75 mm. = 2.95". Pins V and J are obtained each 40 mm. = 1.575" diameter, with room for the guin-metal bushes  $L_1, L_2$ .

The object of the general arrangement is to get the centar of the joints V and J in the same vertical plane in order to avoid a twisting action on the valve spindle. This is accomplished by coupling the end of the valve spindle,  $P_{\gamma}$  to a long stripp  $F_{\gamma}$  which carries the joint V centrally, and is guided in a straight line by the bracket  $G_{\gamma}$  bolted to the slide bars. A gun-metal block  $B_{\gamma}$  held up by the bolts  $b_1,b_2$  forms, with a gun metal piece  $C_{\gamma}$  a guide for the stirrup. The block  $B_{\gamma}$  is hollowed out centrally to allow clearance for the valve rod when the motion block P is at the upper part of the link

(5) Having fixed the lengths VD and JD calculate the value of r from expression (2) substituting therein the maximum value of u. Thus

$$r = \frac{JD}{VD} \times \frac{eB}{u} \qquad \dots \qquad (4)$$

- (6) Find the proper angular advance of the cecentric sheave, or return crank, in the way detailed in the example following
- 118. Example. Design a Walschaert valve motion, the full gear conditions being —

Cut. off, 80 per cent of the stroke Maximum opening, 1 625 inches Lead, 0.3 inch The equivalent eccentric corresponding to these conditions is

$$\rho = 2.655$$
 inches  $\psi = 120$  degrees 15 minutes.

Therefore

$$A = \text{lap} + \text{lead} = \rho \cos \psi = 1.33 \text{ mehes.}$$
  
 $B = \rho \sin \psi = 2.3 \text{ mehes.}$ 

The steam lap is therefore 103 inches.

Design of the lever VJD. Let the stroke of the pisten be 24 inches, so that the crunk radius, R, is 12 inches, and let the distance VJ be 3 inches. Then from equation (3) of Article 117,

$$JD = \frac{12 \times 3}{1.33} = 27$$
 inches.

Determination of the radius of the eccentric sheare. Let it be assumed that the preliminary drawing has shown that the following dimensions will be convenient, namely,

$$c = 10$$
 inches.

u = 6 inches for a maximum value.

Also the calculation just made gives JD=27 inches; and VD=(27+3)=30 inches. Then from equation (4) of the present article,

$$r = \frac{10 \times 27 \times 23}{6 \times 30} = 3.45$$
 inches.

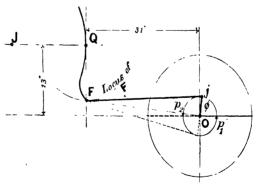


Fig. 133. WALSCHART GEAR. THE SETTING OF THE ECCENTRIC SHEAVE.

To find the angular advance of the eccentric sheave, or the angular position of the radius of the return crank. Set out the link, Fig. 133, in the position where J is the centre of curvature. J is to be taken on a line parallel to the line of stroke of the valve and passing through the

rentre of the link Q - JQ is equal to the length of the valve rod and this length is determined by the preliminary drawing

Draw QF at right angles to the line of stroke of the piston. Join FO. Then the points  $p_i$  and  $p_i$  are very nearly the positions occupied by the centre of the eccentric sheave when the point F is at its lead points. Draw Oj at right angles to FO. Then Oj is the position which the eccentric must occupy when the erank is at 0 degrees, and therefore  $\phi$  is the angle at which it must be set with regard to the grank. The dotted position of the crank and eccentric shows that the point F is brought to the same position in its path when the crank is in the 180 degree position. Hence for either of these positions the motion block may be moved from one extreme position of the link to the other, without moving the valve, because J is all the time at the rentre of curvature of the link

The weigh-har shaft centre can now be chosen to minimise the slip in either gear or to keep the slip as small as possible in both forward and backward gear.

119 Radial gears. Hackworth's gear. John Wesley Hackworth, in 1859, patented a valve gear, based upon the principle of combining two motions at right angles, which differed considerably from the forms of gear in use up to that date, and this gear may be booked upon as the first of a class of reversing motions which have since been developed under the name of radial gears.

Fig. 134 shows the principle of the gear which Hackworth patented in his specification, number 2448. An eccentric OD is placed at 180 degrees angular advance with the main crank, OK. The eccentric rosshead J is constrained to move, by the guide PP, in a straight path which may be placed exactly at right angles with the line of stroke of the piston of it may be inclined to the right or to the left of this vertical position and held at a definite angle, by means of suitable controlling gear, motion taking place about the fixed axis W. The valve rod VY is now jointed to the eccentric rod at a point V

It will be seen at once that the horizontal projection of the motion of V gives a component at 180 degrees with the erank, the half stroke of which may be made equal to the quantity A, the lap plus the ead, by suitably choosing the eccentric radius and the position of he point V along the rod, and that the horizontal projection of the notion of J in its inclined path P gives a 90 degree component, which, reduced in the ratio VD/JD, combines with the 180 degree component to produce a resultant horizontal motion of V suitable for working a slide valve. The magnitude of the 90 degree component is

varied by varying the inclination  $\kappa$  of the path PP. When the path is vertical, the 90 degree component vanishes (neglecting the obliquity of the valve rod VV) and the motion is in mid-gear. When the inclination is changed over from one side to the other of, the vertical position, the sign of the 90 degree component is changed, and the engine is reversed. Such briefly is the principle of the action of Hackworth's gear. An approximate expression for the motion of the valve can easily be obtained, when the effects of the obliquities of the connecting rod and the valve rod are neglected.

The horizontal projection of the motion of D in terms of the crank angle is given by

$$-0D\cos\theta$$
.

Assuming the path PP to be vertical, so that the 90 degree component is zero, the corresponding horizontal motion of V is

$$-\frac{VJ\times OD}{JD}\cos\theta$$

Again, assuming the path PP to have its fixed axis W placed at the mid-position of J's motion, the vertical displacement of J from its central position in the path, neglecting the obliquity of the eccentric rod, is given by

$$OD \sin \theta$$

When the path is inclined at an angle  $\kappa$  to the vertical, the horizontal projection of this is approximately

and since J is turning about the point D as fulcium the magnitude of this must be reduced in the ratio VD, JD. Hence the 90 degree component is given by

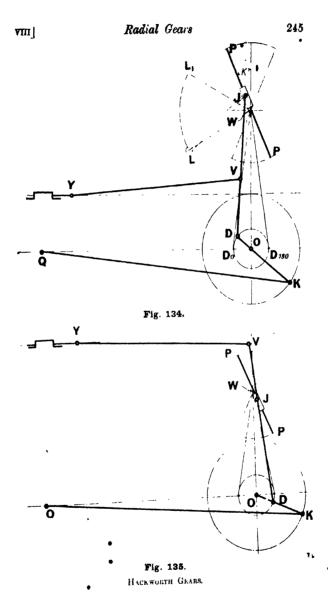
$$\pm \frac{\tan \kappa \times VD \times UD}{AD} \sin \theta \quad .. \qquad . \qquad .. \qquad .. \qquad . (2),$$

the plus sign being used when the path is inclined to the left of the vertical and the minus sign when it is inclined to the right. The former position corresponds to negative rotation, and the latter to positive rotation. Therefore the whole displacement of the valve from its central position is given approximately by

$$x = -\frac{VJ \times (iD)}{JD} \cos \theta \pm \tan \kappa \frac{VD \times (iD)}{JD} \sin \theta . \dots (3),$$

from which

$$\begin{split} A &= -\frac{VJ \times (\partial D)}{JD}\,, \\ B &= \pm \frac{VD \times (\partial D)}{JD} \tan \kappa. \end{split}$$



The variable angle  $\kappa$  occurs in the second term of the expression only, consequently the lead is constant, because when  $\theta = 0$  or 180 degrees, this term vanishes.

Hackworth shows an arrangement, in the specification quoted above, in which the path PP is replaced by a radius link LJ, so centred, that the point J is guided in a curved path. The inclination of the curved path is changed by changing the centre L about which the link LJ can vibrate. The controlling go it must be so designed that the centre L may be held fixed anywhere along the path  $DL_0$ .

Hackworth's inclined path may be placed between the points V and D, as shown in Fig. 135.—In fact he shows such an arrangement in his specification No. 4246 taken out in 1876.—In this case the eccentric sheave OD must be placed with zero angular advance, because the fulcium of the rod J is between V and D, the motion of V is therefore 180 degrees out of phase with the crank.

120 Marshall gear. In 1879, specification No 2138 Marshall patented the arrangement of the Hackworth gear, Fig. 134, in which a

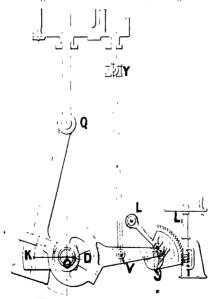


Fig. 136. MARNHALL VALUE GEAR,

curved path was used instead of the straight slide PP, in combination with certain-modifications of the steam ports, with the object of correcting some of the inequalities of distribution connected with this type of radial gear. The curved path is determined by a radius rod. Marshall's gear applied to a marine engine is shown in Fig. 136, where the arrangement used for changing the postion of  $L_i$  along the arc  $LL_i$ , is shown. The eccentric OD is placed at 480 degrees with the main crank, and the point J is constrained to move in a curved path whose inclination to the mid-position can be varied by means of the worm wheel and quadrant shown in the figure

- 121 Two geometrical conditions which must be satisfied by a radial gear. There are two principles connected with the design of radial gears which require closer examination. These may be stated as two conditions which must be satisfied, if the gear is to give a fairly symmetrical motion to the valve about the centre of oscillation combined with the property of constant lead.
  - (1) When the crank is placed at 0 or 180 degrees, the movement of the reversing gear from one extreme position to the other should not cause any motion of the slide valve. This condition implicitly fixes the position of W, Fig. 134, the fixed axis of the path PP, because it is the turning of this path about the axis W, from one extreme position to the other, which reverses the engine from full forward to full backward gear. Hence the point J must coincide with the point W in these two crank positions, if the condition is to be fulfilled.
  - (2) The point W should be as nearly as possible the centre of the stroke of J, otherwise, the movement of the valve will be unequal about the centre of oscillation, because the 90 degree component will have different maximum values during the rotation of the crank from 0 to 180 and from 180 to 360 degrees.

Briefly, for an accurate gear, J must move as though driven by a rod infinitely long, so that J is at the centre of its stroke when the main crank angle is 0 or 180 degrees, and when the inclination of the axis is changed it must turn about an axis coincident with J's central position.

It will be seen at once that Hackworth's gear does not exactly realise these two conditions. So far as the first is concerned, this is exactly realised if the axis of the path is made to coincide with the

<sup>.</sup> Reproduced from the Proceedings of the Institute of Methanical Engineers, 1880.

position J occupies in a line at right angles to the stroke through the crank shaft centre, when the crank is placed at 0 or 180 degrees. But by placing W thus it makes it impossible to realise the second condition exactly, because owing to the obliquity effect of the rod DJ, W is not then the mid-position of J's travel. It is also evident that when the path PP is placed in the mid-gear position there will be a small value of the 90 degree component due to the obliquity of the rod YV.

122 Impracticability of connecting the point D directly to the connecting rod. An examination of Fig. 134 would suggest the practicability of taking the motion of D from some point on the connecting rod, thus obtaining a valve gear which is both a reversing and an expansion gear, without the use of eccentric sheaves at all. Try it, and then apply the conditions of the previous article. Thus, set out the crank circle, Fig. 137, and assuming some point on the connecting rod, R, find the points  $R_a$  and  $R_{19a}$  occupied by this point when the crank is respectively at 0 and 180 degrees. Bisect  $R_aR_{pr}$  in  $O_1$ , and through  $O_1$  draw a line  $O_1Z_1$  at right angles to the line of stroke of the

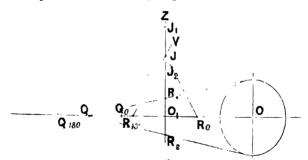


Fig. 137. Obliquity Uperet of the Link RJ

piston. Then take any point J on this line. Then  $JR_0$  is the link corresponding with the eccentric rod DJ of Fig. 134, in the position when  $\theta=0$ .  $JR_{10}$  is the position of the link when  $\theta=180$  degrees. The point J must therefore coincide with the axis W of the path, if the first condition of the previous article is to be fulfilled; for only then can the path be moved from one extreme position to the other without moving the valve. If the second condition is to be fulfilled, J must also mark the mid-travel of the end of the link  $JR_0$ . Mark off  $J_1$  and  $J_2$ , the dead points of J's motion, and it will be seen at once that the realisation of the second condition is impossible.

123. Brown gear. This is shown in Fig 138, as applied to a Swiss locomotive. The connecting rod drives the crank through the rocking lever GHI. And with the gear shown, it is possible to connect the point D of the lever VJD to a point on the lower connecting rod IK so that the two conditions of Article 121 may be approximately satisfied. In gears of this type, the effect of the obliquity of the valve rod on the movement of the valve, may be approximately corrected by causing the point J to move in a path struck with a radius equal to the length of the valve rod itself. A characteristic feature of Brown's gear is the use of a system of compound levers to guide J in an approximately circular path of large radius, for the purpose of correcting the obliquity of the valve rod, whilst the levers themselves are short. The arrangement is clearly shown in Fig 138. A frame which can be turned about

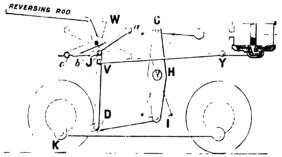


Fig. 138. BROWN VALVE GLAR

a fixed axis W, carries two fixed centres at a and c respectively. The link ab vibrates about the centre a, guiding the point b in the arc of a circle. A slide is centred at c through which the end of the lever Jb is free to move. The motion is in fact geometrically the same as that of the oscillating cylinder engine, ab being the crank, and cb the cylinder and piston rod, but the piston rod is produced to J. By properly choosing the proportions, the point J may be constrained to move in a curve whose curvature is approximately constant. By choosing the proportions so that the curve has a radius equal to the length of the valve rod the obliquity errors of the valve rod may be approximately corrected.

Many examples of this gear may be seen on the locomotives in Switzerland, to which country the use of the gear has been principally confined.

<sup>\*</sup> For further illustration of the Brown gear and some historical notes in connection therewith, see a paper by Otto Grunger, published in Engineering, Jan. 15, 1886.

124 Joy gear. In 1879, specification No. 929, Mr David Joy patented a gear worked from the connecting rod. The point D, Fig. 139, is connected to a lever RS, R being pinned to the connecting rod itself, and S being guided along the line  $O_1Z$ . With this arrangement it is possible to choose the point D in such a position along the link RS that the two conditions of Article 121 may be simultaneously satisfied. The way to choose this point will be shown in Article 129.

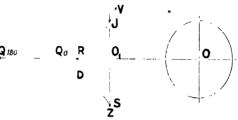


Fig. 139. Correction of the Obliquity Explict of DJ by the introduction of the Link RS

This gear formed the subject of a paper communicated to the Institute of Mechanical Engineers at the Barrow meeting in 1880, at which Mr F. W. Webb exhibited a London and North Western six coupled goods engine, cylinders 18" diameter × 24" stroke, fitted with the gear. Subsequently, the gear was used extensively on the London and North Western Railway, nearly the whole of the compound locomotives being fitted with it. It was used to some extent on the Great Eastern Railway, by Mr T. W. Worsdell, and to a much greater extent on the North Eastern Railway. Mr Aspinall has introduced the gear on the Lancashire and Yorkshire Railway, and Fig. 140 shows the gear applied to a four coupled express engine, belonging to the Lancashire and Yorkshire Railway.

It will be seen that the 180 degree component of the valve displacement is obtained from the lever VJD, the lower end receiving a horizontal movement from a link RDS, jointed to the connecting rod at R, and to a radius rod at S. The object of the radius fod FS is to guide the lower end of RDS as nearly as may be in a vertical straight line.

The lever VJD must be so proportioned, that considering the point J to be a fulcium, at rest, the end D receives such a horizontal movement, that the point V moves a distance equal to the lap plus the lead, to the left or to the right of its central position. The fulcrum J must also be placed between the points V and D in order to secure

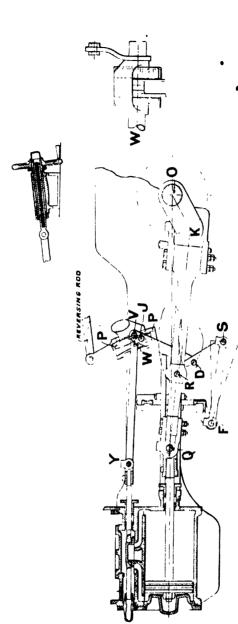


FIG. 140. JOY VALVE GLAR LANCASHIRE AND YORKSHIRE RAILWAY The dimensions are given in Figs. 142 and 145

the reversal of the movement of V with regard to the movement of the point D. Thus the point V communicates a motion to Y, so that Y moves as though it were connected to an eccentric crank having 180 degrees angular advance, and a radius equal to the lap plus the lead

The 90 degree component of the motion is obtained by guiding the point J- in a fixed inclined path, PP, which is centred at W, and which is curved to the radius of the valve rod VY. The projection of J's motion on the line of stroke, multiplied by the ratio VD/JD, is the value of the 90 degree component. The multiplication by the ratio VD/JD is necessary, because, so far as the motion of V is influenced by the sliding of J in the inclined path, the lever may be supposed to move with the end D always in a vertical straight line, so that D is a fulcium about which the lever is turning

When the crank angle is 0 or 180 degrees the projection of J's motion is zero, and when the crank is at 90 degrees or 270 degrees, the projection is in the neighbourhood of a maximum

Hence the projected motion of J, combined with the motion which Y receives from the horizontal movement of the point V, together give a displacement to the valve, which is suitable for distributing the steam.

The magnitude of the 90 degree component is changed by changing the inclination of the path PP and the change in the inclination is made, just as in the Hackworth gear, by means of a rod, connected with a reversing wheel of the usual type. When the reversing wheel is turned into the position where it holds the path PP, so that a tangent to it at W is vertical, the 90 degree component of the motion is zero, and the apparatus is in "mid-gear" J simply slides up and down in the path without moving Y, and the only motion Y receives is that from the horizontal movement of P about the fulcium J.

The sign of the 90 degree component is changed by changing the inclination of the path PP from one side to the other of the mid-position.

The condition that the lead shall remain constant for all degrees of expansion is fulfilled if the point J coincides with the point W, the fixed axis of the path PP, when the crank occupies either the zero or 180 degree positions. Then, and then only, may the path PP be turned about its axis W, from one extreme inclination to the other, without moving the valve.

The fulfilment of this condition cannot always be realised exactly when the gear is fitted to a locomotive, especially one of the tank engine class, because the variation in weight of the eigene, due to the

gradual consumption of fuel and water, allows the frame to rise slightly on the springs, carrying with it the axis W, without any corresponding movement of the crank axle. Consequently, when such movement takes place, the points J and W do not coincide when the crank is either in the zero or the 180 degree position.

The arrangement of the gear shown in Fig. 140 is that which is applied to some 7' 3" four coupled express passenger engines on the Lancashire and Yorkshire Railway.

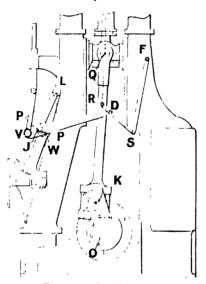


Fig. 141. JOY VALVE GLAR

Fig. 141 shows the gear applied to a marine engine, where a radius rod JL is used to guide J in the path PP. The radiuation of the path is changed by changing the position of the centre L.

125 Joy gear continued. Displacement curves for the gear shown in Fig. 140. Here the variable quantity u, which has hitherto been used to define the different settings of the gears examined, is replaced by a constant  $\kappa$ , which defines the angle made by the path PP with its mid-position

Defining this constant more accurately, let a tangent to the path PP, at the point W, when the path is in mid-gear, be considered the

`- 3' .a

zero position. Let  $\kappa$  now be defined as the angle which the tangent to the path  $\mathcal{A}$  W, makes with the zero position, being reckoffed positive when the angle is measured to the left of the zero position and negative when measured to the right. A little consideration will show that with this definition of the sign, a positive value of  $\kappa$  corresponds to positive rotation, always assuming that the steam is admitted at the outside of the valve.

Displacement curves corresponding to values of  $\kappa$ ,

$$21\frac{1}{2}^{\circ}$$
,  $14\frac{1}{3}$ ,  $7\frac{1}{3}^{\circ}$ ,  $0$ ,  $-7\frac{1}{3}^{\circ}$ ,  $-14\frac{1}{3}$ ,  $-21\frac{1}{3}^{\circ}$ ,

are shown in Fig 142. It will be observed that the common vertical axis is placed to secure equality of lead in the two cycles, and that the lead is constant. The piston displacement curve is added, and also the lap lines, thus converting the drawing into a valve diagram for the gear.

126. Joy gear continued. The drawing of the displacement curves. The gear should be drawn in the configuration corresponding to, at least, 24 equidistant crank positions in order to find the corresponding positions of the valve. It is necessary to set the gear out full size in order to obtain the accuracy required in practice. This is a somewhat troublesome process, and it is generally more expeditious to make a light model of the gear in wood, and to use it for the purpose of finding the position of Y, for a series of crank angles, by direct measurement, thus obtaining data for the drawing of the displacement curves.

There is a way, however, in which, by the use of templates all the rods of the gear may be "suppressed," and the paths of different points in the gear may be drawn, without using the actual centres or lengths of the links at all, so that all the point paths, necessary to the solution of the problem of locating the valve for a given crank position, may be drawn grouped about a centre, and thus all the work may be done on a reasonable sized sheet of paper. The method will be given in detail, because it may be applied generally to many similar problems, and the working out of the Joy gear by its means therefore may be considered as a particular application of a general method of great utility.

The method depends upon the following Theorems A particular application of Theorem 1 has been given already in Article 35.

127. Theorem 1°. Fig 143. If the respective paths of two soints, P and Q, of a rigid link, be given, and if one path be displaced

<sup>\*</sup> Due to MM Coste and Manquit, Traité Théorique et Pratique des Machines à Vapeur au point de vue de la Distribution. Baudry & Cie, Paris, 1886.

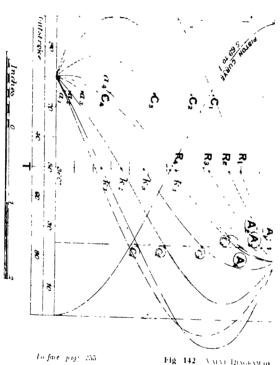


Fig. 142 VALVE DIAGRAM OF

a distance PQ, parallel to any fixed direction, corresponding positions of P and Q in their respective paths may be projected, the one from the other, by a template, shaped, so that one edge is circular and of radius PQ whilst another edge is a radius of that circle and placed so that when the corner of the template is on the displaced path, the curved edge passes through the given position or the other path, whilst the straight radial edge is parallel to the direction of displacement, and is pointing in the direction of the true position of the path on which the corner of the square is placed.

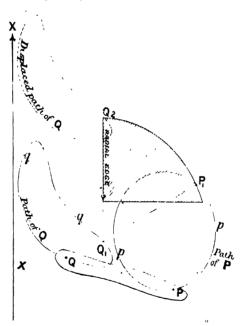


Fig. 143. LOCATING CORRESPONDING POINTS ON DISPLACED PATHS

Proof Let P, Q be two points on the rigid link whose respective paths are Ppp and Qqq. Let  $P_1$  be any given position on the path of P. The corresponding position of Q in its path, is found by drawing an are, with radius PQ, from  $P_1$  as centre, cutting Qs path in Qs. Suppose the path Qqq to be moved parallel to XX, and through a distance equal to QP.

Considering the point  $Q_1$ , its new position will be  $Q_1$ ,  $Q_1Q_2$  being equal to  $QP_2$  and parallel to XX. But  $Q_1Q_2$  is equal to  $Q_1P_1$ . Therefore the points  $P_1$  and  $Q_2$  lie on the arc of a circle drawn from  $Q_1$  as centre.

Clearly the position  $Q_i$ , in the displaced path, may be fixed by using the set square indicated by shading in the figure, where it is shown both shaped and placed as required by the theorem.

The proof is true for every pair of corresponding points on the paths. Hence the theorem,

Corollary. If the path of Q is displaced, parallel to XX, a distance QC, and the path of P, parallel to XX, a distance PC, then, if the algebraic sum of the two displacements is equal to PQ, an arc of radius equal to PQ will still pass through a pair of corresponding positions

It will be noticed that one of the points, Q, is fixed by the corner of the template. In actual work it is rather awkward to locate a point in this way and it will be found more convenient to make a template of the kind already described in Article 35. No difficulty will be found in applying the principles of the theorem with a template or curve so shaped. Another way is to draw a curve of radius PQ on a sheet of squared tracing paper. The lines of the paper enable the curve to be placed on the paths quickly and conveniently so that the corresponding positions of two points on the paths may be pricked through.

This Theorem was extended by MM. Coste and Maniquet to find the position of any point on the link relatively to the displaced paths, the locus of this point being of course the displaced point-path. The following form of this extension of the Theorem, which is simpler and more quickly applied, is due to Mr Archibald Sharp.

**Theorem 2.** If the displaced paths of two points P, Q, of a rigid link, be given (the paths having been displaced relative to one another a distance PQ, in a direction parallel to a fixed direction XX), and a series of corresponding points on them be joined by straight lines  $p_1q_1, p_2q_2, p_3q_4$ , etc., then, if each of these straight lines be divided at  $c_1, c_2, c_3, c_4$ , etc., in the same proportion that a point C divides the straight line PQ, a curve drawn through the points  $c_1, c_2, c_4, c_5$ , etc., is the point-path of C, displaced a distance CP, relatively to the path P, in a direction parallel to XX.

<sup>\*</sup> See an article by Mr Archibald Sharp, who applied them to draw the point paths of several mechanisms, including a Joy gear, in an article in Lagracering, April 6, 1894.

Let the circle and the dotted curve, Fig. 144, be the given paths which have been displaced a distance PQ relatively to one another, in a direction parallel to XX. Displace the dotted path through a distance equal to PQ, parallel to XX, in the reverse direction to the original displacement. Then the two paths will be placed in the same relative position with regard to each other which they actually occupy in the mechanism, and in this position the distance between each pair of corresponding points on the paths is constant, and equal to PQ, the length of the link

Let p, Q be a pair of corresponding points on the actual paths, and let q be the corresponding position of Q in the displaced path. Jum pq and take a point  $\iota$  so that

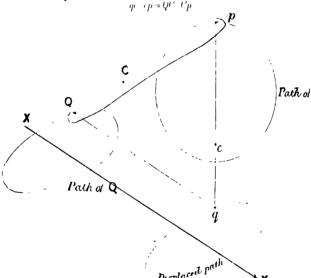


Fig. 144. Given two Displaced Paths, to find the Displaced Path of a Third Point on the Link

Then the theorem is proved if it can be shown that Ce is equal to Cp, and that Ce is parallel to XX

Since c and C divide the sides pq and pQ of the triangle pQq in the same proportion, Cc is parallel to Qq. Hence the triangles pCc and pQq are similar, and therefore, by the terms of the theorem, pQ is equal to Qq and pC is equal to Cc. Also since Cc is parallel to

Qq it is parallel to XX. Hence the theorem—It may be noticed that the theorem is equally true if the point C is taken in Qp produced. Then of course c must be taken in qp produced.

The theorem may be extended to include the case where C is taken anywhere in the link. C is then to be regarded as the apex of a triangle of which PQ is the base. The corresponding position of c in the displaced path is fixed by the apex of a triangle, whose base is pq, and which is similar to the triangle pQC.

By means of these two theorems, all the point paths required in the determination of corresponding positions of the crank and the valve may be easily found in any type of valve gent

Stating an example formally, given the dimensions of the Joy gear Fig. 145, find the 24 positions of the valve that is of the point Y, corresponding to 24 equidistant crank positions. Before proceeding to apply the method to the gear, the following templates must be prepared, the general shape being similar to the template shown in Fig. 28.

I template, 74" radius, for suppression of the connecting rod.

1 template, 20' radius, for the suppression of the rod RS

I template, 43½' radius, for the suppression of the rod YV

1 template  $20\frac{a}{16}$  radius, for the suppression of the rod VJD.

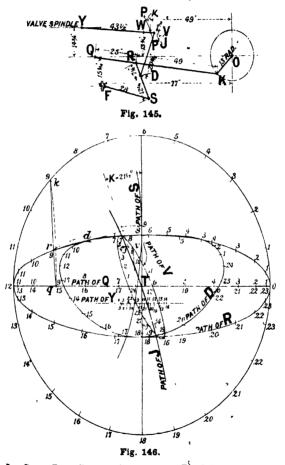
- (1) Applying the corollary to Theorem (1), displace the circular path of the crank pin a distance KR along the line of stroke, and the straight path of the crosshead a distance QR along the line of stroke. The whole relative displacement in the direction of the line of stroke is thus equal to 74%, the length of the connecting rod, and the path of Q therefore becomes the diameter of the crank pin eight which coincides with the line of stroke produced, as indicated in Fig. 146. Divide the circle into 24 equidistant crank positions, and project them by the proper curved template on to the path of Q. Thus, point k is shown projected to point q by the dotted curve.
- (2) Apply Theorem (2) to find the path of R. Consider the crank position No. 9, and lettered k. Join k to the corresponding position of g, and take the point r so that

$$kr \cdot rq = KR \cdot RQ = 49 \cdot 25$$

Then r is a point on the path of R. Repeat the construction for correspondingly numbered points, and sketch in the path of R.

(3) Now fix the attention upon the link RDS. The path of R is known and also the 24 points on it corresponding to the 24 equilistant crank positions. It is required to find the

corresponding series of points on the path of S. Applying Theorem (1), displace the path of S vertically through a distance equal to SR. It a vertical line be drawn through the fixed point F, Fig. 145, and a point f be taken above it, so that Ff is equal to the length



Joy Gear. Point Paths of Gear shown in FG 140, the dimensions of which are given in Fig. 145.

of the link SR, an arc struck from f as centre with radius FS, will represent the path of S, displaced vertically, through a distance RS. Then with the proper template, project the 24 points from the path of R on to the path of S. The point r is shown so projected to s. (The positions of the other points on S are omitted to avoid confusion.)

(4) Apply Theorem (2) to find the path of D. Considering the pair of points r and s, corresponding to No. 9 position, join them, and take the point d so that

sd 
$$dr = SD DR = 12\frac{9}{4} + 7\frac{1}{4}$$

Then d is a point on the path of D. Repeat the construction for correspondingly numbered points and sketch in the path of D.

- (5) Consider now the link VJD. The path of D is known and 24 positions in it. The path of J is known when a particular value of  $\kappa$  is given. It is required to find the 24 positions on the path of J corresponding to the 24 positions on D, and also to find the path of V and the 24 corresponding positions in it. Applying Theorem (1), the path of J is to be displaced vertically downwards, with regard to the path of D, through a distance JD. But D has already been displaced upwards a distance DR. Therefore J must be displaced downwards through a distance  $JD DR = 13\frac{5}{10}\%$ , thus bringing the centre W on to the centre of the circle. Let  $\kappa = 21\frac{1}{2}\%$ . Then, draw the path as indicated and using the proper template, project the numbered points on the path of D to the path of J. The point d is shown so projected to J.
- (6) Apply Theorem (2) to find the path of V. Considering one pair of points d and j, produce the line dj to v, taking v so that

$$d_{I} \ jv = DJ \ JV = 20 \frac{9}{16}'' \ 215''$$

Repeat the process for correspondingly numbered points and sketch in the path of V.

(7) Since the path of V has been displaced vertically downwards through a distance  $DV - RD - 16\frac{1}{4}$  inches, the path of V has come down with it through the same vertical distance, consequently the path of V is  $1\frac{1}{4}$  inches below the centre line. Now, applying Theorem (1), displace the path of V horizontally through a distance equal to V, and using the proper template project the 24 positions from the path of V on to it. The point v is shown so projected.

Thus, 24 positions of the valve are known for 24 equidistant crank angles, and therefore the corresponding displacement curve can at once be set out.

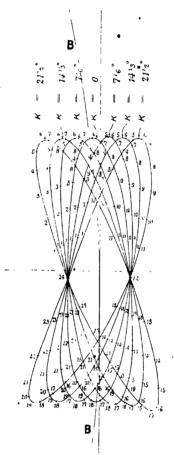


Fig. 147. JOY GEAR. PATHS OF POINT, V. FIG. 145.

A somewhat more convenient way of getting the positions of Y, from the path of V, is to draw an arc, with radius YV, through the point T, constructing what is called a "big end base" in Article 37.

Then, the horizontal distance between any point on the path of V and this are, is the corresponding displacement of the valve

Fig. 147 shows the paths of V corresponding to the values of  $\kappa$  already specified. The arc BB represents the "lig end base," so that the horizontal distance from this curve to any of the numbered points on the paths gives at once the displacement of the valve for the value of  $\kappa$  to which the path corresponds, when the crank occupies the correspondingly numbered position

128. Joy gear continued. Approximate theory. Fig. 145 Neglecting the obliquity of the connecting rod, the horizontal displacement from the central position of every point on the rod is given by

This is therefore the horizontal displacement of the point R from its central position

Again, the point S may be assumed to move in a vertical straight line without introducing sensible error, so that the horizontal displacement of the point R from its central position multiplied by the ratio DS—RS, is the horizontal displacement of D

The lever DJV reduces the horizontal displacement of D in the ratio VJ JD, so that finally, the horizontal displacement of V from its central position, when the path PP is vertical, is given approximately by

The minus sign is prefixed because an inspection of the diawing of the gear will show that the displacement is 180 degrees from angular agreement with the ciank. This represents the 180 degree component of the motion of the valve in terms of the ciank angle  $\theta$ , and it is the actual motion when the path is vertical, that is to say, when the motion is put in mid-gear

The magnitude of the 90 degree component depends upon the movement of J above and below the centre W, of the path PP. With proper proportions of the links, the mid-position of this vertical displacement is as nearly as possible at the point W. The actual vertical distance of the point R above or below the line of stroke of the piston for a given value of the crank angle  $\theta$  is

$$\frac{QR}{QK} \times QK \sin \theta,$$

and neglecting the obliquity of the rod DJ, this also gives the approximate vertical displacement of the point J, from its central position W.

When the path PP is inclined to the vertical & degrees, the horizontal projection of the displacement, on a horizontal fine through  $J_{\rm r}$  is therefore approximately

$$\frac{QR}{QK} \times OK \sin \theta \times \tan \kappa \dots (2).$$

The actual magnitude of the projection is increased in the ratio  $VD \cdot JD$  because so far as this component is concerned the, lever VJDis turning about the fulcrum D. Hence the whole displacement x is given approximately by

$$x = -\frac{VJ \times DS \times OK}{JD \times RS} \cos \theta \mp \frac{VD \times QR \times OK}{JD \times QK} \tan \kappa \sin \theta \dots (3).$$

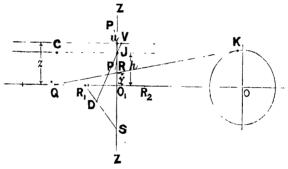


Fig. 148. Joy GEAR

The minus sign before the second term is to be used when the path is inclined to the left of the vertical through W, and the plus sign when it is inclined to the right. The former position corresponds to forward gear. Hence for the Joy gear

$$A = -\frac{VJ \times DS \times OK}{JD \times RS} \qquad (4)$$

and

$$A = -\frac{VJ \times DS \times OK}{JD \times RS} \qquad .....(4)$$

$$B = \mp \frac{VD \times QR \times OK}{JD \times QK} \tan \kappa \qquad ..... \qquad .....(5).$$

Using the dimensions of the Lancashire and Yorkshire year shown in Fig. 145, the expression reduces to

$$x = -1.184 \cos \theta - 5.019 \tan \kappa \sin \theta$$
.....(6).

Giving  $\kappa$  the value 21 degrees, corresponding to full gear, the expression becomes

$$x = -1.184 \cos \theta - 1.97 \sin \theta$$
 .......(7).

When  $\kappa = 0$ , the mid-gear condition,

The curves corresponding to the equations (7) and (8) are shown by chain dots on the valve diagram, Fig. 142. Comparing these with the actual curves they purport to represent, the extent to which the approximate theory is useful may be estimated.

- 129 Design of the Joy gear. The actual design of a gear is somewhat tentative, but the following method will probably be found useful.
  - (1) Find the equivalent eccentric for the cut off, maximum opening, and lead desired, and calculate the values of A and B
  - (2) Set off, anywhere along the line of stroke, a distance  $R_1R_4$ , Fig. 148, equal to the stroke of the piston. Bisect  $R_1R_2$  in  $\theta_1$  and draw the perpendicular  $\theta_1Z$ . Choose a length  $R_1S$  so that the angle  $R_1S\theta_1$  is less than 45 degrees.
  - (3) Draw the line of stroke of the valve CV at a distance z above the line of stroke of the piston. The distance z is settled in the design of the cylinder.
  - (4) The position of the point D, and the position of the fixed centre W, must now be chosen to fulfil the two conditions of Article 121, together with the condition that the horizontal motion of V, to either side of the central position, must be equal to A, the lap plus the lead

If h is the height of W above the line of stroke, and  $y_1$  is the vertical distance of R above the line of stroke when the links SR and DJV are on the line ZZ, the highest position of J above the line of stroke is

$$y_1 - RD + DJ$$
,

and the lowest position of J when the connecting rod is below the centre line is

$$-y_1 - RD + DJ$$

The mean of these two values must be equal to h, if the second condition of Atticle 121 is to be fulfilled, that is

$$b = DI - DR$$

Other equations may be formed, which, combined with the conditions already stated, enable the position of D to be found by calculation, but the expressions become so complicated that they are not of much practical use

The most convenient way to find D, and at the same time h, so that all the conditions are satisfied, is by the following tentative graphical method. First, set out a distance nV, equal to A, the lap plus the lead, on one or other side of the vertical ZZ, and on the line of stroke of the valve. Then, draw RS in the position corresponding to  $\theta = 0$  or 180 degrees, take any point D on the link  $R_1S$  and join it to V, cutting the vertical ZZ in the point J, thus fixing some value of h. Then try if  $DJ - DR_1 = h$ . After a few trials a position of D will be found which does satisfy this condition, fixing thereby the proper value of h and the position of the fixed axis W, which of course in the position of the gear used to find D, is concident with J

Then, not only does this position of D satisfy the second condition of Article 121, but it satisfies the other conditions also, so that the fixing of D is really a crucial point in the design of the gean.

(5) Calculate y, the maximum vertical distance of the joint R of the connecting rod above the line of stroke from

$$y = \frac{B}{\tan \kappa} + \frac{JD}{VD}$$

B is known from (1). A value of  $\kappa$  is chosen. And the ratio JD to VD is known from (4).

(6) Calculate the distance QR from the relation

$$QR = \frac{g \times QK}{OK}$$

in which OK is the crunk radius and QK is the length of the connecting rod. This fixes the position of the vertical ZZ in relation to the crank shaft because the dead points are at the distances QR measured to the left of  $R_{\pm}$  and  $R_{\pm}$  respectively.

(7) The point J represents, and coincides with, the fixed axis W, Fig. 145, of the path PP. Select some suitable value for the length of the valve rod VY, draw a line through J. Fig. 148, parallel to the line of stroke of the valve, and from a centre C in this line and with radius VY, draw an arc through J. This arc is the mid-gear position of the centre of the radius link guiding J, when the gear is arranged as shown in Fig. 141.

A gear set out in this way will give approximately the distribution

fixed upon and the leads for both strokes will be constant. What the actual distribution will be can only be found by drawing the actual displacement curves.

If found more convenient the link RS may be replaced by a link RD, the point D being connected to a return crank on the main crank

130 Reversing by the interchange of the steam and exhaust pipes. The difference between miside and outside steam admission has already been explained in Articles 18 and 43. With outside steam admission, the eccentric sheave must have an angular advance greater than 90 degrees, with inside admission the angular lag must be less than 90 degrees. If the angular advance is less than 90 degrees in the first case and the angular lag is greater than 90 degrees in the second case the slide valve current effect a distribution of steam suitable for driving the engine

Suppose, that in an engine fitted with a slide valve of the ordinary type, and arranged for outside steam admission, the steam supply is suddenly interchanged with the exhaust, that is to say, steam is conveyed from the engine by the steam pipe and conveyed to the engine through the exhaust pipe. What would happen? If the angular advance of the eccentric sheave were greater than 90 degrees the effect of the change would be to stop the engine because after the change the angular advince would become an angular lag greater than 90 degrees, so that the engine would not run. If however the angular advance were just 90 degrees (the valve having therefore no steam lap and no lead being possible) the interchange converts the 90 degrees angular advance into 90 degrees angular lag. The engine would therefore run in the opposite direction on the admission of steam through the exhaust pipe. In neither case however would the engine be able to use steam expansively, and this is the price which must be paid for the convenience of the method.

Thus, providing that the angular advance of the eccentric sheave is made 90 degrees an engine may be reversed by simply admitting steam through the exhaust pipe and exhausting through the steam pipe. The design of the valve must be such as will allow of this change, because with inside steam admission the pressure tends to lift the valve off the face, the form of the valve must be modified accordingly. In order to interchange the functions of the two pipes they must be connected to a controlling valve, itself designed on the same principle as a slide valve. The arrangement is diagrammatically illustrated in Fig. 149. The ends of the two pipes, A and B, are brought together in the casing of the controlling valve, and formed into steam

ports, a and b, precisely as in the valve chest of a steam engine. Lying between these ports is an exhaust passage E, leading directly into the exhaust pipe. Steam is brought to the controlling valve casing through the pipe S, and a slide valve C, of the usual type, is placed over the ports. When the valve C is moved downwards, the bottom port b, and therefore the pipe B leading to the central port of the cylinder, is placed in communication with the exhaust pipe E, whilst at the same time the pipe A is in direct communication with the steam in the controlling valve casing through the open port a.

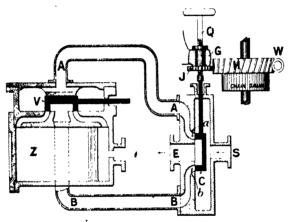


Fig. 149. RIVERSAL BY INTERCHANGE OF THE STEAM AND EXHAUST PIPES DIAGRAM OF SILAM CONNECTIONS IN COMMINATION WITH "HUNTING GEAR"

With the controlling valve in this position the engine, therefore runs with outside steam admission and turns so that the eccentric sheave is in front of the crank.

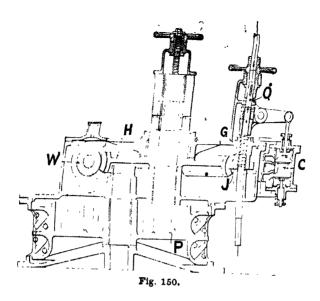
Suppose now, that the controlling valve is moved up; the pipe A is placed in communication with the exhaust port E, and a way for the steam supply is opened through the port b, and the pipe B, into the inside of the slide valve V. The engine will therefore, inn in a direction where the eccentric sheave is behind the crank, being in fact reversed. Hence the engine can be reversed by merely moving the valve C up or down.

131. Steam steering gear. The combination of a "hunting gear" with this arrangement results in a useful and convenient mechanism,

a mechanism which is to be found on almost every ship, namely the steam steering gear. In the ordinary hand steering gear, a definite angular position of the rudder corresponds to a definite angular position of the steering wheel. The object of the steam steering gear is to interpose between the wheel and the rudder a motor, or mechanism, which will do the actual work of changing the rudder's position without breaking the geometrical relation between the wheel and the rudder, Consequently the man at the wheel has merely to carry out the steering operation as if no engine existed, with this difference however, that he can steer the largest ship with as much case as he can steer the smallest boat, because between him and the rudder is a steam engine so connected up that it is obedient to the slightest turn of the wheel. It works whilst the wheel is being turned, it stops when the wheel stops, and starts only when the wholl starts to be turned. In fact it follows faithfully every motion of the steering which seeningly always on the lookout to save the muscles of the steersman. Quite a small steering wheel is sufficient to steer with in this case, because all the work the steersman has to do is to overcome the slight friction of certain mechanism connected with the gear

The combination is shown in diagrammatic form in Fig. 149. The tiller chains are wound on the drum  $H_i$  and this has a worm wheel mounted with it, the worm wheel being driven by the worm W, which is connected directly or indirectly with the crank shaft of the engine belonging to the cylinder Z. Gearing with the wheel H, is a small wheel J, which forms part of a sleeve free to rotate in the fixed bearing G. The spindle Q, operating the controlling valve C, passes through this sleeve, engaging with it by means of a sorew thread. J is in fact a nut to the spindle Q. When the nut J is at rest, a slight turn of the spindle Q moves the valve up or down and starts the engine in one direction or the other. Immediately the engine starts, however, the nut J begins to rotate, and in so doing brings the valve C back to its central position, and unless the spindle Q is turned at exactly the same rate by hand, as the nut J is turned by the engine, thus holding the valve C open, the engine will stop. In an actual steering gear the spindle Q is carried up and, by means of bevel gearing, brought on to the bridge in a position which allows the small strong wheel to be fixed in the usual fashion, namely, so that it turns about a horizontal axis

Figs. 150 and 131 show a half sectional plan and half sectional elevation, of a steering engine made by Messis Alley and Maclellan Sentinel Works, Polinadic, Glisgow, who have kindly allowed the gear to be illustrated. The figures are lettered similarly with Fig. 149. In



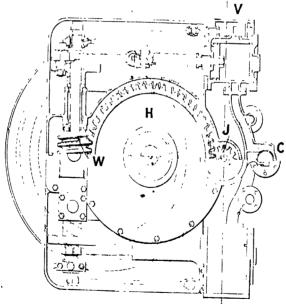


Fig. 151. Steam Steering Gear

this case the slide valve V, of the steam engine, takes the form of the main valve of a Meyer valve gear, and the steam ports are brought out to the side of the steam chest. There is apparently only one pipe between the controlling valve and the steam chest, but this pipe is divided into separate passage ways corresponding to A and B of Fig 149, and also contains the steam passage S and the exhaust passage E, the flanges for the connection of the steam and exhaust pipes being seen in the figure. The controlling valve C, Fig 150, is made in the form of a piston valve. The hunting gear is clearly shown in the figure, the valve C being connected indirectly to the spindle Q through a rocking lever. In this illustration the chain dum is not formed with the worm wheel H but is grared to it through the pinnon P

Crank angles from which an engine cannot be When the stop valve is opened and steam is admitted to started. the steam chest of an engine which is at rest, it does not follow thatthe engine will start. The crink may have stopped in a position where the slide valve has cut off steam in which case no steam can get to either end of the cylinder since the valve covers both steam ports. Consider first the case of a single evhilder engine. Let OCFig. 152 be the crank position at cut off, and OA the crank position at admission. Whilst the crank turns through the angle COA, the slide valve completely covers the steam ports and no steam can get into the cylinder. Hence if the engine should stop with the crank anywhere within the angle COA, the mere opening of the stop valve will not start the engine Further when steam is admitted at the crank position OA, the piston cannot evert an effective turning moment on the crank shaft in the positive direction, until the crank has passed through the 180 degree dead point to a position OB, where the torone due to the pressure on the piston it just greater than the torque resisting motion at the crank shaft. Ict M be the torque at the crank shaft against which the engine is required to start, F the force along the connecting rod due to the steam pressure, i the crank radius, then, neglecting the obliquity of the ninceting rod the turning moment exerted by  $\Gamma$  on the crank is,  $\Gamma_{\ell} \sin \theta$  and therefore at starting

 $F_I \le n \theta = M$ .

from which the value of sin  $\theta$  can be found when F and M are given. Hence, if the crank should happen to stop anywhere in the shaded angular region  $COB_{\bullet}$  the engine will not start when steam is turned on. The same considerations apply to the other cycle, so that  $C_1OB_1$  is a second angular region from which the crank will not start. The diagram therefore shows that the crank must be brought to rest

somewhere in the unshaded regions, if the engine is to start when the stop valve is opened. Large, single cylindered, engines are provided with a barring gear, so that the engine crank can be turned into a starting position. In some types of barring gear steam is turned into the main engine, and into the small engine operating the gear, simultaneously. If the crank is in a non-starting position, the engine is driven round by the barring engine, which usually operates by a spur pinion in a large spur wheel incorporated with, and forming part of, the flywheel, until at a favourable crank position the main engine begins to drive the barring engine, but directly this happens the barring engine falls out of gear automatically.

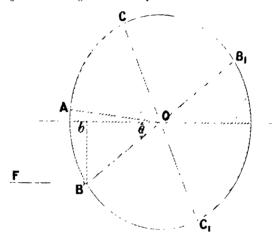


Fig. 152. "Non Starting" Crank Anglis

If the valve is set to give an early cut off it will be perceived from Fig. 152, that the shaded area will be enlarged, and the unshaded area reduced, in angular dimensions, so that the range of crank positions from which the engine can be started by the admission of steam to the steam chest is reduced.

If the engine has two cranks at right angles, if the one stops in a non-starting region, the other generally stops in a starting position, though not always. This is an important question in connection with locomotives. Locomotives always have to be started with a load on them, and they must of course be able to start with the full load, from rest, on the steepest gradient over which they are required to work.

In these circumstances the angle  $\theta$  may be so large that the angle COB becomes greater than a right angle. If this should happen, both cranks may come to rest within the shaded area and then the engine would not start. Fortunately, the shaded areas for the opposite direction of running occupy different angular positions on the diagram to those shown in Fig 152, so that if the engine is reversed, the effect is to bring one of the cranks into a starting region. This point may be illustrated by an actual example in connection with the valve diagram. Fig. 86 By measurement from the diagram the following results are obtained.—

Fore gear (positive i station of crank)		Crank angle
Instroke cycle - Cut off		124 degrees.
Outstroke cycle - Cut off		298 degrees
Back gear (ne ative rotation of crank)		
Instroke cycle Cut off		= 121 degrees
Outstroke cycle   Cut off		297 degrees

The minus sign prefixed to the crank angles of the backgear, means, that the angle is to be measured out from the initial line in the clockwise direction.

Conlining our attention at first to the fore gear positions set out, Fig. 153,  $\partial C$  at 124 degrees with the initial line, and  $\partial C_1$  at 298 degrees, both being measured out of course in the counter clockwise direction. The position of  $\partial B$  is not easy to find. It may however be calculated approximately in the following way. The turning moment at the crank axis which must be overcome before the engine will start, is equal to the total train resistance, multiplied into the radius of the driving wheel. The total train resistance is made up of several factors. These are, the train resistance from rest, the engine and tender resistance from rest, the resistance from rest, the engine and tender a resistance due to a curve. Suppose the total train and engine resistance to be f pounds per ton. Then the steating resistance from this cause will be  $W_f$  pounds W being the gross weight in tons of the train including engine and tender. If the incline is 1 in  $G_t$  the resistance in points, due to it is

$$W\times 2240$$

Hence, the total resistance, neglecting the curve resistance is equal to the sum of these two quantities, and if R is the radius of the driving wheel, the torque which has to be overcome to start the train is

$$RW\left(f + \frac{2240}{G}\right) - M$$

If p is the maximum steam pressure, and A the area of the cylinder in square inches, F, the force along the rod, is pA lbs. The starting condition is then expressed by

 $pAr\sin\theta=M,$ 

from which

$$\sin\theta = \frac{RW\left(f + \frac{2240}{G}\right)}{pAr}.$$

By way of example suppose the total weight of engine, tender and train to be 350 tons, and that the average starting resistance is 15 lbs. per ton. Let the train be standing on a gradient of 1 in 230, and suppose the engine cylinders are 18 inches diameter and 24 inches stroke, the steam pressure being 160 lbs per square inch. Also let the diameter of the driving wheels be 7 feet. Substituting these values in the above equation it reduces to

 $\sin\theta=0.655,$ 

from which  $\theta = 40$  degrees.

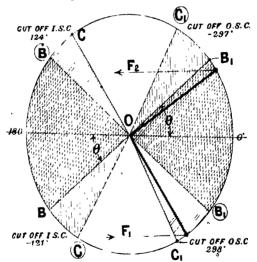


Fig. 153. Non-Starting Crank Angles with two Cranks at 90 engless. "

In Fig 153 OB is set out at 40 degrees below the 180 degree dead point position, and  $OB_1$  40 degrees above the 0 degree dead point

position, thus marking off the two angular non-starting spaces COB, and  $C_1OB_1$ , for the instroke and outstroke cycles respectively. In each case the angle is greater than 90 degrees and therefore the cranks may come to rest in a position where it is impossible to start the engine. The thick line represents one of these positions where the cranks have stopped in the outstroke cycle region

These non-starting areas are cross-hatched with lines sloping at 45 degrees

The lines  $O\bigcirc$  and  $O\bigcirc$  represent respectively the crank positions for cut off when the engine is reversed,  $O\bigcirc$  and  $O\bigcirc$  being the positions of the crank where the connecting rod can excit the necessary starting couple. The non-starting areas corresponding to these crank positions are cross-hatched with vertical lines.

It will be seen at once from this diagram that if the cranks stop in the position shown by the thick lines, the effect of reversing the engine is to bring the lower crank into a starting region, the upper crank however still remaining in a non-starting region

In practice the effect of the draw-bar springs is to modify the angular dimensions of the diagram in favour of casier starting

In compound engines, boiler steam is only admitted to the high pressure steam chest and if the valve happens to close the poins the engine cannot start. Starting valves have therefore to be fitted either to admit steam directly to the other cylinders or to the receivers between the cylinders. The steam in a receiver, for certain crank positions, is in communication, through the respective valves with two pistons, and if acting to drive the larger, appears as a back pressure on the smaller. The actual effect is therefore that due to the receiver pressure, multiplied into the difference of the areas of the two pistons between which the receiver lies. There is no difficulty in starting marine engines under these conditions, because they never have to start under a full load. But with locomotives the case is entirely different. They must start under full load and must start promptly. When compound locomotives were first introduced into this country the starting difficulty at once forced itself to the front.

One example may be given. Fig. 154 shows a diagrammatic section through the cylinders and starting valve of a Worsdell and con Bornes two cylinder compound locomotive. The high pressure crank is supposed to have come to rest in such a non-starting position, that the high pressure slide valve covers both steam ports, but is open to the exhaust port. Hence, when the regulator is opened, no steam can get into the cylinder. In these circumstances, a small valve A is opened by the driver and steam makes its way, through the reducing valve D, to the

steam chest of the low pressure cylinder, and, assuming the low pre-sure crank to be in a starting position, and therefore one of the steam ports open, the steam will find its way into the cylinder and start the engine from the low pressure crank alone. To prevent the steam acting as back pressure on the high pressure piston, the valve E is closed, by the piston C, immediately the valve A is opened. Very soon after the

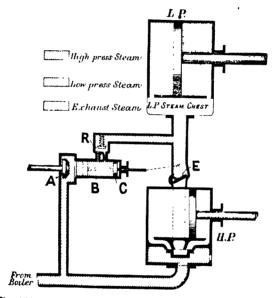


Fig. 154. Diagram of Catinders, Sham Connictions, and Starting Value Worsdell and von Borries Two Catinder Compound Locomotive.

engine moves, steam is admitted to the high pressure cylinder, and when release takes place, the steam, which at release is at a higher pressure than the steam in the receiver pipe, forces open the valve E on its way to the low pressure cylinder, thereby pushing the piston C back to the dotted position R, and thus cuts off the steam to the low pressure cylinder automatically.

The actual arrangement of starting and intercepting valves is shown in Fig. 155.

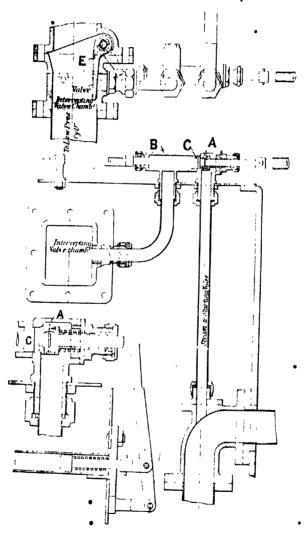


Fig. 155. Delails corresponding to Fig. 154.

If it should happen that the low pressure crank stops in a nonstarting position as well as the high pressure crank, then the engine must be reversed, so that one or other crank is in a starting position for backward running, it the high pressure, the engine will start when the regulator is opened, if the low pressure the starting valve must be opened as well as the regulator.

For further remarks regarding the starting of compound locomotives, see an article by the author, "The development of Compound Locomotives in England," Engineering Magazine, Sept. and Oct., 1904.

## CHAPTER IX.

STATICAL AND DYNAMICAL PROBLEMS IN CONNECTION WITH THE DESIGN OF A VALVE GEAR.

The general problem. After the centre lines of a genr have been found so that the valve may effect the distribution of steam desired, various problems in connection with the mechanical design of the gear have to be solved. The first of these is to design the size of all the pins and joints so that the gear shall run cool, and the second is the design of the several links so that there shall be no danger of breakdown Both these problems involve an estimate of the maximum forces which are likely to come on the joints and the loads which the links have to transmit from one to the other This estimate is generally based upon some calculated value of the force required to overcome the resistance of the steam valve to motion, connection with slide valve friction have been cited in Chapter II. When designing the gear, the whole unbalanced surface exposed to the action of the steam should be multiplied into the maximum boiler pressure to get the force producing frictional resistance between the surfaces of the valves and the ports, and this should be multiplied by a suitable coefficient of friction to find the naximum frictional resistance of the valve, to be used in the design. Assuming this force to be known, the problem resolves itself into the determination of the loads on the joints of the valve gear when the force acting along the valve spindle is given and the point is specified at which the gear is driven.

But now a complicated question locus in view. When the engine is working so slowly that the acceleration of the motion of the various links forming the genr is small, the forces acting at the joints of the links are not sensibly different from those due to the overcoming of the force at the valve spindle. The problem in this case is merely a static one and the solution is straightforward and simple.

As the speed of the engine increases, the forces which must act on the several links to accelerate their motion increase sapidly from negligible amounts, to magnitudes which render it imperative to consider them. At high speeds, in fact, these accelerating forces are of paramount importance, and many breakdowns have occurred through neglecting to take them into account. The peculiarity of this problem is that it cannot be solved directly. A preliminary design of the gear must be made based upon the forces acting due to the estimated valve resistance, and upon experience, and then each link must be weighed, and its mass centre and moment of mertia about its mass centre computed, before it is possible to find the accelerating forces. It becomes a trial and error method. The gear automatically loads itself as the speed increases, and any gear which is intended to run at high speeds, should be examined with respect to this mertia loading and the design of the links modified to meet the case. In order to fix our ideas, consider the Joy gear shown in Fig. 140. An important practical problem is to find the force acting at R, the driving point of the valve year, because this force loads the connecting rod with a transverse load. In the solution of this problem the forces at all the other joints are found incidentally. The problem therefore splits up into two separate and distinct parts, thus -

- (1) The finding of the force at the joint R of the gear when the valve spindle load is given, assuming the speed to be so slow that the mertia loading of the gear is negligible.
- (2) The finding of the force at the joint R due to the mertia loading of the gear, the weight and form of each link being assumed.

The actual force, corresponding to a given speed acting at any joint, is then the resultant of the forces due to (1) and (2), but as will be seen further on, the effect of the valve resistance, that is (1), can be found simultaneously with the determination of the mertia forces under (2)

The problem is further complicated by the effect of friction at the joints, but, assuming proper lubrication, the disturbance produced on the forces due to this cause may be neglected. Since the force at the joint R, both in case (1) and (2) above, is in a state of continuous variation, the only way to deal with the problem is to find the force for a series of positions of the gear. Once having worked through, say 24 positions, a matter of some perseverance, not to say tediousness, knowledge will have been obtained which will ginde the judgment im subsequent cases without actually analysing them in such profusences of detail.

- 134. Given the crank angle  $\theta$ , and the force acting along the valve spindle, to find the force acting at the joint R of a Joy gear when the inertia loading is neglected. This problem is a statical one, and requires the use of the two following statical principles for its solution -
  - (1) It a link carrying two joints is held in equilibrium by forces acting at the joints, the magnitudes of the resultants at the respective joints must be equal and opposite, and they must act along the line joining the two joints, neglecting the effect of the friction of the joints.
  - (2) If a link curving three joints is held in equilibrium by forces using at the joints, the forces must either be parallel or must meet in a point, and in each case the resultant of the three forces must be zero.

The method of applying these principles is most castly illustrated by taking an example

**Example.** Find the forces acting on the joint R of the Joy gear, illustrated in Fig. 140, for full forward g, u, the crank angle being  $\theta$  and the force acting at the valve spindle being  $P_1$ .

Draw the gear in the configuration corresponding to a crank angle  $\theta_i$  as in Fig. 156, and draw the path PP in the full forward position. Whether the force  $P_i$  required to move the valve involves a tension or compression of the valve spindle is to be found from the valve diagram, because the diagram shows which way the valve is moving for a given crank angle. For the value of  $\theta$  shown in the figure, the valve spindle is in tension, and the force  $P_1$  acts as shown at the joint Y. The problem may perhaps be made more complete as an exercise by going one step further and finding the forces  $P_1$   $P_2$  at the slide bars and crank pin respectively, which balance the action of  $P_1$ .

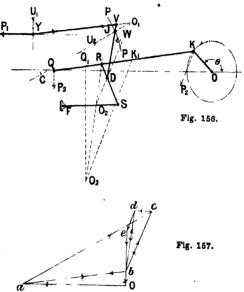
In consequence of the application of the force  $P_1$  and the balancing force acting at R, there will be the following reactions from the framework of the engine, neglecting the effect of friction -  $\sim$ 

- (1) The normal reaction of the slide at  $Y = U_4$ .
- (2) The normal reaction of the path PP, at J = U.
- (3) The reaction of the joint F, which must have the direction of the link FS by principle (1)

By principle (1), the resultant of  $P_1$  and  $U_1$  must be equal and opposite to the force at  $V_1$  and must act along  $YV_1$ . Set out Oa, Fig. 157, to represent  $P_1$  to some scale draw Ob parallel to  $U_1$  and ab parallel to  $YV_2$ . Place an arrow head on Oa, indicating the direction of  $P_1$ 's

action, and follow the direction it indicates round the triangle, in this way discovering the sense of ab and bO. Then the triangle shows that a force represented by ab acts from the joint Y along the rod YV, and a force represented by bO acts from the slide at Y, to the joint.

Again, fix the attention on the joint V. The force acting at Y is necessarily accompanied by an equal and opposite force acting at V by principle (1) Hence cross out the arrowhead on ba and place another, pointing in the opposite direction, to indicate the change of the force



JOY GEAR ILLUSTRATED IN FIGS 140 AND 142 FORCE DIAGRAM.

to ba. The link VID is held at rest by forces acting at the three points V, J, and D. Of these forces that at V is completely known, that at J is known in direction, being normal to the path PP. By principle (2) therefore, the forces through V, J and D must meet in a point. Produce the normal at J to meet the direction of YV produced, in  $O_i$  join  $O_i$  to  $D_i$  thus fixing the direction in which the force at D must act Returning to the force diagram, Fig. 157, draw de parallel to  $JO_1$ , and through the point b draw cb parallel to  $O_1D$ . Follow round the direction of the new arrow head on ba, and the

directions in which the forces must act, from without, on the link VJD, are at once shown; so that ac is the force acting from the path PP to the joint J, and cb is the force acting at the joint D, from the joint to the link DJV.

Again, the link RDS is held in equilibrium by forces at R, D and S. Of these, the force at D is known in magnitude and direction, being represented by bc, the arrow head being reversed as before, the force at S is known in direction, being along the link SF. Therefore, produce the force through D, to cut the link FS in  $O_2$ , then  $O_2$  is the point through which the three forces acting on RDS must pass. Hence join O2 to R, thus fixing the direction in which the force at R must act. Returning again to the force diagram through the point c, draw cd parallel to SF, and through the point b, draw db parallel to  $RO_2$ . Follow round the direction of the reversed arrow head on be then, cd represents the force acting from the link FS to the joint S, the direction of the arrow showing that the link is in tension for the value of  $\theta$  taken; and db shows the force acting at the joint R. For practical purposes this is the force of interest in the design of the gear, because, resolving it along and at right angles to the connecting rod, the value of the normal component is at once found, and it is this component which causes bending of the rod

Forces at Q and K are found in a similar manner, but here a point of interest arises in connection with the application of principle (2) to the connecting rod. The point at which the direction of the force through R, meets the force  $P_I$ , is practically maccessible. The difficulty is easily surmounted however, by taking  $Q_1$  and  $K_1$  conveniently near to R, so that  $Q_1RK_1$  represents the rod to a smaller scale. Then the point  $O_4$  is found for this small scale rod, and  $O_4K_1$  is the direction of the force through  $K_1$ . But this must also be the direction of the force through K, since the mere alteration of the scale cannot affect the direction of the forces. Hence a line parallel to  $O_4K_1$  drawn through K, gives the direction required. In the force diagram, Fig. 157, the triangle bde corresponds to these directions.

The scale of the force diagram is fixed when an actual value is assigned to  $P_1$ , because this fixes the number of units in the line Oa of the diagram. The maximum value  $P_1$  is likely to assume for any given crank angle, can generally be estimated with fair accuracy, care being taken to make the estimate err on the right side. Examples of the value of  $P_1$  have been cited in the case of a locomotive in Article 24.

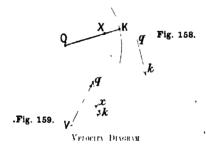
If a diagram like Fig. 157 be drawn for 24 positions of the crank, the varying values assumed by the different forces can easily be followed and the maximum value found in each case.

135. Given the speed of the crank shaft and the instantaneous value of the crank angle  $\theta$ , to find the force at the joint R, Fig. 156, due to the inertia loading of the valve gear. In solving this problem it is convenient to draw, first, a velocity diagram from which the magnitude of the velocity of any point in the gear can be scaled off. Scrondly, an acceleration diagram from which the acceleration of any point in the gear can be scaled off. From these diagrams, and the application of certain dynamical principles which will be explained in due course, the required force can be found.

## 136 To draw a velocity diagram for a given mechanism. The drawing of a velocity diagram for a mechanism depends upon a kinematic principle concerning the motion of a rigid body in a plane, which may be thus stated.—

If a link QK, Fig. 158, has motion in its own plane, and the velocity of any point in it, as Q, be given in direction and magnitude, then, the velocity of any other point K on the link is the vector sum of the velocity of Q and the tangential velocity of K turning about a line through Q, at right angles to the plane of motion as axis

Take any origin V and let the vector Vq Fig. 159 represent the velocity of Q. Then, a line drawn at right angles to the line joining Q and K must represent the direction of the tangential velocity of K turning about Q as axis. Let qk indicate the velocity's magnitude and way of action, then Vk the vector sum of the velocity of Q and the tangential velocity of K about Q, is the velocity of K.



For whether the point Q is moving or is at rest, the only motion which

. \* The method of drawing velocity and acceleration diagrams used in this and in the following articles is that given by Prof. R. H. Smith in *Graphics*, published by Longmans, Green and Co., and originally communicated to the Royal Society of Edinburgh in 1885.

K can have relatively to it is one at right angles to QK, since the line joining K and Q is supposed to be unalterable in length. If there is no turning about Q, every point in the bar moves in a parallel path, and the translational velocity impressed on Q is common to every point in the body. Hence, when there is turning in addition, the velocity of K is compounded of the common translational velocity Vq, and the tangential velocity about Q

If  $\omega$  is the angular velocity of QK, the magnitude of the tangential velocity of K about Q as axis is

$$\omega \times QK - qk$$

$$\omega = \frac{qk}{QK}$$

Hence

So that when the velocity triangle  $\Gamma q k$  is once found, the angular velocity of the link can be deduced from it by the above relation, if it is not already known.

There is a further property of the avology triangle which is useful

If points  $X_i$  as a tale in dividing the link QK in Fig. 158, and the tangential velocity qk in Fig. 159, respectively in the same proportion, then Vi represents the velocity of the point X in magnitude and direction

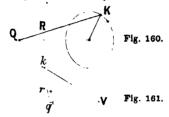
Because, applying the previous proposition, the velocity of X is the vector sum of the velocity of Q and the tangential velocity of X about Q. That is the vector sum of Vq and  $\omega = QX$ , in a direction at right angles to QX.

Therefore the lines representing the remonstral velocities of K and X must be in the proportion of QX/QK. Thus, qx represents the tangential velocity of X about Q and therefore Vx represents the velocity of X. In the application of these principles to mechanisms, the problem is reduced to the drawing of the velocity triangle for each link of a mechanism. Since each joint of a mechanism is common to two links, adjacent links will have a common ade in their respective velocity triangles, and it will be found that the velocity diagram of a chain of links consists of a series of lines rediating from a point, giving the velocities of the points of the various links, the lines joining the ends of these lines being the respective tangentral velocities.

It frequently happens that of the six elements in the drawing of the velocity triangle of a link, four of which must be given, the magnitude and the direction of one side is given completely, that is the velocity of one point in the link is completely stated, and the directions of the remaining two sides are given. The direction of the tangential velocity is always known directly the position of the link is given, since it is always at right angles to the link

137. Example. Apply this to the simple case of a crank and connecting rod, Fig. 160, to find the velocity of Q, the crosshead, the velocity of H, the crank pin, being supposed given.

Take any point V, Fig. 161, and draw Vk in the direction of the velocity of K, which will be at right angles to the crank. From V, draw Vq parallel to the direction in which Q moves, that is parallel to the line of stroke. The remaining side of the triangle must be at right angles to the rod. Draw kq, therefore, at right angles to the connecting rod, thus fixing the point q - Vq now represents the velocity of the crosshead Q to the same scale that Vk represents the velocity of the crank pin K. Let K be any point on the connecting rod. Divide qk in r so that QR, RK = qr - rk. Then Vr represents the velocity of the



VILOCITY DIAGRAM. CRANK AND CONNECTING ROD.

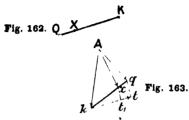
point R in magnitude and direction. Since qk may be looked upon as a scale drawing of the rod always at right angles to the actual position the rod occupies, it has been called the **velocity image of the rod**. The line joining any point on the image to the pole V, represents the velocity of the corresponding point in the actual link, in magnitude and direction.

138. To draw an acceleration diagram for a given mechanism. The drawing of this diagram depends upon a kinematical principle regarding motion in a plane which may be thus stated —

If a link QK, Fig. 162, has motion in its C in plane, and the acceleration of any point K in it be given magnitude and direction, the acceleration of any other points of the acceleration of K, the radial acceleration of Q about K as axis, and the tangential acceleration of Q about K as axis.

Thus, if the vector Ak, A being an origin taken anywhere, represents the acceleration of the point K, then kt, representing the radial acceleration of Q about K, must be drawn parallel to QK, from Q towards K, and tq, representing the tangential acceleration of Q about

K, must be drawn at right angles to QK. Assuming the magnitudes of kt and tq to be known, the sum of these three vectors is Aq, and this is the acceleration of the point Q.



Acceleration Discress

It will be observed that the directions of the radial and tangential accelerations are known directly the position of the link is known. With regard to their magnitudes the magnitude of the radial acceleration is expressed by

wheing the velocity of the point Q about the axis K. This velocity can always be found from the velocity diagram, it is represented in the case of Fig. 161 by the line qk. If  $\hat{\omega}$  is the angular acceleration of the link,

$$\omega \times KQ$$

is the tangential acceleration of the point Q about K. In general this angular acceleration is unknown in magnitude, and it becomes part of the problem to determine it. It will be observed, that the acceleration of the link is determined by the drawing of a four sided figure, so that enough data must be given to settle the value of all but two of the quantities concerned in the setting out of the figure

It is also important to notice that if the acceleration quadrilateral is obtained, the angular acceleration of the link it corresponds to can always be found from the magnitude of the tangential acceleration. Thus, if tq represent the tangential acceleration,

$$\dot{\omega}$$
, the angular acceleration of the link =  $\frac{tq}{KQ}$  .

A second proposition with regard to the diagram is -

If points X and x are taken, dividing the link QK and the whole acceleration of Q about K, namely qk, in the same ratio, then Ax represents the acceleration of the point X, in magnitude and direction.

Referring to the Fig. 163, draw xt, parallel to qt. Then if \omega and \omega are respectively the angular velocity and the angular acceleration of the Link,

the radial – acceleration of X about K is,  $\omega^2 KX$ , the angular acceleration of X about K is,  $\omega KX$ .

Therefore in the acceleration diagram the bases respectively representing these quantities will be respectively proportional to KX, whilst the lines respectively representing the radial and tangential accelerations of Q about K will be proportional to KQ. Therefore in the diagram the condition must be satisfied.

$$kt \cdot kt_1 = tq \cdot t_1x - KQ \cdot KX$$

Hence x divides qk in the same ratio that X divides KQ.

The drawing of the acceleration diagram for an ordinary fourbar chain well illustrates the application of the method in general, and in particular illustrates the construction which has to be applied successively to the links to find the acceleration diagram for a Joy gear.

139. To draw the acceleration diagram of a four-bar chain for a given configuration. Let B, C, D, E Fig. 164, be a four-bar chain, the link DB being fixed, and assume the crank BC to revolve with uniform angular velocity  $\omega$ 

It is first necessary to draw the velocity diagram. The velocity of the point C is  $\omega BC$ . Let this be represented in magnitude and direction by the vector Vc, Fig. 165, V being any origin. Vc is drawn at right angles to the crank BC, and its length to scale is equal to  $\omega BC$ .

The tangential velocity of the point E, about C as axis, is in a direction at right angles to the link CE, and the direction of its actual velocity is at right angles to the link DE. Accordingly, complete the velocity diagram by diagonal lines ce and Ve at right angles respectively to the links CE and DE. The intersection at e then defines the magnitude of the velocity of E and its tangential velocity about C.

Measuring these velocities to scale the radial acceleration of E about C is

$$\frac{ce^2}{CE}$$
 , in the direction  $EC_t$ 

and the radial acceleration of E about D is

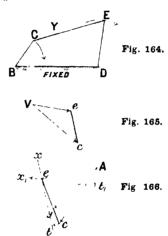
$$\frac{Ve^2}{DE}$$
, in the direction  $ED$ .

The acceleration diagram may now easily be drawn. Take any origin A, Fig. 166, and remembering that the acceleration of E, about C, is the

D. V.

vector sum of the acceleration of C, the radial acceleration of E about C, and the tangential acceleration of E about C, and also that since BC revolves uniformly in a circle the acceleration of C is  $\omega^{\bullet}CB$ , in the direction CB:—

Set out, Fig. 166, Ac equal to  $\omega \cdot CB$  in a direction parallel to CB, to represent the acceleration of C and C equal to the radial acceleration of E about C, the magnitude of which has just been found, in a direction parallel to EC, tx, at right angles to CE, giving the direction of the tangential acceleration of E about C, its magnitude being unknown.



FOURBAR CHAIN VELOCITY AND ACCHERATION DIAGRAMS

Again, consider that the point E belongs to the link ED. Its acceleration is the vector sum of the acceleration of D, which is zero, the radial acceleration of E about D, which has just been found, and the tangential acceleration of E about D which is known in direction only. Starting from the origin A, therefore, set out  $At_i$  parallel to ED to represent the radial acceleration of E about D, and  $t_i x_i$  at right angles to ED giving thereby the direction of the tangential acceleration of E about D. The intersection e of these two lines defines the respective magnitudes of the tangential accelerations of E about E. Hence E is the acceleration of the point E. Also E is the acceleration image of the link E. Thus if the points E and E divide the link E and the

image ce in the same ratio, Ay is the acceleration of the point Y. The acceleration of every point in the mechanism may therefore be found from the acceleration diagram.

140. To draw the acceleration diagram for the Joy gear shown in Figs. 140 and 142, and re-drawn in the configuration corresponding with the crank angle  $\theta$ , the crank being assumed to rotate with uniform angular velocity, and the path PP being in the position for full forward gear. Assume the linear velocity of the crank pin to be one foot per second.

It is first necessary to draw the velocity diagram. Take any pole V, Fig. 168, and draw Vk to represent the velocity of the crank pin  $K_2$ , Fig. 167. Draw Vq parallel to the line of stroke, and draw kq at right angles to the connecting rod KQ. Then kq is a small scale drawing of the rod. Take the point r in kq so that kr, rq = KR : RQ. Then Vr represents the velocity of the point R in magnitude and direction.

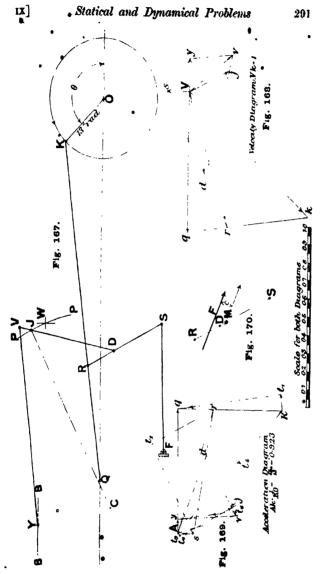
Again, consider the link RDS. The velocity of the point R is completely known, the direction of the velocity of S is known, being tangential to the path of S that is at right angles to the link FS. Hence in the velocity diagram, Fig. 168, draw Vs at right angles to FS and rs at right angles to the link RS, then Vs is the velocity diagram for the link, rs being a small scale drawing of the link. Find the point d in it so that SD/DR = sd/dr, then Vd represents the velocity of the point D.

Again, consider the link DJ. The velocity of the point D is completely known, and the direction of the velocity of the point J, which must be tangential to the path PP. Therefore in the velocity diagram, Fig. 168, draw  $V_J$  at right angles to CJ and dJ at right angles to the link DJ, then  $Vd_J$  is the velocity diagram for the link DJ. Produce dJ to v, taking v so that dJ, Jv = DJ, JV. Join Vv, then Vv represents the velocity of the point V of the link YV.

Again, considering the valve rod VY, the velocity of the point V of the link is completely known, and the direction of the velocity of Y, hence draw Vy in the velocity diagram parallel to the line of stroke of the valve and then draw vy at right angles to VY, thus fixing the velocity Vy of the point Y of the high

Hence, radiating from the point V are lines Vs, Vq, Vr, Vd, Vk, Vj, Vv, Vy representing in magnitude and direction the velocities of the several points in the gear.

The lines qk, rs, dv, ry represent the respective velocity images of the links, each image being at right angles to the position occupied by the link whose image it is.



Joy Gear (Llustmated in Figs. 140 and 142 - Velocity and Acceleration Diagrams,

Immediately the velocity of the crank pin is given, the scale of the line Vk is fixed, and the velocities of all the other points may be scaled off. In Fig. 168, the velocity of the crank pin is taken to be one foot per second

When drawing the diagram, a slide rule is of great assistance in fixing the positions of points on the images corresponding to the position of points on the actual rods. It should be understood that although qk is a scale drawing of the rod QK, and  $rs^{2}$  is a scale drawing of the rod RS, the scales are not the same. Every image has a scale of its own.

During the drawing of the acceleration diagram it will be found that the radial accelerations of the points

Q about K,

S about R,

S about F.

J about D,

J about the centre of the path PP, that is C,

Y about V

will be required

It is convenient to tabulate these quantities in the form shown in Table 11.

## TABLE 11.

Radial accelerations. Joy Gear illustrated in Figs 140 and 142

Data obtained by measurement from the velocity diagram.

The velocity of the crank pin ( $V_b$  in the diagram Fig. 168) is unity. The radial acceleration of the crank pin = 1, 1.084 = 0.923 ft per sec. per sec.

Designation of point and axis	Vector on dra gram Fig. 168 representing the velocity	May intude of velocity measured from deagrain	Radius of point Feet (See Fig. 142)	Radial acceler- ation Feet per sec per sec.
Q about $K$	kq	0.735	; 6 166	0.088
S about $R$	rs	0.834	1 66	0 419
S about $F$	$V_{\mathcal{S}}$	0 135	2 33	0 008
J about $D$	dj	0 607	1713	0 215
$oldsymbol{J}$ about $C$	l')	0.266	3 625	0 0 1 9
Y about V	vy	0 260	3 625	0.018

The figures at the third column are obtained by measurement from the velocity diagram.

The radial accelerations in the fifth column are calculated anth-metically.

The work is now a succession of problems.

(a) The acceleration of the examb pin K being given, to find the respective accelerations of the points Q and R

(This problem often appears in connection with the steam engine mechanism and there are several particular constructions which may be used for its solution)

Since the crank pin K, Fig. 167, revolves uniformly with a velocity of 1 foot per second, its acceleration is

 $rac{1}{KO}$ , in the direction KO, that is 0.923  $\Omega$  -per sec-per sec

Take any origin  $A_k$  Fig. 169 — Select any convenient scale. Set out  $Ak_k$  parallel to  $K\theta$  and equal to 0.923.

 $kt_0$ , the radial acceleration of Q about K, parallel to QK and equal to 0.088

 $t_i q$  at right angles to QK because this is the direction of the tangential acceleration of Q about K

Again, since the direction of Q's neceleration is in the line of stroke set out Aq parallel to the line of stroke intersecting the line  $t_iq$  in the point q - Aq is the acceleration of the point Q, and the line qk is the acceleration image of the red QK

Divide qk in r so that

$$kr = rg = KR - RQ$$
,

then Ar is the acceleration of the point R

(b) The acceleration of R being given, to find the respective accelerations of the points S and D

The acceleration of R is already represented in the diagram, Fig. 169, by the vector Ar. To find the acceleration of S.

Set out  $it_2$ , the radial acceleration of S about  $R_i$  parallel to SR and equal to 0.419 (see Table 11) and then draw  $t_S$  at right angles to  $SR_i$  the direction of the tangential acceleration of S about  $R_i$ .

Again, set out  $At_1$ , the radial acceleration of S about F, parallel to SF and equal to 0.008 and then draw t's at right angles to SF, this being the direction of the tangential acceleration of S about F. The intersection at s then fixes the tangential accelerations of S about R, and of S about F. The acceleration of the point S

is then represented by As, and rs is the acceleration image of the rod.

Divide rs in d so that

$$sd \cdot dr = SD : DR$$

then Ad is the acceleration of the point D.

(c) The acceleration of the point D being given, find the respective accelerations of the points J and V.

The acceleration of the point D is already represented by the line Ad on the diagram. Therefore, set out  $dt_s$ , the radial acceleration of J about D, parallel to JD and equal to 0.215 (see Table 11), and draw  $t_{sJ}$  at right angles to JD.

Again, set out  $At_i$ , the radial acceleration of J in the curved path PP of which C is the centre, parallel to JC and equal to 0.019, and draw  $t_ij$  at right angles to CJ, thus defining the point j. The acceleration of the point J is then represented by  $A_J$ , and  $d_J$  is the image of the rod.

Divide the image externally in v so that

$$dj: jv = DJ \cdot JV$$
,

then Ar is the acceleration of the point V.

(d) tirren the acceleration of the point V, find the acceleration of the point Y.

The acceleration of the point V is represented by Ar in the diagram. Therefore set out  $rt_a$ , the radial acceleration of Y about V parallel to YV and equal to 0.018, and draw  $t_ay$  at right angles to YV

Again, the direction of Y's acceleration is along the line of stroke of the valve spindle BB. Therefore draw Ay parallel to BB, thus defining the point y.

The acceleration of the point Y is then represented by Ay.

These four problems complete the drawing of the acceleration diagram. From the diagram the acceleration of every point in the goar may be obtained.

The full lines form the acceleration images of the corresponding links of the gear.

In order to fix the scale of the acceleration diagram to correspond with a given crank pin velocity it is only necessary to remember that whatever this velocity may be, v say, the line Ak in the acceleration

diagram represents the acceleration  $\frac{v^3}{k^2 U}$ . Also if the velocity of the

crank pin is variable, the vector Ak does not represent the whole acceleration of the crank pin; there is a tangential component to be added, in which case the acceleration of K is not in the direction KO. Whatever it is however, it must be given completely before the diagram can be constructed.

141. To find the angular acceleration of a link from the acceleration diagram. The angular acceleration of a link is found by dividing the tangential acceleration of any point on the link with regard to any other point on the link by the distance between the points.

The tangential acceleration is found, when the two points are specified, by locating these points on the acceleration image of the link and then drawing through them, lines respectively perpendicular and parallel to the actual link. It is of course most convenient to use the end centres of the links for this purpose. The line at right angles to the actual link represents the tangential acceleration, and the line parallel to the actual link represents the radial acceleration.

Thus in Fig 169 the tangential acceleration of the point S about the point  $R_t$  is represented by the vector  $t_2s$ . Hence the angular acceleration of the link RS is

$$\frac{t_{\mathcal{S}}}{RS}$$
 radians per section per sec

The sense of this acceleration is found by observing which way the tangential acceleration acts with regard to the centre about which it is computed. Thus in the link RS, is acts on the point S of the link diagram, Fig. 167, in such a direction that it tends to turn the link RS about the centre R in the clockwise or negative direction.

Applying this method to the diagrams Figs 167 and 169 it will be found that the tangential acceleration of

Q about K is 0.635 and is negative, S about R is 0.54 and is negative, S about F is 0.063 and is negative, J about D is 0.23 and is positive, Y about V is 0.36 and is negative

Dividing these figures by the respective lengths of the links, the angular acceleration of each link is found, corresponding to a crank pin velocity of 1 foot per second. In the case where the crank pin velocity is changed to 30 feet per second say, these numbers must be multiplied by  $30^\circ = 900$  to find the corresponding accelerations. This is further exemplified in Article 144.

- 142. Dynamical principles from which the accelerating forces acting on the links may be found when the accelerations are known. The forces causing the acceleration of any link having plane motion may be analysed into.—
  - A force, acting at the mass centre of the link, in the direction of the acceleration of the mass centre, whose magnitude is equal to the product of the mass of the link and the acceleration of the mass centre.

Thus it a is the acceleration of the mass centre, M the mass of the link, F the accelerating force,

(2) A couple acting on the link, in the plane of motion, whose magnitude is equal to the product of the moment of mertia of the link, I, about an axis through the mass centre perpendicular to the plane of motion and the angular acceleration of the link

Thus if z is the angular acceleration of the link, L the couple producing this acceleration,

$$L = Iz = Mk^2z = \frac{W}{g}k^2z$$
 ......(2)

Having computed the force F from equation (1) and the couple L from equation (2), the two may be combined into one force by moving F parallel to itself through a distance  $\epsilon$  in the plane of motion, from the mass centre,  $\epsilon$  being found from

$$F_{\ell} = L$$

That is, c is given by

$$c = \frac{L}{h} = \frac{k^2 z}{a}$$
 . ....(3)

Thus the magnitude and the position of the single force is found which is able to produce the given instantaneous acceleration of the link

For example, let the link RS, Fig. 170, be supposed isolated from the Joy gear, and suppose that when it formed part of the gear the acceleration of the mass centre was found to be 378 ft. per sec. per sec, and its angular acceleration about the mass centre, 301 radians per sec. per sec in the negative direction. Further suppose its weight to be 35 pounds and its moment of metha about the mass centre to be 0.32. Then the magnitude of the force producing the instantageous acceleration is from (1)

$$F = \frac{35}{23.3} \times 378 = 412 \text{ lbs.}$$

And the couple producing the angular acceleration,

$$L = 0.32 \times 301 = 96.4$$
 foot lbs.

The force cF must now be moved parallel to itself through a distance

$$c = L \cdot F = 96.4 \cdot 412 = 0.242 \text{ foot}$$

so that its moment with regard to the mass centre is negative

This accelerating force is brought on to the link by forces acting through the joints at the ends. The accelerating force F may therefore be looked upon as the resultant of these two end forces. The link is therefore held in instantaneous equilibrium by the two forces at the ends and the accelerating force F, reversed in direction. The problem of finding the end forces thus becomes one of pure statics

143 To find the moment of inertia of a link of a mechanism about an axis, through its mass centre, perpendicular to the plane in which the link moves. The method depends upon the principle that any rod or link is dynamically equivalent to two particles,  $m_1$ ,  $m_2$ , concentrated at two points, distant  $d_1$  and  $d_2$  respectively from the mass centre, as indicated in Fig. 171, these distances being connected

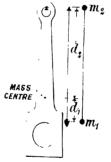


Fig. 171. Swinging a plumb bob and a link in unison to find  $k^2$ 

with the radius of gyration of the rod,  $k_i$  about the mass centre, by the relation

$$d_1d_1 = k$$

This relation is easily established from the conditions, that if the two particles are dynamically equivalent to the link

- The sum of their masses must be equal to the mass of the link.
- (2) The centre of gravity of the particles must coincide with the centre of gravity of the link they represent

(3) The moment of mertia of the particles about an axis, through the mass centre, perpendicular to the plane of motion of the link must be equal to the moment of mertia of the link about the same axis.

Expressed algebraically these conditions are, M being the mass of the link and m<sub>1</sub> and m<sub>2</sub> the respective masses of the particles,

$$m_1 + m_2 = M$$
 ......(1),  
 $m_1 d_1 - m_2 d_2 = 0$  ......(2),  
 $m_1 d_1^2 + m_2 d_2^2 = M h^2$  ......(3).

Substituting the value of M from (1) and  $m_z$  found from (2) m (3) the above relation will be obtained.

Also, substituting the value of m, from (2) in (3),

$$m_1 = \frac{Md_2}{d_1 + d_2}$$
 ... (4),

and similarly

There is no restriction on the choice of the quantities  $d_1$  and  $d_2$  so that there are an infinite number of two particle systems which are dynamically equivalent to the actual link. When either  $d_1$  or  $d_2$  is fixed, a particular two particle system is fixed. If the equivalent two particle system, the particles being supposed connected by a rod without mass, be allowed to oscillate about an axis through one particle, parallel to the given axis through the mass centre, the distance  $(d_1 + d_2)$  to the other particle is the length of the equivalent simple pendulum. The determination of the length of an equivalent simple pendulum therefore for the actual link determines a distance  $(d_1 + d_2)$ , and the determination of the position of the mass centre of the link fixes the distance  $d_1$  supposing the axis about which oscillation takes place is at  $d_1$ .

The way to find an equivalent simple pendulum for the extract link

The way to find an equivalent simple pendulum for the actual link is to suspend the link complete in every particular from some convenient axis. A kinfe edge passed through the journal at one end is usually an easy way of doing this. Then suspend a plumb line from the kinfe edge also, as indicated in Fig. 171, and adjust its length until it swings in unison with the rod. If t is the length of this plumb line, and d<sub>i</sub> is the distance of the mass centre of the link (found by balancing the link on a kinfe edge), from the axis of suspension,

$$d_1 = l - d_1.$$

Hence

$$k^2 = d_1(l - d_1) = d_1d_2$$

and the value of k can be computed. If W is the weight of the link,

its moment of inertia about an axis, through the mass centre, parallel to the axis of suspension is

$$\frac{W}{a} \times k^{9}$$
.

Mr Aspinall has had each of the links of the Joy gear illustrated in Figs. 140 and 142 dealt. 4th in this manner and the results of these experiments are shown in Table 12. Considering a particular case, the link RS of the gear, Fig. 140, was suspended on a kinte edge passed through the journal R. The plumb line which oscillated in unison with it was 14 inches long. By balancing on a kinte edge the distance of the mass centre from the kinte edge was found to be  $8\frac{1}{4}$  inches •Hence

$$d_1 = 8\frac{1}{2}'' = 0.792$$
 foot,  
 $d_2 = 1.166 - 0.792$  foot = 0.374 foot,  
 $k^2 = 0.792 \times 0.374 = 0.296$ 

The weight of the link is 35 lbs. Hence its moment of inertia about an axis, through its mass centre, perpendicular to the plane in which it moves is

$$\frac{35}{32.2} \times 0.296 = 0.32 \frac{W}{g} \text{ foot 2 units}$$

Notice that all the dimensions must be expressed in feet.

The way is now clear for the complete solution of the following problem.

144 Find the accelerating forces in magnitude and position for the links of the Joy gear, Fig. 140, when the crank pin has a velocity of 30 feet per second, and the crank angle has the value  $\theta$  degrees. The given velocity corresponds with a speed of 68 miles per hour for the engine in question, the whitels being 7' 3" in diameter and the stroke, 26 inches

Let Fig 167 represent the configuration of the gear, then Fig 168 and Fig 169 are respectively the velocity and acceleration diagrams. The scale attached to them is however drawn for a crank pin velocity of 1 foot per second.

With the present data,

Vk, Fig. 168, now represents 30 feet per second,

Ak, Fig. 169, represents  $30^{\circ}/1.083 = 830.7$  feet per sec. per sec.

The centre lines of the gear in the configuration determined by the crank angle  $\theta$ , and the parts of the acceleration diagram required for the present problem are re-drawn in Fig. 172 and the proper scale is attached to it. Any line however in the diagram, Fig. 169, measured

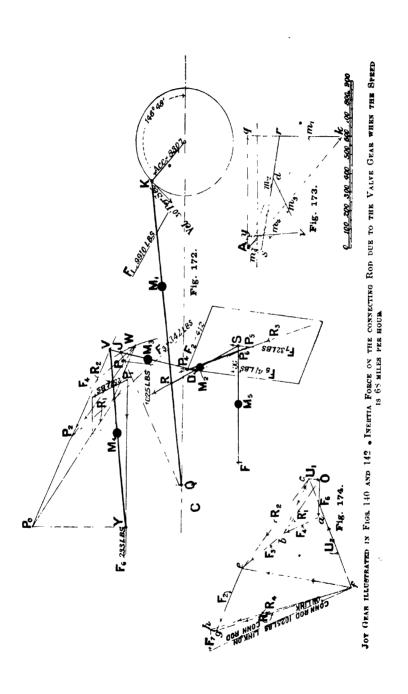
on the scale attached to it multiplied by 900 will give the length measured on the new scale of the diagram, Fig. 173.

The work is to be carried out in the following way, full instructions being given for the sake of completeness.

- (a). Draw the genu in the configuration corresponding to the given erank angle  $\theta$ 
  - (b) Draw the velocity diagram as in Fig. 168.
- (c) Compute from this the radial acceleration of the various points scheduled in Table 11.
  - (d) Draw the acceleration diagram as in Fig. 173.
- (e) Weigh each link and enter the weights as in line 2, Table 12
  - (1) Calculate the masses corresponding to the weights, line 3
- (g) Mark on the drawing of the gear, Fig. 172, the respective positions of the mass centres of the links  $M_1, M_2, M_3, M_4, M_5$
- (b) Find the corresponding points  $m_1$ ,  $m_2$ ,  $m_3$ ,  $m_4$ ,  $m_5$  in the corresponding acceleration images, qk, rs, dv, ry, As, Fig. 173.
- Measure off the accelerations of the points m<sub>1</sub>, etc., and enter the results in line 5, Table 12
- (j) Multiply together corresponding numbers in lines 6 and 3 of Table 12 obtaining thereby the several torces competent to cause the instantaneous accelerations of the respective mass centres of the links.

These forces have to be moved parallel to themselves a distance c such that in the new positions their moments about the respective mass centres can produce the instantaneous angular accelerations of the links of the goar. Hence the next part of the work is directed to the finding of c.

- (k) Adjust a plumb line to swing in unison with each link, suspended in succession from a kinde edge through one journal Enter the plumb line lengths in line 7 of the table.
- (l) Enter in line 8 of the table the distance of the mass centres of the several links from the axes about which they were suspended. This is the dimension  $d_1$ .
- (m) Subtract the numbers of line 8 from the corresponding numbers in line 7, finding thus  $d_{\tau}$ , line 9
  - (a) Compute the several values of  $d_1d_2 = k^2$ , line 10.



(o) The next step is to find the tangential acceleration z The points whose tangential accelerations are required are entered in line 12, and the actual values of the tangential accelerations are placed under them. These accelerations are measured from Fig. 169, the lengths to the scale of that figure being multiplied by 900. The lines in the figure representing these tangential accelerations are, taking them in the order of the table,

$$t_i q = t_i s = t_j = t_i q = t_i s$$
.

- (p) The sign of the tangential acceleration of each link is entered in line 13. This is determined by observing whether the tangential acceleration with regard to the axis specified in line 12. is in the counter-clockwise or clockwise direction. Thus, the acceleration  $t_2s$  with regard to the centre r is clockwise, that is, negative.
- (q) Enter the respective lengths of the links measured between the points KQ, RS, DJ, VY and FS, in line 14.
- (r) Divide the tangential accelerations in line 12 by the corresponding lengths in line 14, the quotients are the corresponding angular accelerations of the several links and these are entered in line 15.
- (s) Though not necessary to the problem in hand, the magnitudes of the couples nécessary to produce the instantaneous accelerations given in line 15 are computed by multiplying corresponding figures in lines 15 and 10 and 3. The products are entered in line 16
- (t) Compute the respective values of  $\frac{k^2z}{a} = c$ , from the numbers in lines 10, 15 and 5. These are entered in line 17.
- (a) Through the mass centre of each link  $M_1$ ,  $M_2$ , etc., in Fig. 172, draw lines respectively parallel to  $Am_1$ ,  $Am_2$ , etc. in the acceleration diagram, Fig. 173, and then parallel to these lines through  $M_1$ ,  $M_2$ , etc draw forces  $F_1$ ,  $F_2$ , etc. at the respective distances  $c_1$ ,  $c_2$ , etc given in line 17, placing each force to that side of the mass centre which enables it to produce a rotation of the sense given in line 13, supposing the link to turn about an axis through its centre of mass. All the forces are shown reversed in direction in Fig. 172 for reasons given in Article 142.

Thus the problem is completely solved.

TABLE 12.

Joy Gear. Lancashire and Yorkshire Railway.
Velocity of crank pin, 30 feet per second, corresponding to a speed of 68 miles per hour with 7' 3" driving wheels and 26" stroke.

1.	Designation of link	• QK	SR	DV	VY	FS	Valve
2.	Weight W lbs	446	35	34	45 25	31.5	111
3.	$\text{Mass} = \frac{W}{g}$	13 85	1 087	1055	1 405	0 98	3 45
4	Point on diagram, Fig. 173, whose acceleration is to be measured	$m_1$	, m.,	m <sub>s</sub>	 	   m <sub>5</sub>	
5	Acceleration = $a$ Feet per sec. per sec.	715	378	324	183	423	67.5
6.	Force, $F = \frac{W}{g}a$ , lbs	F, 9910	F <sub>2</sub> 412		F <sub>4</sub> 257	$F_s$	F <sub>6</sub> 233
7.	Length of plumb line Feet		$\frac{1166}{\mathrm{from}R}$	1 558 from <i>D</i>	2 785 from l'		
8.	Distance of c of gravity of link from axis = $d_1$ Feet	418	0 792	1106	1 777	1 250	
9	$d_2$	1 24	0.374	0.392	1 008	0 635	
10	$d_1d_2 = k^2$	518	0 296	0 457	1794	0 794	
11.	I about mass centre	718	0.32	0.482	2.52	0777	
12	Tangential acceleration 900 times the values in Fig. 169 Feet per sec per sec.	Q about <i>K</i> 565	S about R 501	.f about D 227	Y about V 315	8 about F 85 5	•
13.	Sign of tangential acceleration		_	+	_	-	
14.	Length of link. Feet	6 166	1 66	1713	3625	2 33	
15.	Angular acceleration in radians per sec. per sec $= z$	918	301	132 5	87	367	
16.	Magnitude of couple, $L$ , in foot lbs.	L, 6600	$\frac{L_{i}}{964}$	L, 63.8	$L_4$ 219	L, 28 5	
17.	Distance, $c = \frac{k^2 z}{a} \text{ or } \frac{L}{F}. \text{ Fret}$	0 665	0 242	0 167	0.89	0 636	

145 Bennett's construction for finding a point in the line of action of the force producing the instantaneous acceleration of a link, when the directions of the accelerations of two points of the link are respectively given. The work of the preceding article may be shortened by using the following theorem which was given to the author by Mr G. T. Bennett of Emmanuel College, Cambridge.

**Theorem.** If a rigid link, RS, Fig. 175, have plane motion, and the direction of the acceleration of two points in the link be given, as

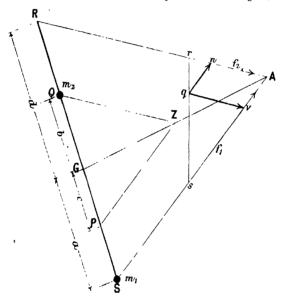


Fig. 175. Bennitt's Conservation for finding Z, a point in the line of Action of the resulting accelerating Porce

R and S, then, if G is the mass centre of the link, and P is the centre of oscillation with respect to R, the force which produces the instantaneous acceleration of the link passes through a point Z found as follows:—

Produce the given directions of acceleration to meet in A and join GA. Through P draw a parallel to SA cutting the line GA in Z. Then Z is the point required.

**Proof.** Let  $k^2$  be the radius of gyration of the given link about an axis through its mass centre at right angles to the plane of motion. And let the directions of the accelerations of the two points R and S be given respectively by RA and SA. Let the mass M, of the link, be supposed concentrated into a system of two particles one of which,  $m_{ij}$ is placed at S. Then it has been shown in Art 143, that if the two particles are to form an equivalent dynamical system, the second particle mo, must be placed at a point Q, whose distance from G, represented by b is found from the relation

$$ab = k^2$$

where a is the distance SG,

Also the magnitude of  $m_i$  is

and the magnitude of  $m_2$  is

Again, let R, P be two other points at which the mass M might be concentrated into an equivalent two particle system, R being one of the points whose direction of acceleration is given. Then if PG = c and GR = d

$$cd = k^{2}$$
Therefore
$$ab = cd,$$
from which
$$c = b + c$$

$$a = a + d \qquad \dots \qquad (3)$$

Assume for the moment that the magnitudes of the accelerations of the points R and S are known, and let them be respectively represented by  $f_2$  and  $f_1$ . Then, if  $rA = f_2$  and  $sA = f_2$  is the acceleration image of the link. Let q in the image, correspond with Q in the link. Then qAis the acceleration of the point Q. This can be resolved into two components, qu and qv, respectively parallel to the directions of the accelerations, SA and RA. From this it will be seen that whatever be the actual magnitude of the acceleration  $f_i$ , the magnitude of the component, qn, parallel to it, is such that

$$qn \cdot sA = rq \quad rs = (d-b) \quad (a+d),$$

$$qn = \frac{f_1(d-b)}{(a+d)} \qquad (4)$$

so that

Refer these component accelerations to the particle at Q and it will be D. V.

seen that the accelerating force acting on the link is the resultant of three component forces, namely,

 $m_i f_i$  acting at S in the direction sA,  $m_i \bar{q} n$  acting at Q in a direction parallel to sA,  $m_i \bar{q} n$  acting at Q in a direction parallel to rA.

The next step is to find the position of the resultant of the two parallel forces of this group by taking moments about the point Q. If x is the distance from Q at which this resultant force cuts the link RS.

$$x = \frac{m_1 f_1(a+b)}{m_1 f_1 + m_2 qu}$$
 ..... (5). •

Substituting the respective values of  $m_1$  and  $m_2$  from equations (1) and (2), and the value of  $\overline{qn}$  from equation (4), the expression reduces to

$$a = \frac{b}{d}(a+d),$$

and introducing the value of the ratio b/d from equation (4) this becomes finally

$$x = b + c = QP$$
.

That is to say, the resultant of the two parallel forces passes through the point P, which is the centre of oscillation of the link with respect to R. If then, this resultant be produced to cut the direction of the remaining component force through Q in Z, Z is a point in the line of action of the force producing the instantaneous acceleration of the link.

Again, since 
$$ab = cd$$
,  
 $a = c \cdot b$ 

Therefore the points G, Z and A lie on a straight line. Hence Z may equally well be found by joining G to A and drawing PZ, parallel to SA, as stated above  $\bullet$ .

It follows that Z may just as well be found by drawing QZ parallel to RA to cut GA in Z, so that either of the two centres of oscillation Q or P may be used in the construction as may be found convenient.

This Theorem may now be applied to find the position of the accelerating force for each link of the Joy gear. It will be sufficient to exemplify the method by using it to find the point through which the

<sup>•</sup> This Theorem is also true of the sense of the acceleration of one of the points be reversed. For instance, if whilst the sense of the acceleration of R remains RA, that of S is changed to AS, Z is still a point in the line of action of the resultant.

accelerating force which acts on the link RS passes. For this purpose the link RS of Fig. 172, has been re-drawn in Fig. 176. With this method it is only necessary to fill in the first ten lines of Table 12.

Having drawn the acceleration diagram (not shown in the figure, but supposed to be drawn in a position near it) draw through the points R and S, lines respectively parallel to the directions of acceleration As, Ar, given by the acceleration diagram, Fig. 173. Mark the position of the mass centre G on the link. Next mark off the point P so that

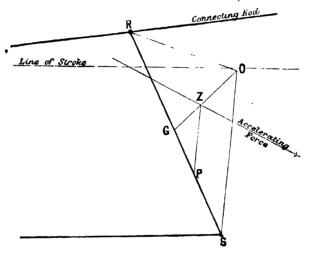


Fig. 176. Construction for finding the Position of the Resultand Accelerating Force in the case of the link RS, of the Joy Gear, Fig. 172.

the distance RP is equal to the length of the plumb line which was found to swing in unison with the link. In the present example the distance RG is 0.79 foot, and the distance RP 1.106 feet. Through P draw PZ parallel to the line SO, cutting GO in Z. Then the accelerating force must pass through Z.

The direction of the accelerating force is given by the line  $Am_i$  in the acceleration diagram, Fig. 173, and its magnitude is given in the sixth line of Table 12. Hence the force producing the instantaneous acceleration of the link is known completely, in magnitude, direction and position.

When all these instantaneous accelerating forces have been marked

on the drawing, the problem becomes a statical one and the continuation of the general solution is given in the next article.

146 Find the force which must act at R to balance the accelerating forces found in Art. 144. The method of solution is to consider each link in order beginning with YV, reverse each accelerating force F in direction, find the resultant of all the forces acting on the link, and then apply the principles of Article 134. To the system of forces  $F_1 \dots F_s$  must be added the force  $F_6$ , representing the force necessary to overcome the acceleration of the slide valve and valve spindle supposed concentrated at the point Y. The necessary numbers are given in the last column of Table 12.

To  $F_{\delta}$  may be added the additional force required to overcome the friction of the slide valve. In the present case, however, this is considered to be zero because the object is to show the force at R due to acceleration alone.

1. Consider the equilibrium of the link YV, Fig. 172. The forces acting on the link are  $F_{\theta}$  and  $F_{4}$ , known completely, and  $U_{1}$  the vertical reaction at the guide of the joint Y, known in direction only, and the force through the joint V altogether unknown in direction and magnitude. Find the resultant,  $R_{1}$ , of  $F_{\theta}$  and  $F_{4}$ , and produce it to cut a perpendicular to the line of stroke through Y in  $P_{\theta}$ . Join  $P_{\theta}V$ , fixing thereby the direction of the force at V. In Fig. 174 set out  $Oa = F_{\theta}$ ,  $ab = F_{4}$ , and draw through b and O parallels respectively to  $P_{\theta}Y$  and  $P_{\theta}V$  in Fig. 172, thus fixing the point a. Then

cO is the reaction at Y, bc is the reaction at the joint V.

The system of torces,  $F_4$ ,  $F_4$ ,  $U_1$ , and bc then hold the link YV in equilibrium.

2 Consider the equilibrium of the link VJD. The link is kept in equilibrium by the reaction at the joint V, that is cb (notice the reversal of the sign here), the torce  $F_s$ , the reaction  $U_s$  at  $J_s$  and the reaction at the joint D. Of these forces the first two are completely known. Find the resultant  $R_s$  of the forces  $F_s$  and cb. The directions of these two latter forces meet in  $P_s$ . Then this resultant, the force at  $D_s$  and the reaction at  $J_s$  must meet in a point. Produce  $R_s$  to meet the direction of the reaction at  $P_s$ , which is normal to the path of  $J_s$  and join  $P_sD$ , thus fixing the direction of the reaction at  $D_s$ . In Fig. 174 draw be equal to  $F_s$ ,

and through e and c draw parallels respectively to the lines P.D and  $P_{\theta}J$  in Fig. 172, meeting in f. Then ef is the force at the joint D, and fc is the reaction at J, called  $U_{\theta}$ .

3. Again, consider the equilibrium of link RS. It is kept in equilibrium by the forces fe acting at D,  $F_{c}$ , and a force  $F_{c}$  acting at S parallel to  $F_{b}$  and equivalent to 32 lbs. ( $F_{c}$  multiplied by the fraction Fa/FS), the reaction at the joint  $R_{c}$  and the reaction at  $S_{c}$  which must be along the line  $SF_{c}$ . The resultant of the three forces fe,  $F_{D}$ , and  $F_{\tau}$  is  $R_{c}$ , whose line of action cuts the direction of the reaction of the joint S in  $P_{b}$ . Join  $P_{c}$  to the joint  $R_{c}$  fixing thereby the direction of the reaction of the joint  $R_{c}$ . In Fig. 174 set on eg to represent  $F_{c}$ , gh to represent  $F_{c}$  and then through h and F draw lines parallel respectively to  $P_{a}S$  and  $P_{c}R$  in Fig. 172, thus fixing the point e. Then e is the force at R whose magnitude is to be found. Its magnitude, measured from the diagram, is 1025 lbs.

So that at 68 miles per hom with the motion in full forward gear, at the instant the crank angle passes through the angle  $\theta$  a force of 1025 lbs acts on the rod at the joint R to accelerate the motion of the links of the valve gear alone.

At this speed it is very improbable that the motion would be in full forward gear, but the engine would be linked up so that the path PP would be nearer the mid-vertical position. This point does not make a material difference to the problem, and it has been worked out in full forward gear in order to take extreme conditions

To find the maximum value of this force at R it would be necessary to work out its value for a series of values of the crank angle. Practically the maximum value of the force is unimportant compared with a knowledge of its value when the connecting rod is in the position where its inertia loading due to its own mass is a maximum. Because, whatever this maximum loading may be, the force at R must then be added to it. The mertia loading of the connecting rod may be considered to reach its most dangerous point when the rod is at right angles to the crank, because then the direction of acceleration of each particle of the mass of the rod is approximately at right angles to the red, and it becomes loaded transversely and has to sustain bending stresses. When the rod is at right angles to the crank the value of the force at R works out to 835 lbs in a direction almost at right angles to the rod. This was determined in the manner set forth in the previous articles

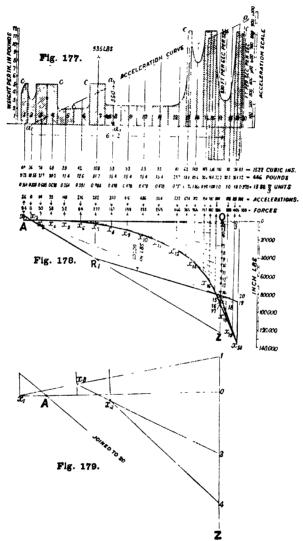
147. To find the maximum bending moment on the connecting rod, Figs. 140 and 172, due to its own inertia and to

the inertia of the valve gear when the crank and the rod are at right angles and the speed is 68 miles per hour. It will be found that when the crank is in the position where it is at right angles to the connecting rod, the radial acceleration of Q about K is negligible. The direction of the tangential acceleration of Q about K therefore practically coincides with the vector representing the acceleration of K, the crank pin. The velocity image is therefore a vector Ak at right angles to the rod. Hence the acceleration of K at right angles to the rod is a maximum and equal to  $\omega^i r$ , the acceleration of Q is practically zero and the acceleration of every other point along the rod is proportional to its distance from Q. In any other position of the rod the component acceleration at right angles to the rod results in  $\mathbf{a}_{\bullet}$  bending moment curve having a smaller maximum value, than in the case assumed

To find the inertia loading of the rod the force required for the acceleration of the motion of each particle of the rod should strictly be estimated, but to make such an estimation is impossible unless the weight of the rod per foot follows a definite law, in which case the equation of the bending moment curve may be found easily enough. In practice the weight per foot of a connecting rod is quite arbitrary. For practical purposes, however, it is quite sufficiently accurate to consider the rod made up of a series of elements, and then to suppose that the mass of each element is concentrated at its mass centre. Then the acceleration of the mass centre of each division is to be found, and then the force which must act to cause the acceleration of the division is the product of its mass and the acceleration of its mass centre.

It should be understood that the accelerating forces are brought on to the rod by the two forces acting at the crank pin and the slide bar, so that for drawing the bending moment curve the rod is to be thought of as a beam, supported freely on two supports a distance apart equal to the length of the rod, measured from the centre of the small end to the centre of the big end, and carrying a system of concentrated loads, each load being the force required to accelerate the motion of a particular division of the rod, reversed in direction.

The method is illustrated in Figs. 177 to 179. First a curve is to be plotted, c, c, c, c, whose ordinates represent the weight of the rod per inch, and whose base is the length of the rod. The curve plotted represents the weight of the Lancashire and Yorkshire rod used with the Joy gear under discussion with sufficient accuracy for the purpose in hand. The projection below the line on the right side of the diagram represents the flanges of the big end brasses. It is more convenient to add their weight this way than to add the weight to the upper side of



JOY GRAB ILLUSTRATED IN FIGS. 140 AND 172. BENDING MOMENT DIAGRAM FOR THE CONNECTING ROD CORRESPONDING WITH A SPEED OF 68 MILES PER HOUR.

the curve. The weight per foot here is of course the full vertical width of the diagram.

Next divide the diagram into a series of short divisions, numbered 1 to 20, not necessarily equal in length, but chosen so that the respective mass centres can easily be marked off. Then calculate the weight of each division and find its mass centre. Set out the acceleration curve  $a, a_t, a$  for the position where the crank and the rod are at right angles. As just explained, the acceleration is practically zero at the small end, and at oth r points it is proportional to the distance from the small end, and is  $\omega^2 r$  at the crank pin. For 68 miles per hour with 7' 3" driving wheels and 13 inch stroke the acceleration of the crank pin is, as already found in the previous diagrams, 830 feet per sec. Per sec. Hence. the acceleration may be represented by a straight line passing through the small end centre, and having such an inclination to the base line that the ordinate at the big end represents 830 on some conveniently chosen scale. Then from this curve, scale off the acceleration of the mass centre of each division and multiply by the mass of the division. For example, the weight of division 8 is 154 pounds. The point mrepresents the mass centre of the division. The ordinate to the acceleration curve passing through  $m_i$  namely  $a_i$ ,  $a_i$ , measures its acceleration and scales 350 feet per sec per sec. The force required for the acceleration of this division is therefore

$$F = 350 \times \frac{15.4}{32.9} = 167$$
 lbs.

In the figure the forces corresponding to each division are written under the line passing through the mass centre of each division.

In order to check the accuracy of the work, the resultant of all these forces may be found by taking moments about the big end centre as indicated in Table 13, and comparing it with the resultant found by the graphical methods already explained. From Table 13, it will be seen that the sum of the moments is 81512 meh lbs, and the resultant force is 7770 lbs. Therefore the resultant of all the forces acts at a distance

$$\frac{81512}{7770} = 10.5$$
 inches from the big end centre, ,

Neglecting the distribution of the accelerating forces along the rod and finding the single accelerating force by the graphical methods already explained, the total force works out to 7728 lbs acting at a distance of 101 inches from the big end centre. There is therefore a very good agreement between the two results

The problem now becomes the static one of drawing the bending moment curve corresponding to these forces, reversed in direction, and

TABLE 13

Inertia loading of the Connecting Rod of the Lancashire and
Yorkshire locomotive.

		Distance from	Moment about but end centre
Division	Force	•big end centre	in inch lbs
1	-95	76.75	- 721
•2	0	74	0
3	30 1	70 25	2113
4	57.8	66 0	3820
5	52.4	61	3170
G	845	.5.5	4650
7	277	49	13540
8	167	4:3	7170
9	199	.37	7.370
10	233	31	7220
11	265	2.5	6630
12	466	17 75	8270
13	385	14.25	5480
14	966	11	10626
15	707	7.25	5130
16	882	.5	4410
17	806	2.5	2013
18	858	- 25	2148
19	1005	- 5	- 5025
20	339	- 65	- 2206
	77703		+91612 - 10100 = 81512

to the force acting on the rod from the valve gear at the joint R. The reversed accelerating forces along the rod, and the force from the valve gear act in the same sense. This may be done in a variety of ways, but the following method is the one which requires least labour.

Take  $\circ OA$ , Fig. 178, to represent the length of the rod, centre to centre. Draw a line OZ at right angles to OA. Calculate the moment of each force about O, setting out these moments in order from O beginning with that corresponding to division 1. Those forces to the right of O, corresponding to divisions 18, 19, and 20, have opposite moments about O to the rest and must be set out in the opposite

direction along OZ to the moments of the forces on the left of O. The force corresponding to division No. 1 is also to be set out upwards

Table 13 gives the forces, their distances from  $\theta$ , and the corresponding moments in unch fls

finally arriving at point 20.

Now join point 1 on  $\partial Z$  to the point  $x_0$  where the direction of the force corresponding to No 1 division cuts  $\partial A$ . Join point 3 on the line  $\partial Z$  with point  $x_3$ , where the direction of the force 3 cuts the line  $1x_1$ . Join point 4 on the line  $\partial Z$  with the point  $x_4$ , where the direction of the force number 4 cuts the line  $3x_1$  and so on — Fig. 178 is too small to show this, and Fig. 179 is drawn to a distorted scale in order to show the points referred to clearly

Finally, join the point 20 on the line  $\partial Z$  with the point A. Then  $A(x_1,\ldots x_2,\ldots x_3,\ldots x_3,\ldots 20)=A$  is the bending moment diagram required, and the vertical width of this diagram at any point represents the bending moment at the corresponding section of the rod.

To find the additional effect due to the component of the force R, at right angles to the rod, the magnitude of which is 835 lbs., set out 20-Z downwards on the line OZ to represent the moment of the force about O. This moment is equal to 40915 inch lbs. Join Z to A; produce the line of action of the component at R to cut this line in  $R_1$ , and join  $R_1$  to the point 20. Then the triangle  $AR_120$  is the bending moment on the rod due to the component force at R alone. Consequently the total bending moment at any section due to the acceleration of the rod and the valve gear is given by the vertical width of the diagram shown by thickened lines.

It will be found by measurement that the maximum bending moment on the rod is about 40,000 inch lbs, but that the section at which the maximum occurs is not well defined. All the sections between  $a_0$  and  $x_0$  have to resist a bending moment of about this value.

The design of the rod is admirably suited to meet this condition because it is of uniform section through the divisions 8 to 11, being 12 inches wide and 5 inches deep.

The maximum stress, f, at any specified section of the rod can now be found from the relation

$$M = Zf$$

where M is the bending moment measured from the curve just found, at a position where the modulus of the section is Z.

At the section  $x_{io}$ , where the bending moment is a maximum, the value of  $Z \triangleleft s$ 

$$\frac{1}{6}bd^2 = \frac{175 \times 25}{6} = 73,$$

and M is 40,000 inch lbs = 17.85 inch tons

Therefore

$$f = \frac{17.85}{7.3} = 2.45$$
, say 2.5 tons per square meh.

There will thus be a tensile stress of this amount in the upper edge of section  $x_0$ , and a compressive stress of equal amount in the lower edge of the section

When the rod is in the lower position and at right angles to the crank, the bending moment curve on the rod due to its own mass will be exactly the same as in Fig. 178, but the bending moments will be of opposite sense. The effect of the valve gear at R will not be quite the same, but whatever its magnitude its sense will change and will be the same as the sense of the bending moment due to the mass of the rod. The bending moment curve of Fig. 178 will therefore approximately represent the total bending moment on the rod for the lower position, it being understood that the sense of the moments is reversed. Consequently section  $x_0$  will now have to sustain a compressive stress in its upper edge, and a tensile stress in the lower edge. The stress acting therefore alternates between a maximum tensile stress of 2.5 tons per square inch and a maximum compressive stress of 25 tons per square inch. The range of stress is thus 5 ton per square inch. So long as the range of stress is within the clastic limit of the material (15 to 16 tons per square inch for mild steel) the rod is safe, but to have a factor of safety the range should not exceed 8 tons per square inch at the highest speed ever reached by the engine.

When the stress due to acceleration at any point of a given section is known for any one speed the corresponding stress at any other speed can easily be computed, because these stresses vary as the squares of the speeds.

Thus at 80 miles per hour the stress f at  $x_{10}$  is found from

$$f: 2.5 = 68^{\circ}: 80^{\circ}$$

from which

f = 3.46 tons per square inch,

giving a range of stress of 692 tons per square inch.

The stresses due to the merita loading of the rod are of course in addition to the stresses in the rod due to the transmission of force between the crosshead and crank pin, and to the stress caused by the moving of the valve against friction.

Any other link of the valve gear may be examined in the same way, bearing in mind that the mettra loading of the link is to be computed for the position where it is a maximum

It may be pointed out that if a rod is found to be weak when examined for the acceleration stress, no addition is made to the strength by merely increasing its width, because by doing this the mertia load is increased exactly in the same proportion as the modulus of the section, and f remains the same. But if the depth of the rod is increased although the mertia loading increases in proportion to the increase of depth, the value of Z increases as the square of the depth.

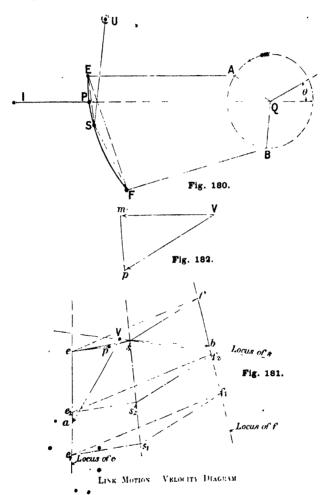
148 Link motion. Velocity diagram. The preceding method may be applied to find the velocity and acceleration of all points in a link motion, but neither the velocity nor the acceleration diagram can be drawn directly as in the case of the Joy gear. It will be remembered that the position of the link for a given crank angle can only be found by a process of fitting a template of the link to three curves which are respectively the loci of the ends of the eccentric rods and the end of the suspension link. The same kind of difficulty occurs in the drawing of the velocity and acceleration diagrams. This may be illustrated by drawing the velocity diagram for the position of the link motion shown in Fig. 180.

Take any pole V, Fig. 181. Draw Va at right angles to the eccentric QA, and Vb at right angles to the eccentric QB, making the length of each of these proportional to the respective velocities of the points A and B. In general these will be each equal to  $\omega_1$ ,  $\omega$  being the angular velocity of the crank shaft, and r the eccentric radius.

The direction of motion of the point E of the link relatively to A is at right angles to the eccentric rod AE. Draw therefore an indefinite line through a in the velocity diagram at right angles to the rod AE. Again the direction of motion of the point F of the link relatively to B is at right angles to the eccentric rod BF. Draw therefore an indefinite line through b in the velocity diagram at right angles to the eccentric rod BF.

Again the direction of motion of the point S of the link is at right

angles to the suspension link US. Draw therefore in the velocity diagram as indefinite line through the pole V at right angles to US. Then, joining S to E and F, a triangle must be found in the velocity diagram similar to ESF, placed so that its sides are at right angles to



the corresponding sides of the triangle ESF, and so that its corners be upon the indefinite lines which have already been drawn in the velocity diagram. This triangle esf is the velocity image of the triangle ESF.

By constructing a triangle on es similar to the triangle ESP the position of P is found in the image. The triangle may be found by the following construction.—

Draw any line  $s_i f_i$  at right angles to EF and construct a triangle  $e_i f_i s_i$  similar to the triangle ESF. Again draw any other line  $e_i f_i s_i$  at right angles to EF and construct a triangle  $e_i f_i s_i$  similar to ESF. Then the indefinite line joining the points  $s_i s_i$ , is the locus of the apexes of all the triangles similar to ESF which have the end points of their bases on the loci of e and f. Therefore the point s, where the line joining  $s_i$  and  $s_i$  cuts the required locus of  $s_i$  is the position of the apex of the required triangle. Then

Vp is the velocity of the centre of the motion block, Vs the velocity of the point of suspension, Ve the velocity of the upper end of the link, Vf the velocity of the lower end of the link;

and the velocity of any point in the gear can be found when the corresponding point is located in the velocity diagram and joined to V. The method need not be pursued, particularly as the objects of the construction, namely the finding ultimately of the acceleration of the various points in order to obtain the forces acting on the mechanism, can be found with sufficient accuracy for practical purposes by simpler approximate processes.

It may be pointed out that the velocity of the point P in the diagram is in the direction Vp, and this is drawn to a larger scale in Fig. 182. The centre of the motion block is, however, constrained to move in a direction PI. It follows that the block must slide, or slip in the link to allow this to take place. The direction in which this relative motion is possible is parallel to the tangent to the link at the point P. Hence if a line pm, Fig. 182, be drawn parallel to the tangent to the point P of the link cutting the direction of motion of the motion block in m, Vm is the velocity of the valve spindle, and mp is the velocity of the motion block relatively to the link, that is the instantaneous velocity of slip.

149 Link motion. Inertia forces. The link is at any instant a beam supported at its ends, with a lead applied at the centar of the motion block. The design of the link therefore requires that the maximum bending moment on the link should be estimated. The lead on the link is made up of two parts, namely:—

- (1) The static force required to move the valve against the friction produced by the steam pressures plus the gland friction.
- (2) The mertia loading due to the acceleration of the valve, valve spindle and parts up to the motion block which have the same motion as the valve.

The estimation of the first part is not difficult when the form of valve is given.

The second part requires the acceleration of the valve to be found. For all practical purposes this can be found at any instant from the approximate displacement equation (5), given in Article 97. This equation, expressed in terms of the equivalent eccentric, is

$$x = \rho \cos(\theta + \psi)$$

When the crank is revolving uniformly the angle  $\theta$  increases uniformly with the time, so that if  $\omega$  is the angular velocity, the angle turned through in t seconds is  $\omega t$ , and hence  $\theta = \omega t$ . Hence

$$x = \rho \cos(\omega t + \psi)$$

Differentiating this with regard to the time, the velocity of the valve is

$$v = \dot{x} = -\omega \rho \sin(\omega t + \psi),$$

and the acceleration is

$$a = \ddot{x} = -\omega^2 \rho \cos(\omega t + \psi),$$

and this is a maximum when  $\omega t + \psi = 0$  or 180 degrees, in which case it is equal to  $\omega^2 \rho$ . If W is the weight of the valve and all the parts attached to it which move with the same motion, reckoned up to the motion block, the maximum accelerating force is

$$F = \frac{\Pi'}{\sigma} \omega^2 \rho.$$

This force is a maximum for a given speed when the link motion is in full gear, since then,  $\rho$  has its maximum value. It is a minimum in mid-gear since then  $\rho$  has a minimum value. For a given speed the force varies as the magnitude of the radius of the equivalent eccentric  $\rho$ , and if its value be plotted on the link an estimation of the maximum bending moment can soon be made.

To illustrate this consider the Great Eastern Railway link motion, Fig. 76. The length of the equivalent eccentric in full gear is about two inches. At 60 miles per hour, with driving wheels 7 feet in diameter, the crack shaft makes almost exactly 4 revolutions per second, so that  $\omega$  is equal to 2512 and  $\omega = 632$ . The maximum

acceleration of the valve and the associated valve spindle is thus equal to

• 
$$\omega^2 \rho = \frac{632 \times 2}{12} = 105.3 \text{ ft. per sec. per sec.}$$

If the valve, valve spindle, etc., weigh 200 pounds, the force required for acceleration is

$$\frac{200}{32.2} \times 1053 = 654 \text{ lbs.}$$

The force required to overcome the friction of the valve would be about 2000 lbs. (see Article 24) so that the total force exerted by the link would be in the region of 2650 lbs. The effect of the mertia of the valve and its attachments is thus seen to be considerable at high speed.

A locomotive would not run in full gear at 60 miles per hour, so that the above example may be considered as exhibiting an extreme case. The engines of torpedo boats, however, run at high speeds in full gear, and the above example indicates how to find the loading on the link of engines of this type.

## 150. Link motion. Inertia stresses in the eccentric rod.

The maximum stress in an eccentric rod, due to the merita loading, at a given speed, may be found by the semi-graphical method already exemplified in Article 147 for the Laneashue and Yorkshire connecting rod, the assumption being made that the end of the eccentric rod moves in a straight line which passes through the centre line of the crank axle. The curve representing the weight of the rod would be in most cases simpler in form than that shown in Fig. 177, in fact for all practical purposes the weight of the eccentric rod per foot may be considered constant, and equal to the mean weight of the rod per foot, this mean weight being calculated from the central part of the stem of the rod. Let w be the mean weight per foot of the rod.

l the length in feet, r the eccentricity,  $\omega$  the angular velocity

Then the maximum bending moment occurs at a section distant 0.58l feet from the small end of the rod, and its value is

$$0.065 \frac{l^2 w \omega^2 r}{g}$$
 foot lbs .....(1).

These expressions are easily proved. As in Article 147, and illustrated in Fig. 177, the acceleration of the crosshead contre may be taken equal to zero; the acceleration of the eccentric strap centre is  $\omega^2 r$ , and

the acceleration of a point along the rod may be taken as proportional to the distance of the point from the small end. Let AB, Fig 183, be the rod, and let BC represent the acceleration of the centre of the eccentric strap. Then the inertia load per foot, at a distance x from the small end, will be  $\frac{w\omega^2 rx}{gl}$ , the value of which is zero at the small end and  $\frac{w\omega^2 r}{g}$  at the crank end. Represent this latter quantity by the symbol  $\gamma$  shown by BD in Fig. 183. Then the problem is reduced to finding the maximum value of the bending moment for a beam supported freely at each end

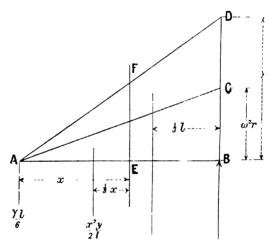


Fig. 183. Bending Moment due to Inertia Loading.

Approximate Solution for an Eccentric Rod

and carrying a load varying as the distance from one support. Let this loading be represented by the triangle ABD. Then the whole load is  $\frac{\gamma t}{2}$ , acting at the centre of gravity of the triangle ABD, which is  $\frac{t}{3}$  from the support B. The reaction at A corresponding to this is  $\frac{\gamma t}{6}$ .

Consider a section EF, distant x from A. Then the bending moment there will be that due to the reaction at A, minus the moment of the area AEF. EF is equal to  $\frac{xy}{I}$ , so that the load represented by

the area AEF is  $\frac{x^2\gamma}{2l}$  acting at  $\frac{x}{3}$  from EF. Thus the bending moment is

$$M = \frac{\gamma l x}{6} - \frac{x^3 \gamma}{6l} \, .$$

Differentiating this and equating the result to zero, M is found to be a maximum when  $x = 1/\sqrt{3} = 0.58l$ . Substituting this value of x in the equation for M, the maximum value is found to be  $0.065l^2\gamma$  as above stated and the corresponding maximum stress in the section is  $\frac{My}{I}$ .

Consider an eccentric rod 4.5 feet long, centre to centre, with an average section 3½ inches deep and 1 inch wide. This would weigh, about 11 pounds per foot run. Let the eccentric radius be 3 inches. Calculate the maximum stress due to the inertia loading when the engine runs at 80 miles per hour, the driving wheels being 7 feet in diameter.

At 80 miles per hour the angular velocity is 335.

Substituting these data in expression (1) above, remembering that r must be expressed in feet,

Maximum bending moment = 
$$\frac{0.065 \times 4.5^2 \times 11 \times 33.5^3 \times 3}{32 \times 12}$$
= 127 foot pounds
= 1524 inch pounds.

The section is rectangular and at 0.58l from the small end is taken to be  $3\frac{1}{2}$  inches deep and 1 inch wale. The modulus of this section, namely,  $\frac{1}{4}bd^2$ , is approximately 2. Hence the maximum tensile, or maximum compressive stress due to the inertia loading is

$$\frac{M}{Z} = \frac{1524}{2} = 762$$
 lbs. per square inch approximately.

This is a small amount, and indicates that with the deep section of the eccentric rods usual in locomotive practice, the inertia loading is fully provided for. In cases where round eccentric rods are used, as in some types of modern high-speed engines, the stress would probably be higher because the circular section, though well adapted to act as a strut, does not give sufficient depth in the plane of motion to keep the inertia stress within small limits if its diameter is fixed solely with regard to the forces it is required to transmit between the eccentric sheave and the valve.

A connecting rod may of course be examined in the same way, and inasmuch as the radius of the crank is so much greater the inertia loading is much more severe than in the case of an eccentric rod.

151. Stresses in an eccentric rod, a connecting rod, or coupling god due to the inertia loading and an end thrust combined. When a rod is transmitting a load along it as a strut, the load being applied at the ends so that the line of action of the load passes through the centre of gravity of every section of the rod, the stress over each section is uniformly distributed, so that if A is the area of a particular section, and F the end load, the stress is

$$\frac{F}{A}$$
lbs per square inch

If there is inertia loading also, causing a bending moment at the section of M inch lbs, and if Z is the modulus of the section, the maximum \*stress at the section due to the lateral mertia load is

$$\frac{M}{Z}$$
lbs, per square meh.

Z is here assumed to be the same for both tension and compression.

If the rod be assumed to remain perfectly straight under the action of the bending moments so that no deflection occurs to modify the condition stated above, the maximum stress at the particular section whose area is A and whose modulus is Z is

$$f = \frac{F}{A} + \frac{M}{Z}$$
 lbs per square inch ..... (1).

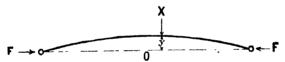


Fig. 184. Bending Mournt due to Thrust.

If however the bending of the rod is taken into account it will be seen from Fig. 184 that at any section X, the bending moment on the rod is that due to the inertia loading plus the bending moment Fy due to the thrust. Hence the total bending moment on any section is

$$(Fy + M)$$

and the relations between the several quantities concerned are obtained from the well-known equation connecting deflection y and bending moment

$$EI\frac{d^{3}y}{dx^{3}} = -(Fy + M).$$

$$EI\frac{d^{3}y}{dx^{3}} + Fy = -M \qquad (4)$$

 $EI\frac{d^2y}{dx^2} + Fy = -M \qquad ..... (2)$ That is

Before this equation can be solved, the bending moment due to the lateral loading must be expressed as a function of x, and with any loading this can always be done approximately by means of a series, which series being substituted for M enables the equation to be solved by the ordinary rules for the purpose.

Equation (2) represents a particular case of the general subject of struts or ties with lateral loads, a subject which has been thoroughly investigated by Professor Perry\*. A simple illustration may be taken from Professor Perry's paper. Consider a compling rod of a locomotive, of uniform cross section, and weighing wilbs per foot. The inertia loading is given by

$$\frac{w\omega^2r}{g}$$
lbs per foot run,

where  $\omega$  is the common angular velocity of the cranks and r the radius of each crank in feet. The total mertia load is therefore, l being the length of the coupling rod centre to centre in feet,

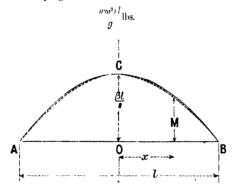


Fig. 185. Bending Moment due to Inertia Loading

Let this quantity be represented by  $\beta$ . The bending moment diagram is a parabola, Fig 185, whose maximum ordinate, OC, represents the maximum bending moment

 $\frac{\beta l}{2}$ 

The dotted cosine curve drawn through the points A, C, B is not greatly different from the parabolic curve. It may therefore be taken to

"Struts and Tre-rods with Lateral Loads," by Professor John Perry, D.Sc., F.B.S., Philosophical Magazine, March 1892.



represent the bending moment curve without introducing sensible error, and this substitution makes the solution of equation (2) quite simple. Observe that the distance OB represents an angle  $\frac{\pi}{2}$  in relation to the cosine curve, and since this distance also represents  $\frac{1}{2}l_{z}$ any distance x represents an angle  $\frac{\pi}{l}x$ . Hence the bending moment corresponding to x is given by

$$M = OC\cos\frac{\pi x}{l} = \frac{\beta l}{8}\cos\frac{\pi r}{l}$$
.

Substituting this in equation (2),

$$EI\frac{d^2y}{dx^2} + Fy = -\frac{\beta I}{8}\cos\frac{\pi x}{l}.$$

The solution of this equation is

$$y = \frac{8^{l} \cos \frac{\pi x}{l}}{k l \pi^{2} - F},$$

and the maximum deflection at the centre, corresponding to x=0, is

$$y_{\text{max}} = \frac{\frac{\beta l}{8}}{\frac{E I \pi^2}{l} - F}$$

The greatest bending moment is therefore

$$Fu_{\max} + M = \frac{\beta l}{8} \left[ 1 + \frac{F}{\pi EI} - F \right]$$

The quantity  $\frac{\pi^2 EI}{\mu}$  gives the buckling load of an ideal column this  $P_i$  and then the greatest bending moment is given by

$$\frac{\beta l \left( P \right)}{8 \left( P + F \right)} \qquad \dots \qquad \dots (3)$$

Divide numerator and denominator of the quantity in the bracket by A, the area of the strut, so that

$$P = p$$
, the brickling load of the strut per square meh in the plane of bending.  
 $F = s$ , the load per square meh due to the end thrust

$$\frac{F}{a} = s$$
, the load per square inch due to the end thrust

Then, if Z is the modulus of the section at the centre of the rod, the maximum stress at the centre, when the coupling rod is in its highest or lowest position, is

$$f_{\text{max}} = s + \frac{\beta l}{Z8} \left\{ \frac{p}{p-s} \right\} \dots \tag{4},$$

that is, s due to the direct loading, and the quantity represented by the second term due to the maximum bending moment caused at the centre by the mertia loading. This formula may be applied to find the maximum speed at which a coupling rod may be driven when the maximum stress at the central section is assigned. Considered as a strut, a coupling rod would fail sideways, the buckling load per square inch at which this would happen being the highest possible value for s. If this value be ascertained and inserted in equation (4), then a value of  $\beta$  can be computed, and since  $\beta = \frac{w \omega^i rl}{g}$ ,  $\omega$ , the maximum angular velocity corresponding with the assumed conditions, can be found.

The maximum value of M in expression (1) is  $\frac{\beta l}{8}$ , hence, comparing expression (4) with expression (1), it will be seen that the only difference is in the factor  $\frac{p}{p-s}$ , which is multiplied into the second term in expression (4).

Consider a coupling rod 100 inches long,  $1\frac{1}{2}$  inches wide, and 4.5 inches deep. The weight of this will be about 22.5 pounds per foot. Let the crank radius be 10 inches and the wheels 6.6" diameter. Calculate the maximum stress at the central section when the speed is 60 miles per heur and there is an end thrust of 1 ton per square inch, using first expression (1) and then expression (4). With the dimensions given  $Z = \frac{1}{4}bd^2 = 5.06$ .

With 6 feet 6 inch wheels the angular velocity of the crank shaft at 60 miles per hour is

$$\omega = 27.1$$
, hence  $\omega^2 = 734$ .

Hence  $\beta = 22.5 \times 734 \times 10 \times 100$  $22.40 \times 32.2 \times 12 \times 12 = 1.59 = \text{total inertia loading in tons.}$ 

And the corresponding maximum stress at the centre of the roe is

$$\frac{\beta l}{8Z} = \frac{159 \times 100}{8 \times 506} = 393 \text{ tons per square inch.}$$

18

The quantity p for a strut 100 inches long and  $4\frac{1}{2}$  inches deep calculated from  $\frac{\sigma n^2 E k^2}{p}$  is approximately 20 tons. Hence the factor

$$\frac{p}{p-s} = \frac{20}{20-1} = 1.05.$$

Hence from (1)  $f_{\text{max}} = 1 + 3.93 \text{ tons}$ 

=4.93 tons

and from (2)

2) 
$$f_{\text{max}} = 1 + (3.93 \times 1.05) \text{ tons} = 5.13 \text{ tons}.$$

The deduction of expression (4) and the working of the example are sufficient to show the nature of the general problem of laterally loaded struts. With connecting rods, even of simple form and cross section, the exact expression for the inertia loading per foot is complex, and the resulting work in connection with the finding of y, the deflection, and from that an expression corresponding to (4), is tedious and hardly necessary for problems connected with coupling rods, connecting rods, and eccentric rods belonging to locomotives. For in the first place the end thrusts are small at high speed, and in the second place the deflections produced by the thrusts are small, and therefore for the purpose in view the maximum stress may usually be estimated by the simpler method of neglecting the deflection and using equation (1). A series of articles appeared in The Engineer\*, in which the subject of coupling and connecting rods is exhaustively treated

" "Connecting and Coupling Rods," by P. H. Patt, The Engineer, Vol. xcr., January to June 1903.

#### CHAPTER X.

# REPRESENTATION OF A VALVE DISPLACEMENT CURVE BY A TRIGONOMETRIC SERIES

152 Preliminary remarks. Many examples have been given above of the representation of a valve displacement curve by two terms of a trigonometric series. In fact the displacement curves of all the reversing motions are approximately represented by an equation of the form

$$a = A \cos \theta + B \sin \theta$$

where x is the displacement of the valve from its central position when the crunk angle is  $\theta$ , and the constants A and B are found from the dimensions of the geau.

Again, the displacement of the piston from its central position given by expression (1), Article 71, may, by the substitution of

$$\frac{1-\cos 2\theta}{2} \text{ for } \sin^2 \theta,$$

be transformed into

$$X = R\cos\theta - \frac{R^2}{4l}\cos2\theta + \frac{R^2}{4l},$$

which may be written

$$X = A_1 \cos \theta + A_2 \cos 2\theta + A_0,$$

where  $A_0$ ,  $A_2$  and  $A_8$  are constants calculated from the dimensions of the gear.

These two examples are only special cases of Fourier's general theorem that any single-valued periodic function of  $\theta$  may be represented by a trigonometric series of sines and cosines of multiple angles with a constant term added.

Referring to Fig. 98, it will be seen that the actual valve displacement curve there shown in full lines, is slightly different from the dotted curve which is assumed to approximately represent it, and which may be obtained by plotting the expression

$$x = A \cos \theta - B \sin \theta$$
,

where  $\boldsymbol{A}$  and  $\boldsymbol{B}$  have the values -1.04 and 1.52 respectively.

If the expression were continued to a few more terms, say

$$x = A_0 + A_1 \cos \theta + A_2 \cos 2\theta + B_1 \sin \theta + B_2 \sin 2\theta$$

then the agreement between the curve plotted from the expression and the actual curve would be much closer, in fact the agreement between the actual curve and the curve plotted from the trigonometric series can be made exact, provided there are a sufficient number of terms in the series.

Each term however involves a coefficient so that if there were twenty terms there would be twenty coefficients besides the constant term  $A_0$ .

There are two points of view from which to consider the question. The first is, given a mechanism, to find a trigonometric series which will represent the displacement of any given point in the mechanism in terms of some variable like the crank angle, the coefficients A, B being calculated from the dimensions of the mechanism. The analytical work involved in calculating only a few coefficients from the dimensions of the mechanism is so formidable that generally speaking only a few terms can be found.

The second point of view is, given the actual displacement curve of a point in a mechanism, to find a trigonometric series which will represent the curve. This can be done for any displacement curve providing only that for a given value of the angle  $\theta$  there is one and only one value of the displacement, a condition generally fulfilled by mechanisms used by engineers.

In order that the matter may be thoroughly understood the way a curve may be built up by me ins of sines and cosines, and then the way a curve may be analysed into sine and cosine components will be explained in the next few articles.

In the following remarks the angle  $\theta$  is expressed in radians, not in degrees

It may also be noticed that in the illustrating figures the axis of the independent variable  $\theta$  is placed vertically, instead of horizontally, in order that the diagrams may correspond with the general arrangement of the valve displacement diagrams. It is only necessary to give the book a quarter turn in the counter-clockwise direction to obtain the figures with the  $\theta$  axis horizontal, as in the usual mode of representation.

The ordinates to a sine curve are denoted by the letter s, and to a cosine source by the letter c

153. A value of the coefficient B may be found so that the curve,  $s = B \sin \theta$ , will pass through a given point P, whose

ordinate, s, has any value positive or negative, and whose abscisss,  $\theta$ , has any value between 0 and  $\pi$ . Let  $s_1$  and  $\theta_1$  be the coordinates of the given point P. Substitute these values in the equation and solve for B, thus

$$B = \frac{s_1}{\sin \theta_1}.$$

The curve which passes through the point  $s_i = 1.7$  and  $\theta_i = \frac{\pi}{4}$  is shown in Fig. 186.

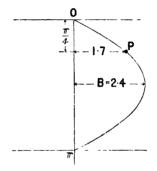


Fig. 186. Sine Curve adjusted to pass through one given point, P.

154. Values of the coefficients  $B_1$  and  $B_2$  may be found so that the curve

$$\mathbf{B} = \mathbf{B}_1 \sin \theta + \mathbf{B}_2 \sin 2\theta$$

will pass through any two points  $P_1$  and  $P_2$ , respectively defined by the coordinates  $s_1$ ,  $\theta_1$ , and  $s_2$ ,  $\theta_2$ , where  $s_1$  and  $s_2$  may have any values positive or negative and  $\theta_1$  and  $\theta_2$  any values between 0 and  $\pi$ . For there are two unknown quantities,  $B_1$  and  $B_2$ , and by substituting the values of  $s_1$ ,  $\theta_1$ , and  $s_2$ ,  $\theta_3$ , in the given equation, there results a pair of simultaneous equations from which  $B_1$  and  $B_2$  may be found.

#### Example.

Let  $s_1 = 3$ ,  $\theta_1 = 1$  radian, define the point  $P_1$ , Fig. 187, and  $s_2 = -0.2$ ,  $\theta_2 = 2$  radians, define the point  $P_2$ .

Substituting these values in the equation we have

$$3 = B_1 \sin 1 + B_2 \sin 2, < -0.2 = B_1 \sin 2 + B_2 \sin 4.$$

Now  $\sin 1 = 0.8415$ ,  $\sin 2 = 0.91$ , and  $\sin 4 = -0.756$ 

Introducing these values in the equations and solving for  $B_1$  and  $B_2$ ,

$$B_1 = 1 41,$$
  
 $B_2 = 1.98.$ 

Therefore if the curve

$$s = 1.41 \sin \theta + 1.98 \sin 2\theta$$
 .....(1)

be plotted, it will be found to pass through the two given points  $P_1$  and  $P_2$ .

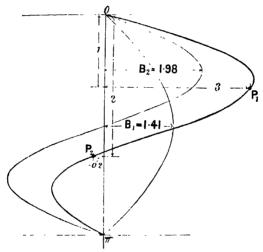


Fig. 187. Sine Curve adjusted to pass through two given points,  $P_1,\ P_2$ 

The component curves  $s=1.41 \sin \theta$  and  $s=1.98 \sin 2\theta$  are shown in Fig. 187 by thin lines. The sum of the ordinates of these curves gives the thick curve represented by equation (1).

155. Values of the coefficients  $B_1,\,B_2\,\dots\,\,B_n$  may be found so that the curve

 $s=B_1\sin\theta_1+B_2\sin 2\theta+B_3\sin 3\theta+.....+B_n\sin n\theta$ will pass through n given points between 0 and  $\pi$ , there being one point and due point only corresponding to each value of  $\theta$ .

Suppose n is equal to 7, for instance. Then the introduction of the

coordinates of each point successively in the above equation will give seven simultaneous equations, and from these equations the seven unknown coefficients

$$B_1, B_2 \ldots B_7$$

may be found

It will now be understood, that the number of terms in a series, is equal to the number of points the curve represented by the series, passes through, and that the coefficients are found from a set of simultaneous equations equal in number to the number of given points.

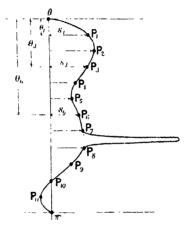


Fig. 188. Arbitrary Curve through eleven points.

Consider the subject from another point of view.

Let  $0, P_1, \dots, P_n, \pi$ , Fig. 188, be any given curve, passing through the points 0 and  $\pi$ , and suppose n points to be selected on the curve, the ordinates of which divide the distance between 0 and  $\pi$  into n+1 equal parts. Eleven points are shown in the figure. Then assuming the values of the coefficients  $B_1, B_2, \dots, B_n$  to have been found, the curve plotted from the equation

$$s = B_1 \sin \theta + B_2 \sin 2\theta + \dots + B_n \sin n\theta$$

will pass through the n selected points, or in other words, the graph of the equation coincides with the given curve at the n selected points. Between a pair of consecutive points however there may be a wide divergence between the graph of the series and the given curve, as for

instance between the points 7 and 8, where the given curve shoots out laterally, and the graph of the equation is indicated by a dotted line

A slittle reflection will make it clear however, that if the number of points, n, is indefinitely increased, the graph of the series, and the given curve, will coincide throughout their whole length.

### 156. To find the value of the coefficients in the series

• 
$$s = B_1 \sin \theta + B_2 \sin 2\theta + \dots + B_n \sin n\theta$$

when n is increased indefinitely. The consequence of increasing u indefinitely is, that the trigonometrical series contains an indefinitely great number of terms, and there is an indefinitely great number of equations in the simultaneous set from which the coefficients have to be found.

The analytical difficulties of solving such a set of equations were overcome by Fourier and a full explanation of his analysis and the application to Heat problems, is given in his famous work *Théorie de la Chaleur*, Paris 1822, a translation of which has been made by Freeman and published by the Pitt Press, Cambridge, in 1878. A very clear exposition of the method of solution is given in *Fourier's Series and Spherical Harmonics*\*, by W. E. Byerly.

It is sufficient for our purpose to state the solution. If  $B_m$  be any one of the n coefficients, its value is calculated from

$$B_m = \frac{2}{\pi} \int_0^{\pi} f(\theta) \sin m\theta \ d\theta,$$

where  $f(\theta)$  is written for the general value of the ordinates hitherto represented by  $s_1, s_2$ , etc

• Every one of the indefinitely great number of coefficients in the series may be calculated from this expression by giving m in succession the values  $1, 2, 3, \ldots, n$ , and performing the operation indicated by the integral in each case

A geometrical illustration may be given of this. Suppose the value of  $B_1$  is to be found for the series which represents the curve  $0P\pi$ , Fig. 189. The expression for  $B_2$  is

$$B_2 = \frac{2}{\pi} \int_0^{\pi} f(\theta) \sin 2\theta \, d\theta$$

Plot the curve  $0Q\pi$  from

$$\alpha = \sin 2\theta$$
.

Then taking a sufficiently large number of divisions between 0 and  $\pi$ ,

\* Published by Ginn and Company, Boston, 1893

multiply together corresponding ordinates of the two curves, (be careful of the signs), and plot the product. Thus

$$ab \times (-ac) = -ad.$$

Then the shaded area, multiplied by  $\frac{2}{\pi}$ , is the value of the coefficient  $B_1$ . That is, the value of  $B_2$  is given by twice the mean ordinate of the shaded area. This may be positive or negative according as the shaded area to the right of the vertical axis is greater or less than the shaded area to the left of the axis.

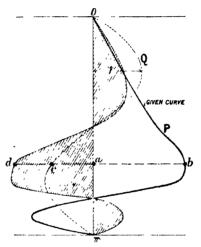


Fig. 189. Geometrical Method of computing the true value of  $B_{\rm s}$ .

In some cases the expression for  $B_m$  can be integrated directly, but in most cases concerned with engineering subjects the curves are of arbitrary form and some method founded on the geometrical method just indicated in principle must be used.

In many cases of interest to engineers the successive terms of the series diminish rapidly, so that it is only necessary to retain the first few terms.

For instance, suppose that in a particular case the terms of the series

 $s=B_1\sin\theta+B_2\sin2\theta+B_2\sin3\theta+\ldots\ldots+R_n\sin n\theta$  converge so rapidly that the first three terms represent the given curvo

хľ

with sufficient exactness. Then, briefly summarising the preceding articles, there are two ways of finding the coefficients  $B_1$ ,  $B_2$  and  $B_2$ .

One way is to select three points on the curve, and form three simultaneous equations with their coordinates in the way already illustrated in Art. 154, and solve for  $B_1$ ,  $B_2$  and  $B_3$ .

A second way is to calculate the values by the general method, assuming an indefinitely large number of points on the curve

The values of the coefficient obtained by the first method will not quite agree with the values obtained by the second method

Thus, in particular,  $B_2$  would have one value if three points were taken on the curve, another value if four points were taken, another if five points were taken, the value gradually approaching a limit as the number of points is indefinitely increased. If the series converges rapidly,  $B_2$  found from a finite number of points on a given curve will not differ greatly from its limiting value found by the general method.

157 Cosine series. The preceding articles apply mutatis mutandis to the cosine series,

$$c = A_0 + A_1 \cos \theta + A_2 \cos 2\theta + \dots + A_n \cos n\theta.$$

As indicated by the constant term, the series holds for a zero value of  $\theta$ . The symbol c is used to represent the ordinates of the curve, and its general value may be written  $f(\theta)$ .

If  $A_m$  be any one of the indefinitely great number of coefficients

$$A_m = \frac{2}{\pi} \int_0^{\pi} f(\theta) \cos m\theta \, . \, d\theta,$$

$$A_0 = \frac{1}{\pi} \int_0^{\pi} f(\theta) \, d\theta.$$

The geometrical illustration already given in Fig 189 applies equally to a cosine series, providing of course the cosine of the multiple angle  $m\theta$  is plotted instead of the sine, to find the corresponding value of  $A_m$ .

The integral for  $A_o$  merely represents the mean ordinate of the serve  $c = f(\theta)$  between the limits 0 and  $\pi$ .

159. Sine and cosine series. From the preceding articles it would appear that it is a matter of indifference whether a sine or a cosine series be chosen to represent a given curve. So long as  $\theta$  is fractricted to values between 0 and  $\pi$ , this inference is correct. But it ceases to be correct if the value of  $\theta$  is taken through  $\pi$ , to values between  $\pi$  and 24, as the curves in Fig. 190 show. In the case of the sine series, a pair of ordinates corresponding to values of the angle  $\theta$ 

and  $2\pi - \theta$  are equal in value but opposite in sign, consequently the curve it continued through  $\pi$  to  $2\pi$  is symmetrical about the point  $\pi$ .

In the case of the cosine series, a pair of ordinates corresponding to values of the angle  $\theta$  and  $2\pi - \theta$  are equal in value and the same in sign, consequently the curve, if continued through  $\pi$  to  $2\pi$ , is symmetrical about a horizontal axis through  $\pi$ .

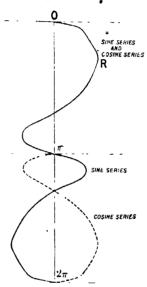


Fig. 190. PROPERTIES OF SINE AND COSINE SERIES

The two cases are illustrated in Fig. 190, where the curve  $0R\pi$ , if represented by the series

$$s = B_1 \sin \theta + B_2 \sin 2\theta + \dots + B_n \sin n\theta$$

becomes the thick curve for values between  $\pi$  and  $2\pi$ , and if represented by

$$c = A_0 + A_1 \cos \theta + A_2 \cos 2\theta + \dots + A_n \cos n\theta$$
.

becomes the dotted curve between  $\pi$  and  $2\pi$ 

Suppose that the two series represent different curves between 0 and  $\pi$  as shown in Fig. 191, where the dotted curve is

$$s = B_1 \sin \theta + \dots + B_n \sin n\theta,$$

# Trigonometric representation of Valve Curves 337

and the thin curve

• 
$$c = A_0 + A_1 \cos \theta + A_2 \cos 2\theta + \dots + A_n \cos n\theta$$
.

Add the ordinates, obtaining thereby the thick curve, whose ordinates are

$$x_1 = s_1 + c_1$$
,  $x_2 = s_2 + c_2$ , etc

The resulting curve is quite arbitrary in form and is represented by the series  $\underline{\ }$ 

$$\boldsymbol{\alpha} = \boldsymbol{A}_0 + \boldsymbol{A}_1 \cos \theta + \boldsymbol{A}_2 \cos 2\theta + \dots + \boldsymbol{A}_n \cos n\theta + \boldsymbol{B}_1 \sin \theta + \boldsymbol{B}_2 \sin 2\theta + \dots + \boldsymbol{B}_n \sin n\theta.$$

The series on the right is known as Fourier's Series.

159. Analysis of a curve, given on a base  $2\pi$  long, into two component curves, one capable of representation by a sine series the other by a cosine series. Let  $x_1$ , Fig. 191, be the ordinate

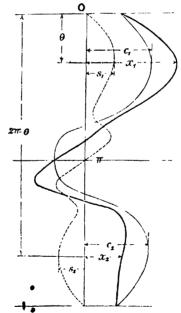


Fig. 191. PROPERTIES OF SINE AND COSINE SERILS

corresponding to  $\theta$ , and  $x_i$  the ordinate corresponding to  $2\pi - \theta$ . Then,  $s_i$  and  $c_i$  being the ordinates of the component sine and cosine curves,

$$x_1 = s_1 + c_1,$$
  
$$x_2 = s_1 + c_2.$$

But in the sine series, for the angles  $\theta$  and  $2\pi - \theta$ ,  $s_1 = -s_2$ , and for the cosine series,  $c_1 = c_2$ .

Hence  $\begin{aligned} x_1 &= s_1 + c_1, \\ x_2 &= -s_1 + c_1. \end{aligned}$  Add  $\begin{aligned} x_1 + x_2 &= 2c_1. \\ x_2 &= -s_1 + c_1. \end{aligned}$  Subtract  $\begin{aligned} x_1 - x_2 &= 2s_1. \end{aligned}$ 

Thus by alternately adding and subtracting pairs of ordinates of any given curve corresponding to angles  $\theta$  and  $2\pi - \theta$ , the corresponding  $\bullet$  ordinates of the cosine series and the sine series are respectively found.

160 Adjustment of the expressions for the coefficients to the limits 0 and  $2\pi$ . Consider the given curve shown by the thick line PQR, Fig. 192 Suppose the second coefficient of the sine series is to be found. Plot the  $\sin 2\theta$  curve, shown dotted in the figure. Multiply together corresponding ordinates of the two curves, obtaining the resultant curve.

$$x = f(\theta) \sin 2\theta,$$

the area of which is shown cross-hatched.

Then the area of the strip  $\Delta\theta$  wide, corresponding to the angle  $\theta$ , is

$$a_1 = (s_1 + c_1) \sin 2\theta \, \Delta\theta$$

The area of the strip  $\Delta\theta$  wide corresponding to the angle  $(2\pi - \theta)$  is

$$x_1 = (-s_1 + c_1) (-\sin 2\theta) \Delta\theta.$$

Therefore the sum of the areas of the two strips is

$$2s_1 \sin 2\theta \Delta \theta$$
.

And the whole shaded area between 0 and  $2\pi$ , multiplied by  $\frac{1}{\pi}$  is the value of the coefficient  $B_1$ . That is, the value of  $B_2$  is given by twice the mean ordinate of the shaded area.

Symbolically

$$B_{\nu} = \frac{1}{\pi} \int_{0}^{2\pi} f(\theta) \sin 2\theta \, d\theta,$$

$$B_{m} = \frac{1}{\pi} \int_{0}^{2\pi} f(\theta) \sin m\theta \, d\theta.$$

and generally

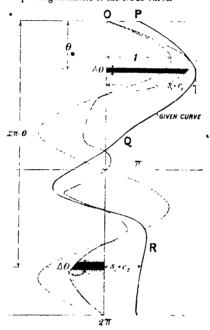
 $\pi \int_0^{\pi} \int_0^{\pi} \int_0^{\pi} (0) \sin nt u dt.$ 

For the second coefficient of the cosine series,

$$(s_1 + c_1)\cos 2\theta$$
.  $\Delta\theta + (-s_1 + c_1)\cos 2\theta$ .  $\Delta\theta = 2c\cos 2\theta$   $\Delta\theta$ ,

represents the sum of the areas of two strips, corresponding to angles

 $\theta$  and  $2\pi - \theta$ , of a curve obtained by multiplying ordinates of the given curve by corresponding ordinates of the  $\cos 2\theta$  curve.



\* Fig. 192. Geometrical method of computing the terf value of  $\mathcal{B}_1$  where the base is  $2\pi$  long

The whole area of the resultant curve multiplied by  $\frac{1}{\pi}$  is the value of the coefficient  $A_2$ . That is,  $A_2$  is equal to twice the mean ordinate of the shaded area. In general therefore

$$A_m = \frac{1}{\pi} \int_0^{2\pi} f(\theta) \cos m\theta d\theta,$$

$$A_u = \frac{1}{\pi} \int_0^{2\pi} f(\theta) d\theta$$

and also

The obvious advantage of these forms is, that a given curve need not be analysed into its component sine-series and cosine-scries curves in order to find the coefficients

Instruments called "Harmonic Analysers" have been devised for

measuring the values of the coefficients directly from a given curve. In the Harmonic Analyser invented by Prof. Henrici, a tracing point is guided along the given curve, but it records twice the mean ordinate of the shaded area. Or put in another way, the readings give twice the mean ordinate of the unplotted curve  $f(\theta) \sin m\theta$  by tracing the curve  $x = f(\theta)$ 

A change in the mechanism of the instrument must be made for each change in m, and it is constructed so that the first twelve coefficients of the infinite series representing any arbitrary sine curve may be found, six of the coefficients belonging to the sine series and six to the cosine series †

There are also simplified methods of finding the coefficients from a selected number of points, the simplification arising from the division of the distance 0 to  $\pi$  into equal parts. For an account of a recent method of this kind depending upon the division of the distance 0 to  $2\pi$  into 4n equal parts, see a paper by Dr S. P. Thompson in the Proceedings of the Physical Society of London, April 1905, entitled, "Note on a Rapid Approximate Method of Harmonic Analysis," and also Articles in the Electrician, May 5, 1905.

These finite-number-of-point methods only give values of the coefficients which approximate to their limiting value.

161. Geometrical method of computing the limiting values of the coefficients  $B_1, \ldots, B_n$ ,  $A_0, \ldots, A_n$ , when the curve to be represented by the series is given. The multiplication of corresponding ordinates of the given curve and the sine  $m\theta$  or cosine  $m\theta$  curve which must be combined with it in order to obtain a curve whose area is proportional to the mth coefficient may be avoided by using a method suggested by the late Prof. Clifford; and applied by Prof. Perry.

Suppose the sheet of paper on which the given curve 1, 2, 3...12 is drawn, Fig. 193, to be wrapped round a cylinder whose circumference is equal to the length of the base  $0.1....2\pi$  of the curve, so that the ordinates through the points 0 and  $2\pi$  coincide along the line ab of the cylinder.

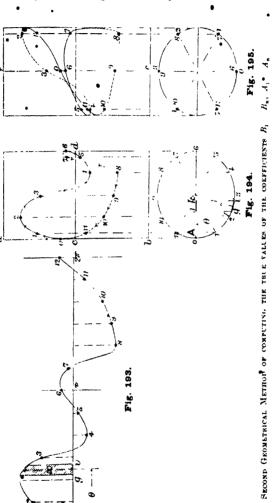
Consider a small area  $x \times gi$ . When the sheet is wrapped on the cylinder this area, as will be seen from the plan of the cylinder, appears in an inclined position. The area of the projection of this area on the vertical plane is

$$\alpha \times jk = \alpha \times qi$$
,  $\sin \theta = \alpha \sin \theta \Delta \theta$ .

<sup>&</sup>quot;On a new Harmonic Analyser," Philosophical Magazine, July 1894.

<sup>†</sup> The instrument is made by Coradi of Zurich and one form of it is constructed so that the values of five pairs of coefficients may be read after once tribing the given curve.

<sup>‡</sup> Proceedings of the London Mathematical Society, Vol. v. pp 11 to 14. See also an article by Prof. Perry in the Electrician, 28 June 1895.



Thus the whole projected area 1, 2, 3......12 (suitably interpreted with regard to the vertical scale), divided by the distance in Fig. 193 representing  $\pi$ , is the value of the first coefficient  $B_1$ .

Due regard must be given to the signs of the loops in the projected area. Starting from 0, consider the elevation of the projected curve, Fig. 194, to be traced out in the direction 0, 1, 2......12, and place arrow-heads to indicate this as shown. A loop of the projected area is to be considered positive when the arrow-heads on its boundary point round in the clockwise direction, and negative when they point round in the counter-clockwise direction. Thus in the figure, the area of the loop bounded by the curve passing through the points 0, 1, 2, 3, 4, 8, 9, 10, 11, 12, is positive, and the area of the small loop, bounded by the curve 5, 6, 7, is negative.

If the area is measured with a planimeter, it is only necessary to run the tracing point round the boundary of the projected curve in the direction 0, 1, 2......, the reading giving finally the algebraic sum of all the loops

To find the second coefficient, suppose the given curve to be wrapped twice round a cylinder whose circumference is half the length of the base of the given curve. Or what is more convenient in practice, suppose the drawing of the curve stretched to double its length and wrapped twice round the same cylinder used for the determination of  $B_1$ 

In general, to find  $B_m$ , suppose the drawing stretched to m times its length and wrapped round the same cylinder used for finding  $B_1$ . The projected curve will wind round the cylinder m times, forming numerous loops. But the area proportional to  $B_m$  is always given by guiding the tracing point of a planimeter round the boundary of the curve in the direction  $0, 1, 2, \dots$ . The value of  $B_m$  is the area measured in this way, suitably interpreted with regard to the vertical scale, divided by m times the length representing  $\pi$  on Fig. 193.

To find the coefficients of the cosmo series, the ordinates through 0 and  $2\pi$  of the given curve must coincide along the line ef. Fig. 195, when the drawing is wrapped round the cylinder, otherwise the process is carried out in precisely the same way.

Fig. 195 shows the curve projected in order to find the second coefficient, A<sub>2</sub>, in the cosine series.

The first term of the cosme series,  $A_{\bullet}$ , is simply the mean ordinate of the given curve.

162. Formulae for calculating the approximate values of the coefficients up to third multiple angle\*. For the special purpose of analysing a valve displacement curve of the kind belonging

<sup>•</sup> I am indebted to Dr Silvanus P. Thompson for the formulat of this article.

to gears which give a continuous motion to the valve, it is more than sufficiently accurate to divide the distance from 0 to  $2\pi$  into six equal parts and then to find the series (which will consist of a constant term and six other terms) whose graph will pass through the six points where the ordinates corresponding to 60, 120, 180, 240, 300, and 360 degrees respectively cut the actual displacement curve of the valve

The series is 
$$x = A_0 + A_1 \cos \theta + A_1 \cos 2\theta + A_3 \cos 3\theta + B_4 \sin \theta + B_2 \sin 2\theta + B_3 \sin 3\theta$$
.

The way to obtain these formulae is to form the series of simultaneous equations corresponding to the number of points, and then solve them, and this can be done without difficulty. Since, however, the ordinates are spaced 60 degrees apart, they all of them miss the  $\sin 3\theta$  component. To include this, therefore, draw an ordinate at 90 degrees and call its value  $x_{20}$ . The way to calculate the coefficients is as follows:

Write down the values of the ordinates in the following schedule and take their respective sums and differences as indicated.—

Then

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### 163. Examples of the representation of valve displacement irves by a series, neglecting all terms after the third multiple angle.

**Example 1.** Apply the method of the previous article to find the series representing the displacement curve, marked  $u=4\frac{1}{2}$ , of the Stephenson Link Motion, Fig. 86. Divide the vertical distance TT into six equal parts. Measure the ordinates corresponding to the angles 60, 120, 180, 240, 300, and 360 degrees and arrange them in the schedule form given in the previous article. Thus —

• 
$$x_1 = -1.98$$
  $x_2 = -0.99$   $x_3 = 1.03$ 
•  $x_4 = 1.80$   $x_5 = 0.80$   $x_6 = -1.03$ .
The sums are •  $z_1 = -0.18$   $z_2 = -0.19$   $z_3 = 0.$ 
The differences are  $d_1 = -3.78$   $d_4 = -1.79$   $d_4 = 2.06$ 

Therefore  $A_0 = -0.37 \div 6 = -0.0617$   $A_1 = \{-3.78 + 1.79 - 4.12\} \div 6 = -1.018$   $A_2 = \{-0.18 + 0.19\} \div 6 = 0.0617$   $A_3 = \{-3.78 - 1.79 - 2.06\} \div 6 = -0.0117$   $B_1 = \{-3.78 - 1.79\} \div 3.464 = -1.607$  $B_2 = \{-0.18 + 0.19\} - 3.464 = 0.00289$ .

The ordinate  $x_{00}$  corresponding to 90 degrees measures - 1.74 inches.

Therefore  $B_s = (-0.0617 - 1.607 - 0.0617 + 1.74) = 0.01$ .

The displacement, x, is therefore

$$x = -0.0617 - 1.018 \cos \theta + 0.0617 \cos 2\theta - 0.0117 \cos 3\theta$$

When  $\theta = 0$ , this reduces to

$$x_0 = -1.0297$$
.

 $-1607 \sin \theta + 00289 \sin 2\theta + 001 \sin 3\theta$ .

When  $\theta = 180$ , it reduces to

$$x_{\text{inc}} = +1.0297$$
.

This confirms the accuracy of the work, since the axis TT was placed so that the displacements should be the same at these two points.

**Example 2.** The displacement curve, marked  $u = 4\frac{1}{2}$ ", of the Alian Straight Link Motion, Fig. 110.

It makes the calculations slightly easier regarding signs, if the measurements are taken from a line parallel to the axis TT, but moved to the left, a distance a, so that all the ordinates to the curve are to the right of the axis, and therefore are all of positive sign. The distance a is then to be subtracted from the constant term in the series in order to obtain the constant term with reference to the axis TT. The coefficients are not affected by the position of the axis.

The measurements of six equidistant ordinates, to the curve  $u = 4\frac{\pi}{4}$ . Fig. 110, corresponding to angles 60, 120, 180, 240, 300, and 360, taken from a line parallel to TT, but displaced  $2\frac{\pi}{4}$  to the left of it, are

$$x_1 = 0.55$$
  $x_2 = 1.76$   $x_3 = 3.77$   $x_4 = 4.25$   $x_5 = 3.04$   $x_6 = 1.28$ 

The sums are  $z_1 = 4.80$   $z_2 = 4.80$   $z_4 = 5.00$ . The differences are  $d_1 = -3.70$   $d_2 = -1.28$   $d_3 = 2.54$ .

Applying the formulae of the previous article,

$$A_0 = 24383$$
  
 $A_1 = -1.25$   
 $A_2 = 0.0666$   
 $A_4 = -0.02$   
 $B_1 = -1.437$   
 $B_2 = 0$ 

The ordinate  $x_{m}$ , corresponding to 90 degrees, measures 0.94. Hence  $B_{s} = -0.01$ .

Subtracting 2.5 from A., to change the axis to TT.

$$A_{\bullet}$$
 with regard to the axis  $TT = 2.4333 - 2.5 = -0.0667$ .

Hence the displacement, x, is given by

$$\mathbf{x} = -0.0667 - 1.25\cos\theta + 0.0666\cos2\theta - 0.02\cos3\theta$$

$$-1.437\sin\theta - 0.01\sin3\theta$$

**Example 3.** The displacement curve corresponding to the simple valve gear in combination with a rocking shaft, shown by full lines in Fig. 52, is

$$\begin{aligned} x &= -0.024 - 0.955\cos\theta + 0.0283\cos2\theta + 0.02\cos3\theta \\ &- 1.075\sin\theta + 0.101\sin2\theta + 0.037\sin3\theta \end{aligned}$$

These expressions may be used to find the velocity and the acceleration of the valve with great accuracy. Thus, the general expression for the displacement is

$$\boldsymbol{x} = A_0 + A_1 \cos \theta + A_2 \cos 2\theta + \dots + A_n \cos n\theta + B_1 \sin \theta + B_2 \sin 2\theta + \dots + B_n \sin n\theta.$$

Differentiating with regard to the time and writing  $\frac{d\theta}{dt} = \omega =$ the assumed constant angular velocity of the crank shaft,

$$\mathbf{v} = \frac{dx}{dt} = \mathbf{\omega} \left( -A_1 \sin \theta - 2A_2 \sin 2\theta + \dots + nA_n \sin n\theta + B_1 \cos \theta + 2B_2 \cos 2\theta + \dots + nB_n \cos n\theta \right).$$

Differentiating again to find the acceleration,

$$\frac{dv}{dt} = \omega^* \left( -A_1 \cos \theta - 4A_2 \cos 2\theta + \dots + n^2 A_n \cos n\theta - B_1 \sin \theta - 4B_2 \sin 2\theta + \dots + n^2 B_n \sin n\theta \right).$$

Applying these expressions to the displacement curve in Example 1 of the present article,

• 
$$v = \omega (1.018 \sin \theta - 0.123 \sin 2\theta + 0.035 \sin 3\theta - 1.607 \cos \theta + 0.58 \cos 2\theta + 0.03 \cos 3\theta),$$

and the acceleration is

$$a = \omega^{2} (1.018 \cos \theta - 0.247 \cos 2\theta + 0.105 \cos 3\theta + 1.607 \sin \theta - 0.115 \sin 2\theta - 0.09 \sin 3\theta).$$

164. Formulae for calculating the approximate values of the coefficients up to the second multiple angle. Examples.

**Equivalent eccentric.** To obtain formulae for the coefficients, let  $x_1, x_2, x_3, x_4$  be the ordinates corresponding respectively to angles of 90, 180, 270, and 360 degrees. Introduce these coordinates successively in the equations

$$x = A_0 + A_1 \cos \theta + A_2 \cos 2\theta + B_1 \sin \theta + B_2 \sin 2\theta \dots (1),$$

thus forming four simultaneous equations from which the values of the several coefficients may be found. Since these ordinates are spaced 90 degrees apart, they all miss cutting the sne 20 component curve. To include this therefore take an ordinate at 45 degrees and call it  $x_{45}$ .

No difficulty will be found in solving these equations, and verifying the following expression. Write down the ordinates in the following schedule and take their respective sums and differences as indicated.

Then

$$A_{0} = (z_{1} + z_{2}) - 4$$

$$A_{1} = -d_{2} - 2$$

$$A_{2} = (z_{2} - z_{1}) - 4$$

$$B_{1} = -d_{1} - 2$$

$$B_{2} = -A_{0} - (A_{1} + B_{1}) 0707 + x_{G}.$$

**Example.** Apply these expressions to find the values of the coefficients in the case of the displacement curve, marked  $u = 4\frac{1}{2}$ ", of the Allan Link Motion, Fig. 110, which has already been analysed in Example 2 of the previous article up to the third multiple angle.

The values of the ordinates, measured from a base 2.5 from  $T\tilde{T}$ , Fig. 110, are

$$\begin{array}{lll} a_1 = & 0.94 & x_2 = 3.77 \\ a_3 = & 3.79 & x_4 = 1.23 \\ z_1 = & 4.73 & z_3 = 5.00 \\ d_4 = & -2.85 & d_2 = 2.54, \end{array}$$

Then

$$A_0 = 2.4325$$
  
 $A_1 = -1.27$   
 $A_2 = 0.0675$   
 $B_1 = -1.425$   
 $B_2 = 0.1625$ 

Subtracting 2.5 from  $A_a$ , to change the axis to TT,

 $A_0$  with regard to the axis TT = 2.4325 - 2.5 = -0.675.

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$$x = -900675 - 1.27 \cos \theta + 0.0675 \cos 2\theta - 1.425 \sin \theta + 0.1625 \sin 2\theta$$
 .......(2).  
When  $\theta = 0$  this reduces to  $x = -1.27$ , and when  $\theta = 180$  it reduces to  $x = +1.27$ .

It will be noticed that the constant term  $A_{\sigma}$  is equal and opposite in value to the coefficient of  $\cos 2\theta$ . This is only the case when the valve is set so that the displacements at the dead points are equal and opposite. In the family of displacement curves belonging to a reversing motion there is only one curve to which this condition strictly applies,

The axis from which valve displacements are measured in the case of the curve just analysed does not coincide with the centre of oscillation of the curve, or in fact with the centre of oscillation of any one of the family to which the curve belongs. It is drawn to bisect the horizontal distance between the points on the mad-gear displacement curve corresponding to the dead points. If the equation of the curve had been referred to an axis passing through its centre of oscillation, that is, an axis bisecting the horizontal distance between two points marking the ends of the maximum positive and maximum negative ordinate respectively, there would have been a slight difference in the value of the constant term  $A_0$ . In the consideration of the displacement curves of a link motion, it is more convenient to refer them all to one axis than to refer each to one axis through the centre of oscillation, since each curve has a different centre of oscillation.

This displacement curve has now been analysed in three ways. In the first way two terms only of the series were obtained and the coefficients corresponding to them were calculated from the dimensions of the gear. In the remaining two cases the actual displacement curve has been analysed, and four and six terms have been respectively

TABLE 14.

Allan Gear-Constants for full forward displacement curve.

	Α,	A <sub>1</sub>	.1,	A,	B <sub>1</sub> •	В,	$B_{ij}$
Art. 104, page, 203 Art. 163, page 345 Art. 164, page 347			0 0666	1	1:42 -1:437 -1:425	3	- 0 0 1

where

retained, and in addition there has been a constant term. It is instructive to compare the several values of the coefficients bearing in mind the substance of Article 154.

The series (2) written in its general form, namely,

$$x = -A_0 - A_1 \cos \theta + A_2 \cos 2\theta - B_1 \sin \theta + B_2 \sin 2\theta$$
 .....(1),

may be reduced to a form which is useful for certain purposes.

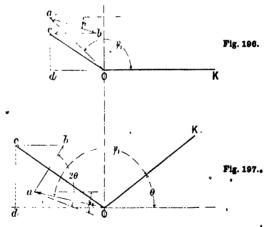
Thus, grouping the  $\theta$  terms together, and the  $2\theta$  terms together, and multiplying and dividing the  $\theta$  terms by the square root of the sum of the squares of their coefficients, and doing the same with the  $2\theta$  terms, the series may be written

$$\mathbf{z} = -A_0 + \rho_1 \cos(\theta + \psi_1) + \rho_2 \cos(2\theta - \psi_3) \dots (2),$$

$$\rho_1 = \sqrt{A_1^2 + B_1^2},$$

$$\rho_2 = \sqrt{A_2^2 + B_2^2},$$

 $\psi_1 = \tan^{-1} \frac{B_1}{-A_1}$   $\psi_2 = \tan^{-1} \frac{B_2}{A_2}.$ 



EQUIVALENT ECCENTRIC WHICH INCLUDES THE SECOND HARMOFIC.

This shows that the displacement, x, is the vector sum of  $-A_{\bullet}$ , together with the projections of the equivalent eccentric  $\rho_1$  whose

angular advance is  $\psi_1$ , and of the equivalent eccentric  $\rho_1$  whose angular lag is  $\psi_1$ , the latter eccentric revolving twice as fast as the crink.

Let OK, Fig. 196, represent the crank at the 0 degree dead point. Then Oa is the position of the first equivalent eccentric, and adding the second to the end of this, ab is the corresponding position of the second equivalent eccentric. Adding now bc, to represent the constant term  $-A_{\bullet}$ , the vector Oc represents the single equivalent eccentric, whose projection Od is the valve displacement, x, at the dead point.

When the crank has turned through the angle  $\theta$ , Fig. 197, the line Oa has turned with it through the same angle, but the line ab has turned through twice the angle  $\theta$  from its initial position. The vector bc remains unchanged in direction, so that the line Oc is now the single equivalent eccentric whose projection Od is the valve displacement corresponding to the crank angle  $\theta$ . Thus the single equivalent eccentric is changing continuously both in magnitude and angular advance.

165 Modification of the Reuleaux valve diagram to find the displacement, x, for a given value of the crank angle  $\theta$ , when the displacement is given by

Mr J. Harrison has modified the Renleaux diagram, described in Article 53, so that the valve displacement may be found approximately, directly the crank angle is given, when the displacement curve has the above equation, providing that the radius of the secondary equivalent eccentric  $\rho_1$  is small compared with  $\rho_1$ . The displacement is measured from the central position of the valve, and in these circumstances the constant  $A_0$  assumes the approximate value

$$\rho_2 \sin{(2\delta_1 + \delta_2)}$$

as will appear presently.

Mr Harrison's construction is as follows

With centre C, Fig. 198, and radius  $\rho_i$  describe a circle, and let  $AA_1$  be the line of stroke, CA corresponding with the zero position of the crank. Set out the angle ACD below CA and equal to  $\delta_1$ , the angle  $A_iCO$  equal to  $\delta_1 + \delta_2$ , and make CO equal to  $2\rho_i$ . Diam CO at the given crank angle  $\theta$  with CA. Drop a perpendicular from P on to  $DD_1$ . Then the length of this perpendicular, namely PM, is very nearly the displacement, x, of the valve, corresponding with the given angle  $\theta$ .

For, denoting the small angle CPO by  $\beta$ ,

$$PM = CP \sin MCP = \rho_1 \sin (\delta_1 + \theta - \beta),$$

and expanding the expression.

$$PM = \rho_1 \sin(\delta_1 + \theta) \cos \beta - \rho_1 \cos(\delta_1 + \theta) \sin \beta \quad \dots \quad (2)$$

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Now in the triangle COP

$$\frac{CO}{\bar{U}\bar{P}} = \frac{\sin CPO}{\sin CO\bar{P}}.$$

$$\sin \beta$$

That is

$$\frac{2\rho_1}{\rho_1} = \frac{\sin \beta}{\sin (\delta_1 + \delta_2 - \theta)}$$

so that  $\rho_1 \sin \beta = 2\rho_1 \sin (\delta_1 + \delta_2 - \theta)$ . Substituting this expression for  $\rho_1 \sin \beta$  in (2), and writing unity for  $\cos \beta$ , since  $\beta$  is small,

$$PM = \rho_1 \sin (\theta + \delta_1) - 2\rho_2 \sin (\delta_1 + \delta_2 - \theta) \cos (\delta_1 + \theta).$$

Splitting the product of the sine and cosine into the sum of two sines,

$$PM = \rho_1 \sin (\theta + \delta_1) - \rho_2 (\sin 2\delta_1 + \delta_2) - \rho_2 \sin (\delta_2 - 2\theta),$$

or  $-PM = \rho_2 \sin(2\delta_1 + \delta_2) - \rho_1 \sin(\theta + \delta_1) - \rho_2 \sin(2\theta - \delta_2) \dots (3).$ 

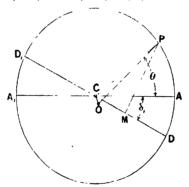


Fig. 198. HARRISON'S MODIFICATION OF THE REULEAUX DIAGRAM TO a INCLUDE THE SECOND HARMONIO.

Comparing this expression with equation (1) at the beginning of the article, it is apparent that -PM is equal to the displacement x, provided that the constant

$$A_0 = -\rho_2 \sin{(2\delta_1 + \delta_2)}.$$

Referring to Fig. 198 again, it will be seen that the constant  $A_0$  is equal to half the perpendicular distance from O to  $DD_1$ ; and since  $DD_1$  is a diameter, the maximum displacements are equal and opposite, that is to say, the perpendicular PM measures the displacement,  $x_0$  from the central position of the valve.

The displacements at the dead points are unequal, hence the valve must have unequal laps to obtain equal leads. If the constant  $A_{\bullet}$  is zero, the line  $DD_{\bullet}$  must be replaced by a parallel line bisecting CO.

This would be the case for diagrams giving in a similar way the velocity and acceleration of the valve

The displacement of the piston from its central position may also be obtained from a diagram constructed according to the above rule suitable modifications being made in the values  $\rho_1$ ,  $\rho_2$ ,  $\delta_1$ , and  $\delta_3$ . Thus, referring to Article 152, it will be seen that the displacement of the piston from its central position is given very nearly by

$$X = R\cos\theta - \frac{R^2}{4l}\cos 2\theta + \frac{R^4}{4l}.$$

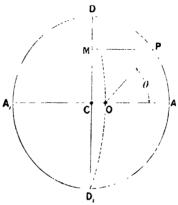


Fig. 199. Diagram for Piston Displacement to include the Second Harmonic

Changing the cosines to sines, and writing u for the ratio  $\frac{t}{R'}$ 

$$X = R \sin(\theta - 90) - \frac{R}{4\pi} \sin(2\theta + 90) + \frac{R}{4\pi}$$

Comparing this with equation (1) of this article, it will be seen that

$$\rho_1 = -R_1$$

$$\rho_2 = \frac{R}{4n},$$

$$\delta_1 = -90^\circ,$$

$$\delta_2 = -90^\circ.$$

The diagram thus takes the form shown in Fig. 199, where CA = R, ACD is the angle  $\delta_i$  set out above CA because  $\delta_i$  is negative.

A diagram similar to Fig. 199 was published in Engineering, Nov. 22, 1889, by Mr O. A. C. Bremma.

The line CO makes with  $CA_1$  an angle  $\delta_1+\delta_2=-180$  degrees; and CO is made equal to  $\frac{R}{2n}$ .

The crank is now supposed to revolve about the point O and to very continuously in length, so that when it stands at the angle  $\theta$  with OA, PM, the perpendicular from P to DD is the displacement.

The point O may be found at once by the geometrical method already used, namely, with a radius equal to the length of the connecting rod draw the arc, shown dotted, through the points D and  $D_1$ , cutting the line of stroke in the point O. The distance CO is equal to  $\frac{R}{2n}$ , as will be seen from Fig. 68, supposing  $\theta$  to be 90 degrees.

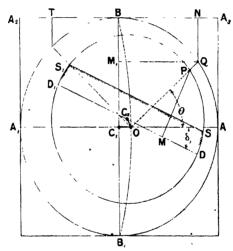


Fig. 200. Harrison's combination of the Reuleaux modified diagram with the piston diagram to form a valve diagram in which the second harmonics from both the piston and the valve gear are included.

If the two diagrams, namely Fig. 198, and Fig. 199, be superposed so that the point O in each coincides, and the horizontal line  $AA_1$  in the one is parallel to the horizontal line  $AA_1$  in the other, a valve diagrams is obtained from which the simultaneous values of the valve and pristoric displacements may be obtained. This combination of the two diagrams is shown in Fig. 200, where also the steam lap line SS' corresponding to the instroke cycle is added.

## Trigonometric representation of Valve Cyrves 355

Summarising the two preceding rules for drawing the diagrams, the following is the rule for the combined diagram —

• With centre  $C_1$  and radius R diam a circle to represent the crank circle. Draw  $AC_1A_1$ , the line of stroke. Make  $C_1O$  equal to  $\frac{AC_1}{2n}$ . Set out the angle  $AOC_2$  equal to  $\delta_1 + \delta_2$ , making  $OC_2$  equal to  $2\rho_2$ . With centre  $C_2$  and radius  $\rho_1$  diam the valve circle, and draw the diameter  $DC_2D_1$ , making a negative angle  $\delta_1$  with  $C_1A$ .

The erank is now supposed to revolve about the point  $O_i$  and it  $\theta$  is the angle it makes with the line of stroke, PM is the valve displacement occurresponding to the piston displacement  $QM_1$ 

The piston displacement may be projected upwards, as shown on to the line  $A_2A_3$ , the point B marking the centre of the stroke

The line  $SS_1$  is drawn parallel to  $DD_1$  at a distance therefrom equal to the steam lap for the instroke.

The point of cut-off,  $T_i$  is thus at once obtained from the diagram. By adding lines parallel to  $DD_i$  corresponding with the steam Lip for the outstroke cycle, and the two exhaust Lips, all the events of the stroke can be found from the diagram.

Mr Harrison points out that this diagram indicates the conditions in which a  $2\theta$  term in the valve curve tends to correct the inegularities of steam distribution due to the finite length of the connecting rod. Thus, from the diagram it will be apparent that if the piston and valve encles were coincident, the distribution would be symmetrical in the two cycles, with equal laps. The conditions that the two encles may be coincident are

$$(\delta_1 + \delta_2) = 0$$

and

$$\rho_2 = \frac{-\rho_1}{4n} .$$

Or again

$$(\delta_1 + \delta_2) = \pm 180 \text{ degrees}$$

and

$$\rho_1 = \frac{\rho_1}{4n}$$

#### APPENDIX.

#### MEASUREMENT OF THE ANGULAR ADVANCE.

Assuming the engine to be provided with a flywheel or crank disc, turned on the rim, the following method may be used to find the angular advance with great accuracy.

Using a transmel of the kind illustrated in Fig 10, and in the way explained in Art. 19, page 18, mark the dead points of the valve's motion on the valve spindle, whilst the engine is being barred round. Fix these points by small centre dots and bisect the distance between them, placing a centre dot in the mid-position. Then, holding the transmel against the spindle whilst the engine is being barred round, stop the barring when the transmel point drops into the middle of the three centre dots. The engine now stands in the position where the valve is exactly in the middle of its travel. Using a transmel of the kind shown at DC, Fig 37, page 55, mark the rim of the wheel (not the three centre dots. The engine is centre dot. Call this dot V.

Assuming the crank web to be accurately machined, bar the engine round again until the crank stands vertical, the vertical position being determined by a spirit level square held against the web. Mark the rim of the wheel with the transmel and put in a centre dot. Call this P. Then, assuming an infinitely long eccentric rod, the angle presponding to the arc VP is the angle between the crank and the centric radius, since the eccentric radius and the crank radius were their respective vertical positions when they passed the training that, which may be imagined always held against the wheel rim as an index. To find the angle corresponding to the arc PV, measure the number of the wheel by means of a thin steel tape; and then have the length of the arc PV. Then

 $\frac{2\pi \times PV}{\text{circumference}}$ 

the circular measure of the angle, and this can be converted into

degrees by the multiplier 57:296 or by the use of a table given in most books of mathematical tables. The result should be corrected for the obliquity of the eccentric rod, and the method of doing this will be clearly seen from Fig. 201.

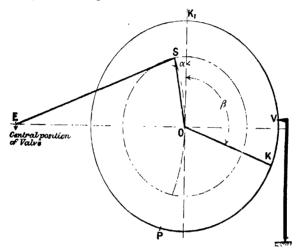


Fig. 201. Measurement of the Angular Advance.

The figure shows the position of the eccentric radius OS when the valve is in the middle of its travel, the eccentric rod SE being taken very short in order to exaggerate the error. Let V be the position of the centre dot made on the run of the which, or crank disc, when the valve is at the centre of its travel. Let OK represent the crank.

Then when the crank is turned into the vertical position, that to  $OK_1$ , the crank shaft turns through the angle  $KOK_1 = \beta$ , and the transition of the white that the arc PV divided by the radius of the wheel, measures the angle that the arc leaving less than the angular advance by the angle  $\alpha$ . Letter angle may be calculated by means of equation (5), page 116, inserting the proper ratio between the eccentric radius and the eccentric radius and putting f = 0, obtaining thus the angle between the eccentric radius and the line of stroke when the valve is in its position. The angle  $\alpha$  is found by subtracting  $90^{\circ}$  from this

If the engine is a vertical one the dot P is to be made when the rank webs are in the horizontal position

In an actual case the distance between the two dots P and  $V_i^*$  neasured by a steel tape laid flat on the rim of the wheel, is 82.25 nches. The circumference of the wheel measured in the same way s 227.25 inches. Hence the angle  $\beta$  in degrees is given by

$$\frac{8225 \times 6282 \times 57296}{22725} = 130\frac{1}{2} \text{ degrees}$$

The ratio of the length of the eccentric rod to the eccentric radius is 30 to 1. Hence from equation (5), page 116,

$$\cos \theta = 30 - \sqrt{901} = -0.0166$$
.

This is the cosme of an angle of 90 degrees 57 minutes, so that the nagnitude of the angle  $\alpha$  is 57 minutes. Call this 1 degree. Then the rue angular advance is 131½ degrees.

If the crank webs are not machined accurately the mark P may be out on the wheel rim when the piston is in the middle of its stroke, the ingme being set in this position in exactly the same way as that just explained for the valve. That is to say a trammel must be made and the dead points of the stroke marked off with it on the piston rod is the engine is barried round. The distance between these two points s to be bisected and the engine then barred round until the trail point drops in the middle dot. The mark P on the wheel will in this ase not correspond to either a vertical or horizontal position mank but to the crank position corresponding to the middle posihe piston. A correction must accordingly be made for the obline the connecting rod. It can easily be seen that if  $\theta_s$  is the and the eccentric sheave makes with the line of stroke when the value its central position, calculated from equation (5), page 116, and 🚱 🦓 angle which the crank makes with the line of stroke when the in its central position, also calculated from equation (5), page 1 the true angular advance is

$$\beta - (\theta_c - \theta_s)$$

 $\mathcal{B}$ , as before, representing an angle equal to the angle subtended by the arc PV. This latter method is the most accurate of the three methods given (namely one on page 55 and the two above) because the respective transmels fix the central position of the piston and the valve when both have the maximum velocity ratio to the crank pin.

In applying this method care must be taken that when the crank shaft is turned, the valve spindle and the piston move away from their mid-positions in the same direction, otherwise the angular advance will be nearly 180 degrees wrong. Also the online must always be turned in one direction. If in placing the transmel point, the und-position is overshot, the engine must be barred the whole way round again in the same direction. If this point is not attended to the slackness in the joints of the gear introduces sensible error into the result

When the crank shaft carrying the sheave, keyed in its proper place, is detached from the engine, the angular advance of the sheave may be measured in the way illustrated in Fig. 202. The crank shaft is to be supported in V blocks and the crank placed horizontally. A fine string, or better a piece of flat steel like the material used for steel tapes, is to be hung over the sheave with suitable weights attached to the free ends. A similar string or tape is to be placed over the crank shaft

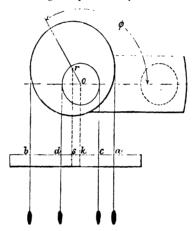


Fig. 202. The Setting of an Ecopsisic Suparc

**Extraight** edge, or strip of wood or steel, is then held near the strings and the lines, coincident with the strings through the points a, c, d, b, are the marked on it. These marks record the horizontal distances between the strings. It will be seen at once that the point s, which bisects the distance ab, is vertically under the centre of the sheave r; and that the point k, which bisects the distance cd, is vertically under the centre of the shaft O. Hence the distance sk is the horizontal projection of the coentric radius, and if  $\phi$  is the angular advance

 $sk = r \cos \phi$ ,

from which of can be found when sk and the eccentric radius are

measured. If the eccentric radius is not otherwise known it may be found by slowly turning the crank shaft in the V's and measuring the maximum value of sk.

When the angular advance is given the quantity sk can be calculated, and with the known diameter of the sheave and the crank shaft the four lines may be set out on a board or steel strip. This strip may be used to setting the eccentric sheave in the proper position on the shaft. For this purpose the strip is clamped in position so that the strings over the crank axle coincide with the lines c and d, and then, the crank being horizontal, the eccentric sheave is turned on the shaft until the strings hanging from it are brought into coincidence with the lines at a and b. The keyway is then marked off on the shaft, to be subsequently cut and fitted with the key.

There are other ways of measuring the angular advance, and other ways of setting the sheave at the proper angle with the crank, and a student will have no difficulty in devising ways for himself to meet any peculiarity of design.

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